

Lab Assignment 6, 05/09/2019, 1800 -- 2000

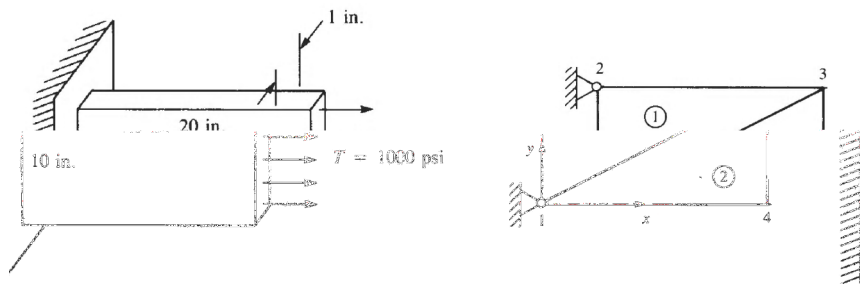
**Due 2000**

**Lab Grading Policy: Attendance 20%, Score 80%, Bonus 20%**

You are expected to complete the basic part during the Lab. In case you have difficulty in finishing the basic part on time, you should upload them before 2100 on Saturday and a penalty of 20% discount will be applied on your score. You are encouraged to complete the bonus part (no penalty applied). Basic and/or bonus parts should be submitted by **2100 on Saturday and no late submission is permitted**. We will in general post the reference solutions by **Sunday**.

Download T3Simple.zip from the course website and unzip it. You will find a folder containing a problem2dTensile.m file with four functions, formStiffness2D.m solution.m outputDisplacements.m, drawingMesh.m.

- (40%)** Modify the MATLAB codes to calculate the element stresses and to draw the undeformed and deformed configurations. In drawing the deformed configuration, allow users to specify the magnification factor. Below is a sample run for the thin plate example subjected to the surface traction with two T3 elements ( $E = 30\text{Mpsi}$  and  $\nu = 0.3$ ):



```
Displacements
Node      UX      UY
  1      0.0000e+00  0.0000e+00
  2      0.0000e+00  0.0000e+00
  3      6.0958e-04  4.1633e-06
  4      6.6370e-04  1.0408e-04
```

```
Stress in element 1
Sigma_xx : 1004.803843
Sigma_yy : 301.441153
Sigma_xy : 2.401922
```

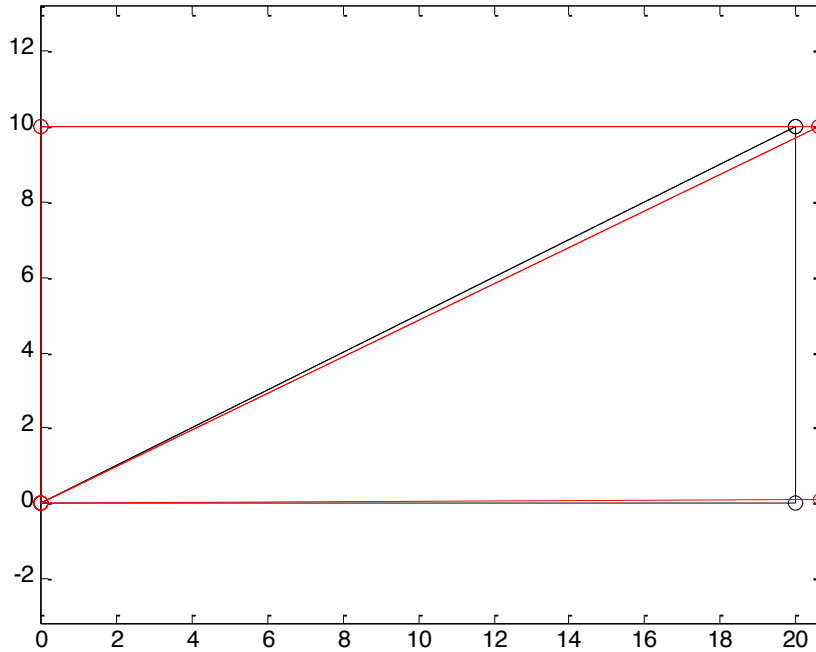
```
Stress in element 2
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```

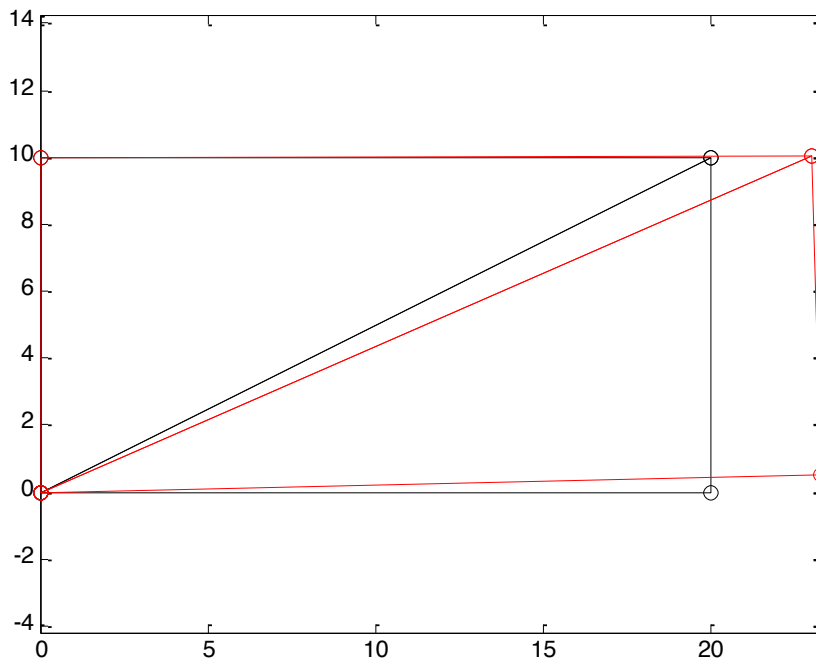
| Sigma_xx : 995.196157
| Sigma_yy : -1.200961
| Sigma_xy : -2.401922

```

Magnification Factor = 1000

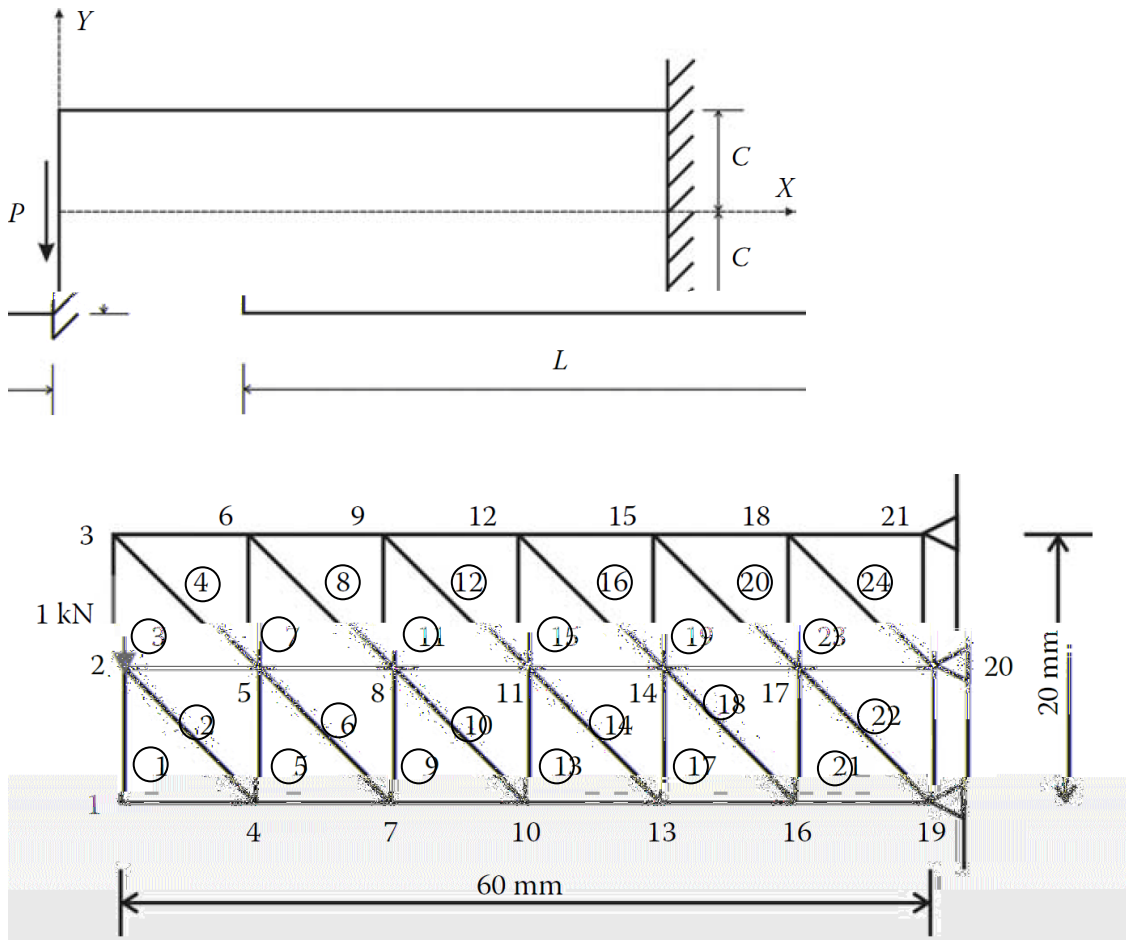


Magnification Factor = 5000

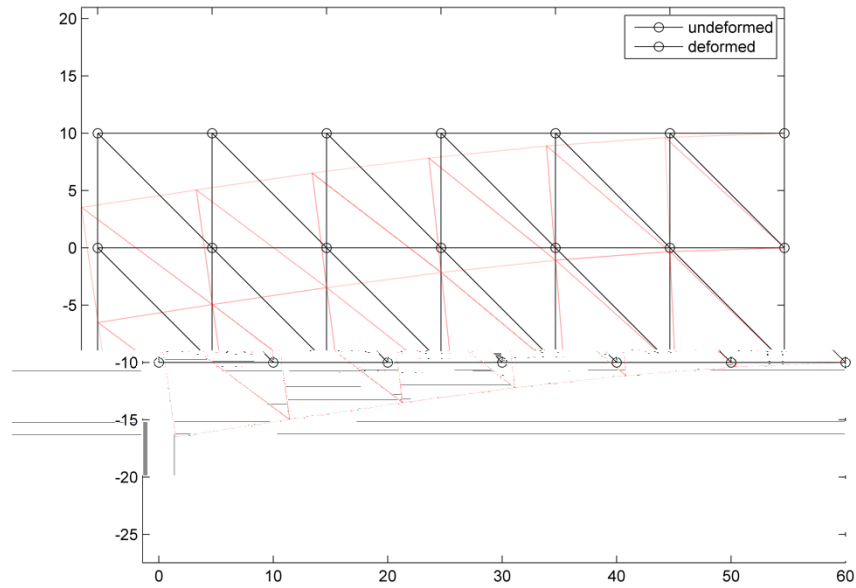


2. **(40%)** Consider a cantilever subjected to a concentrated load as shown below. Let us consider it as a plane-stress problem where  $C = 10$  mm,  $L = 60$  mm,  $t = 5$  mm for the geometrical

properties, a Young's modulus of 200,000 MPa and a Poisson's ratio of 0.3 for the material properties, as well as a concentrated force  $P$  of 1000 N. We will use 24 elements to discretize the domain as shown in the figure below. The nodes numbered 19, 20, and 21 represent the fixed end. The concentrated force  $P$  is applied at node 2.



(a) Plot the undeformed and deformed (magnification factor = 100) configurations. Below is a sample plot:



(b) Report the nodal displacements, reactions and element stresses. Below is a sample output:

Displacements

Node	UX	UY
1	1.4508e-02	-6.4933e-02
2	3.2805e-04	-6.5208e-02
3	-1.4239e-02	-6.4714e-02
4	1.4233e-02	-4.9732e-02
5	1.8295e-04	-4.9453e-02
6	-1.3836e-02	-4.9409e-02
7	1.2974e-02	-3.5050e-02
8	1.3798e-04	-3.4663e-02
9	-1.2672e-02	-3.4756e-02
10	1.0922e-02	-2.1992e-02
11	8.9523e-05	-2.1487e-02
12	-1.0700e-02	-2.1696e-02
13	8.0808e-03	-1.1348e-02
14	2.5642e-05	-1.0726e-02
15	-7.9099e-03	-1.1048e-02
16	4.4638e-03	-3.8838e-03
17	-6.6359e-05	-3.1907e-03
18	-4.2651e-03	-3.6637e-03
19	0.0000e+00	0.0000e+00
20	0.0000e+00	0.0000e+00
21	0.0000e+00	0.0000e+00

Reactions

node	reactions
37:	-2.9520e+03
38:	-1.3524e+02
39:	-9.6009e+01
40:	-2.7235e+02
41:	3.0480e+03
42:	1.4076e+03

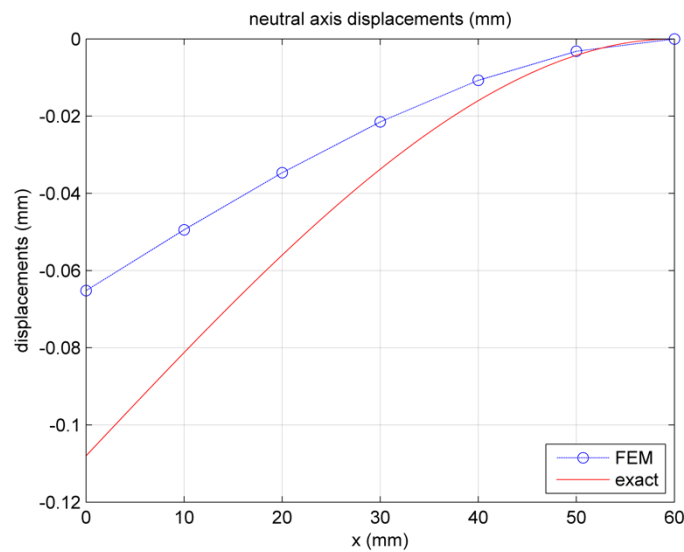
Stress

Node	sigma_xx	sigma_yy	tau_xy
1	-7.8546e+00	-7.8546e+00	7.8546e+00
2	-1.3515e+00	5.1683e+00	1.3112e+01
3	6.6118e-02	9.8937e+00	9.1400e+00
4	9.1400e+00	3.6192e+00	9.8937e+00
5	-2.5827e+01	-2.1744e+00	4.8607e+00
6	1.5601e+00	8.1980e+00	1.5027e+01
7	-6.9913e-01	6.6741e-01	5.9323e+00
8	2.4966e+01	5.6374e+00	1.4180e+01
9	-4.2552e+01	-5.0356e+00	1.6983e+00
10	2.2662e+00	1.0785e+01	1.8024e+01
11	-1.6757e+00	-2.3552e+00	2.8152e+00
12	4.1961e+01	8.4119e+00	1.7462e+01
13	-5.9121e+01	-7.6315e+00	-1.4550e+00
14	2.6997e+00	1.3258e+01	2.0813e+01
15	-2.7809e+00	-5.0108e+00	-2.2163e-01
16	5.9202e+01	1.1322e+01	2.0864e+01
17	-7.5391e+01	-1.0170e+01	-4.5429e+00
18	2.5481e+00	1.4627e+01	2.3117e+01
19	-4.1445e+00	-7.6816e+00	-3.0783e+00
20	7.6988e+01	1.3636e+01	2.4504e+01
21	-9.3536e+01	-1.4198e+01	-4.9720e+00
22	1.4584e+00	4.3753e-01	2.4544e+01
23	-1.6603e+00	-9.9582e+00	-7.7540e+00
24	9.3738e+01	2.8121e+01	2.8182e+01

(c) Plot the vertical displacement of the nodes situated along the neutral axis of the cantilever and compare the results with analytical solution that gives the vertical displacement of any point in the domain:

$$u_y = \frac{\nu Pxy^2}{2EI} + \frac{Px^3}{6EI} - \frac{PL^2x}{2EI} + \frac{PL^3}{3EI}$$

Below is a sample plot:



3. **(Bonus, 20%) You need to finish Problem 2.** Plot a contour of the longitudinal stress  $\sigma_{xx}$  from Problem 2 using the MATLAB patch function. Below is a sample plot:

