

X-ray Diffraction for powder sample

Rigaku Corporation
Application laboratory
Keigo Nagao

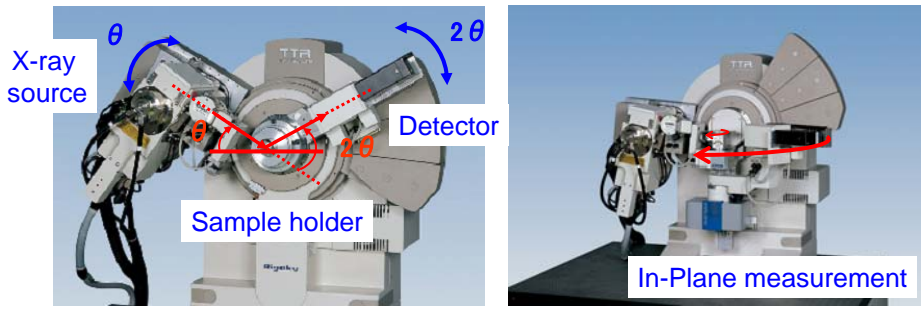


Today's topics (AM)

- Features of Rigaku TTRAXIII
- Basics of powder XRD
 - Feature of XRD
 - Evaluation item
- Texture analysis for bulk sample
 - Measurement and Process
- SAXS for nano-size sample
 - Principle and Optics
 - Application



Rigaku TTRAXIII



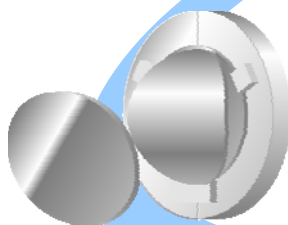
(2θ χ / ϕ scan)

- Horizontal goniometer
- High power X-ray source
- Parallel beam method
- In-Plane axis



In case the sample isn't set to horizontal....

Hard-to-pack sample



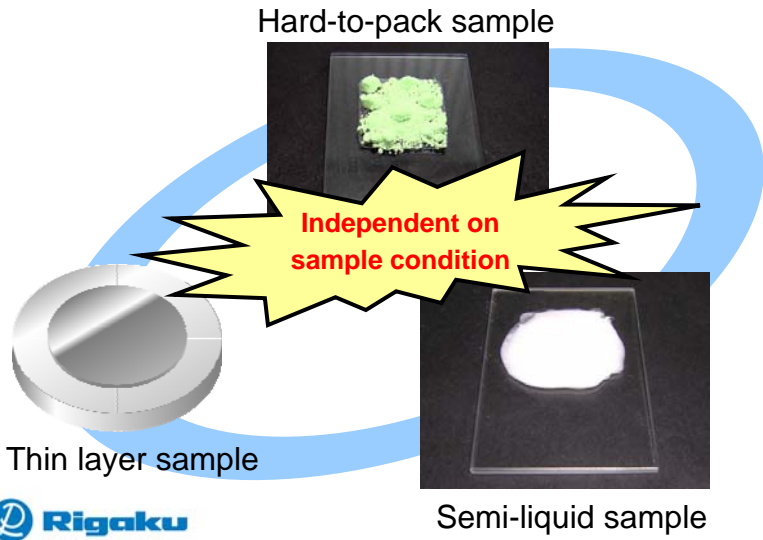
Thin layer sample



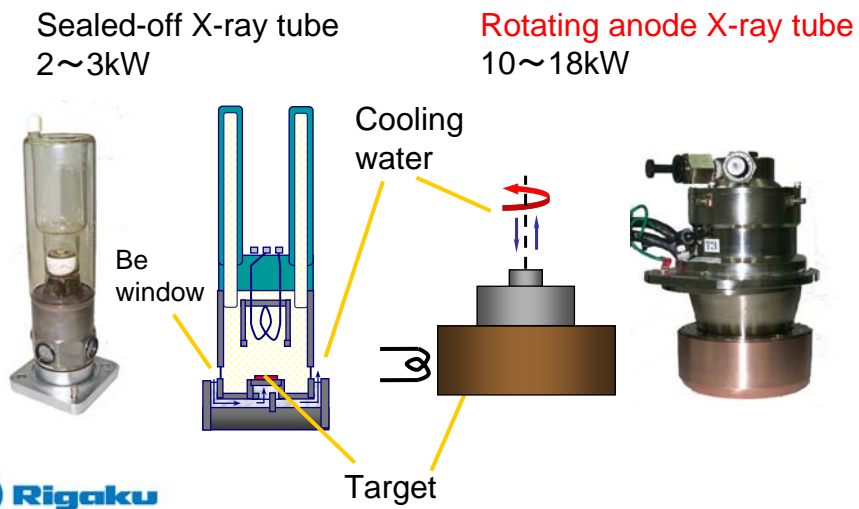
Semi-liquid sample



In Horizontal goniometer



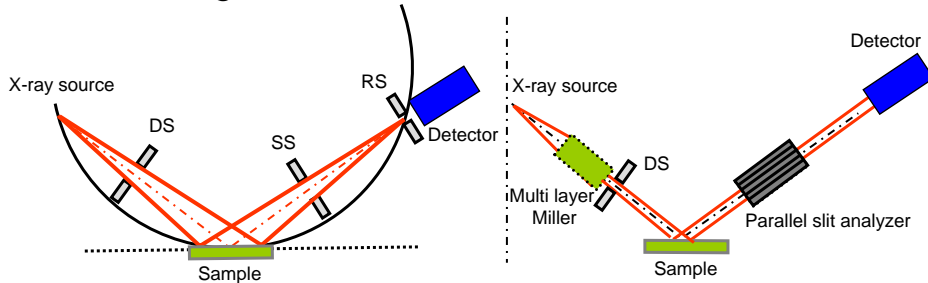
High power X-ray source



Geometry for powder sample

● Focusing method

■ Parallel Beam



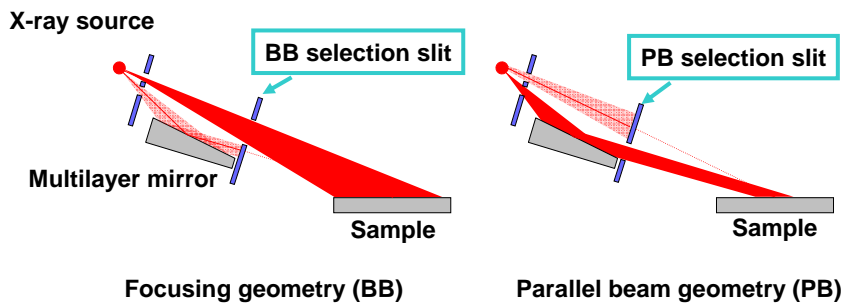
	Focusing method	Parallel beam
Systematic error	1. Flat sample 2. Umbrella effect 3. Adsorption effect 4. Eccentric error	Umbrella effect
Intensity	Strong	medium



Cross Beam Optics

Rigaku patented technology

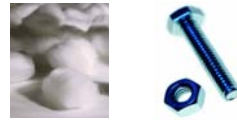
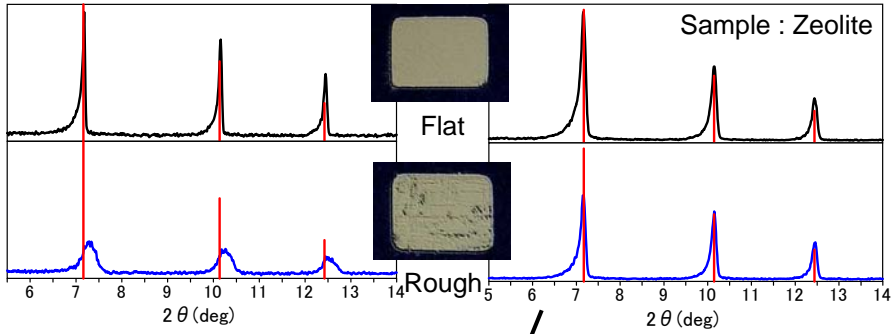
BB and PB geometries are simultaneously mounted, aligned, and selectable.



Measurement of rough sample surface

Focusing method

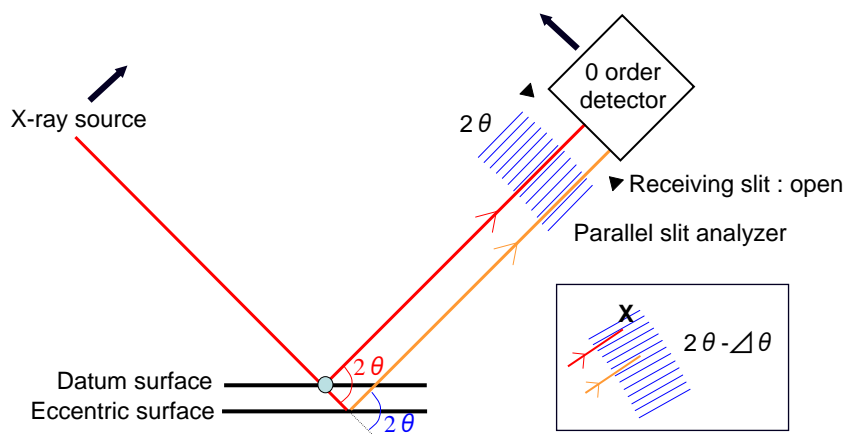
Parallel beam



Hold of peak shape, peak position and FWHM



Free from Eccentric error (Parallel beam)

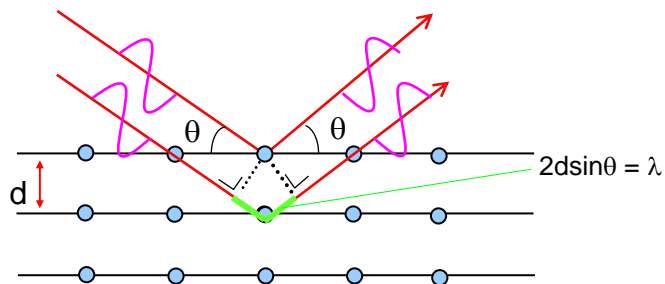


Interaction of substance and X-ray :1

Bragg's condition of diffraction

- The conditions for a reflected (diffracted) beam are given by the relation

$$2d\sin\theta = n\lambda \quad \text{Bragg's equation}$$



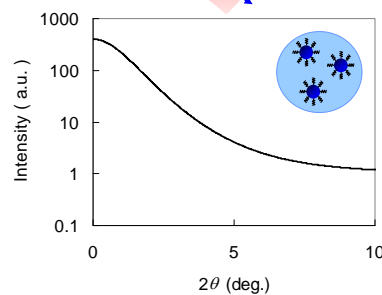
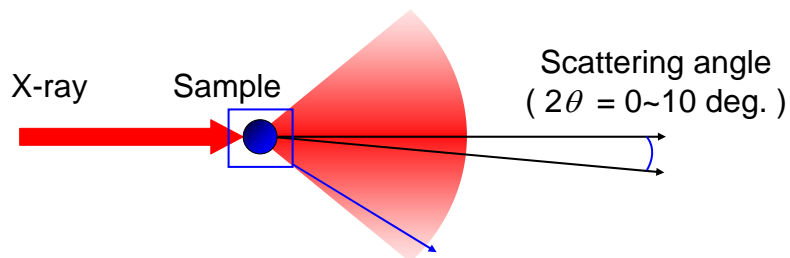
d: Interplanar spacing
 theta: Bragg angle

lambda: X-ray wavelength
 n: 1,2,3...



Interaction of substance and X-ray :2

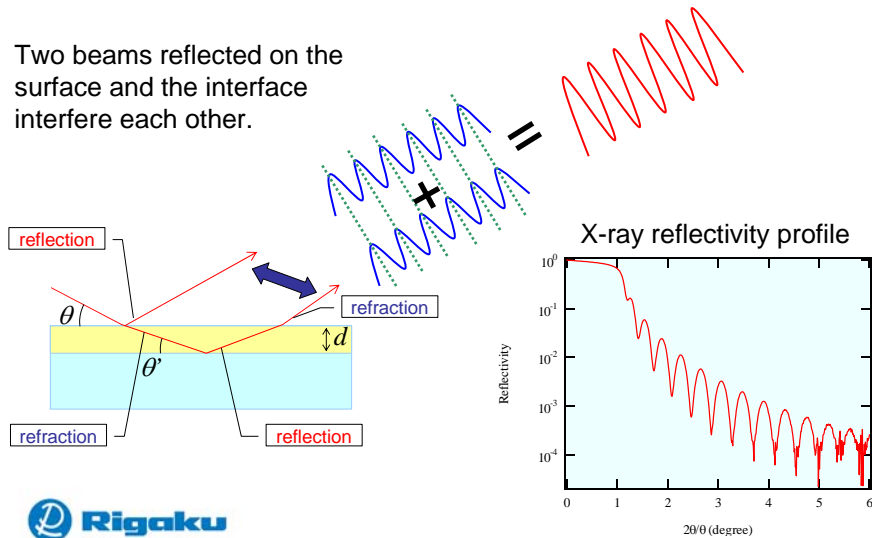
X-ray diffuse scattering



Interaction of substance and X-ray :3

Reflection and interference

Two beams reflected on the surface and the interface interfere each other.



Evaluation item in powder sample

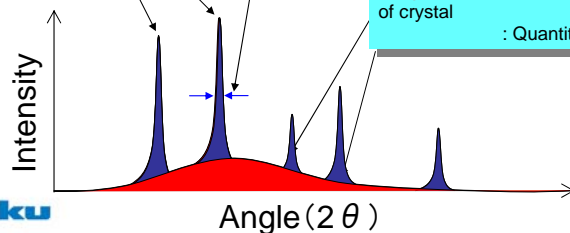
- (more than $2\theta = 5\text{deg}$)

Peak positions
 d values : Phase Identification
 Lattice constant
 d shift : Residual stress
 Solid solution

FWHM
 Crystal quality
 Crystallite size
 Lattice strain

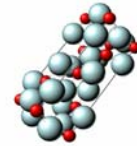
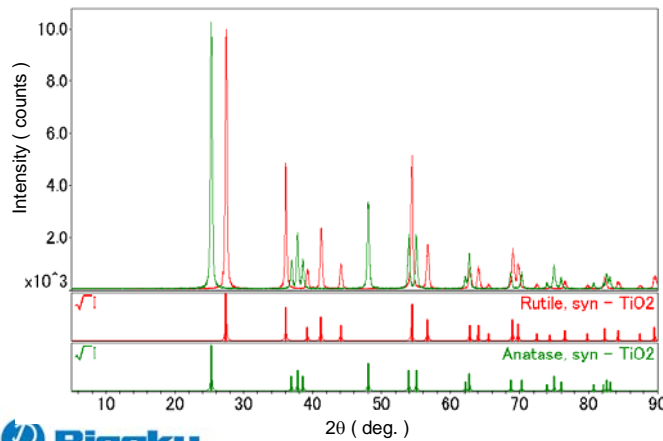
Intensity vs. Orientation
 Preferred orientation
 Fiber structure
 Pole figure

Integrated Int. of amorphous
Integrated Int. of crystal
 } Crystallinity
 : Quantitative analysis



Phase Identification in X-ray diffraction

- The powder diffraction pattern is characteristic of the substance
- The diffraction pattern indicates the state of chemical combination



Anatase
(Photocatalyst etc)

TiO₂



Rutile
(Cosmetic etc)

Quantitative analysis(RIR method)

The concentration of each phase is calculated by integrated intensity and RIR value

Polymorphs of TiO₂

Rutile (RIR:3.40)

Anatase (RIR:3.30)

Brookite

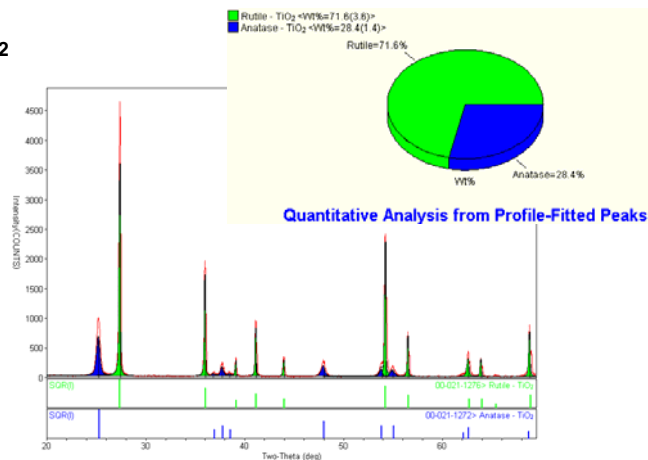
Preparation

Rutile:Anatase=3:1

Result

Rutile: 71.6wt%

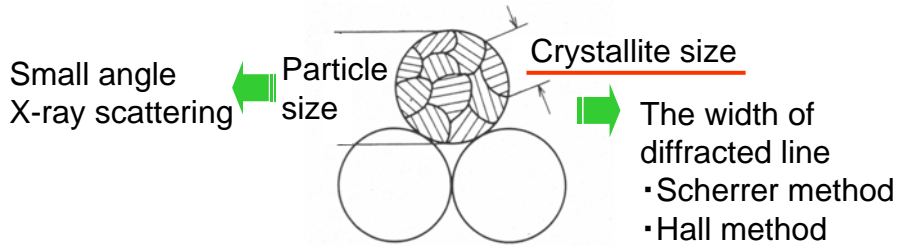
Anatase: 28.4wt%



Crystallite size

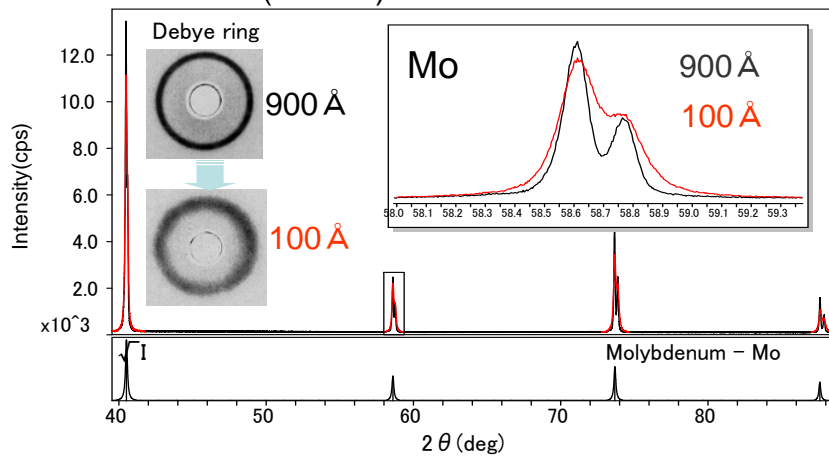
Polycrystal

There is one or multiple crystalline in one particle.



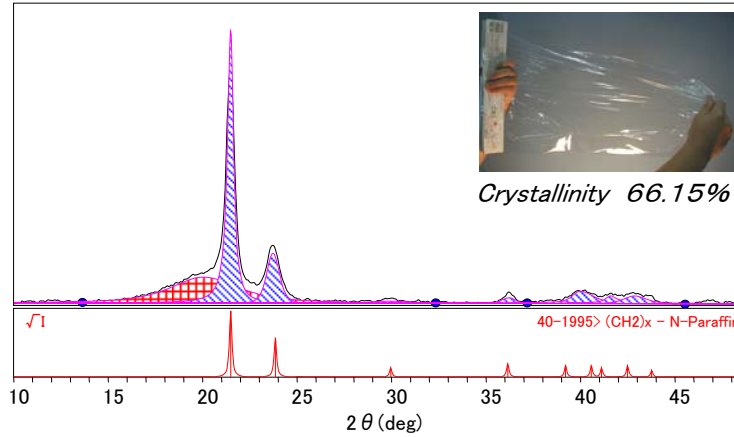
Crystallite size -Mo-

The width of diffracted line broaden in crystallite size less than 100nm(1000 Å)

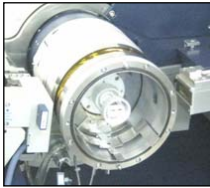


Crystallinity

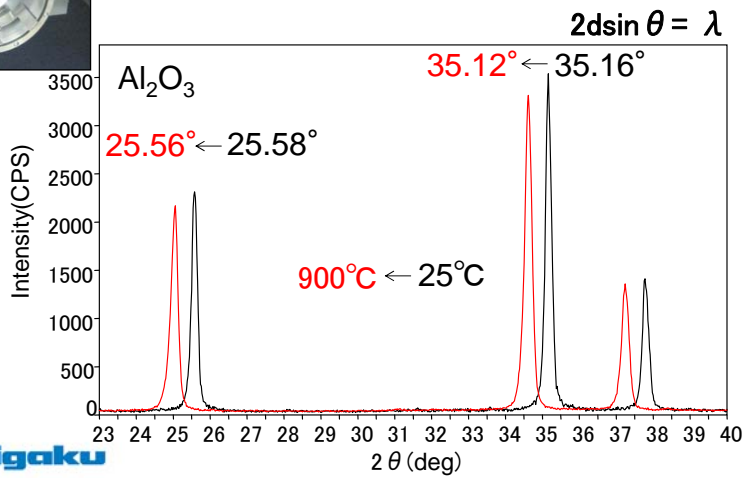
Plastic wrap



Change of lattice constant

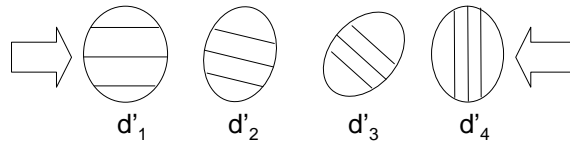


Monitoring the change of lattice constant in real time
→ in situ measurement

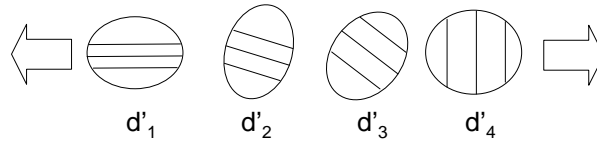


Stress and interplanar spacing

Compressive stress $d'_1 > d'_2 > d'_3 > d'_4$



Tensile stress $d'_1 < d'_2 < d'_3 < d'_4$

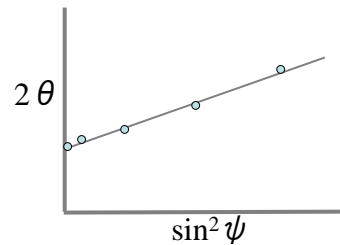
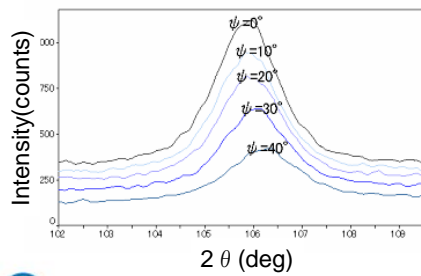
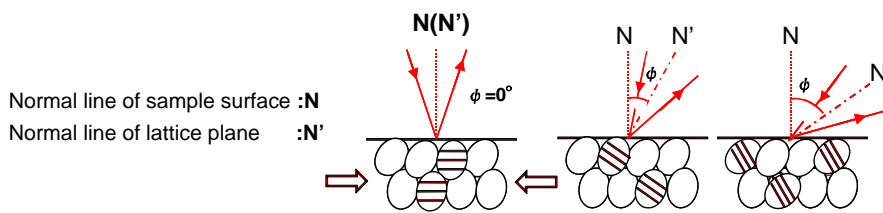


Bragg's condition of diffraction

$$2d \sin \theta = n \lambda$$



Peak shift and $\sin^2 \psi$ diagram



Calculation of stress value

$$\sigma \text{ (stress value)} = K \cdot \frac{\Delta 2\theta}{\Delta \sin^2 \psi}$$

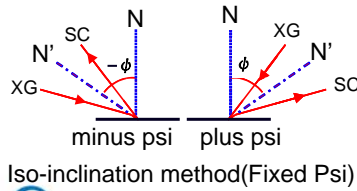
Slope of $\sin^2 \psi$ diagram

$$K \text{ (stress constant)} = \frac{-E}{2(1+\nu)} \cdot \cos \theta_0 \cdot \frac{\pi}{180}$$

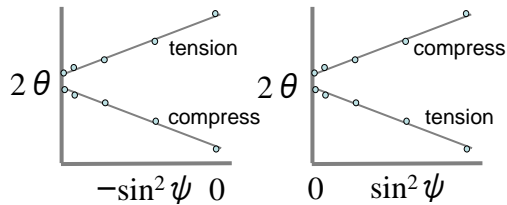
Material-specific value

{E : young's modulus, ν : poisson ratio,

θ_0 : diffraction angle in stress free condition}

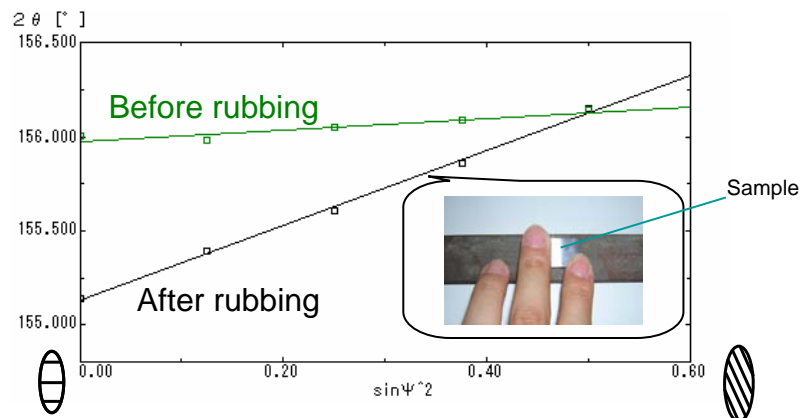


Iso-inclination method(Fixed Psi)



Measurement of residual stress

- Iron plate

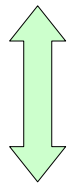


Texture evaluation and pole figure analysis for bulk sample



Texture and substance

Nonoriented sample : brick, concrete, (powder)



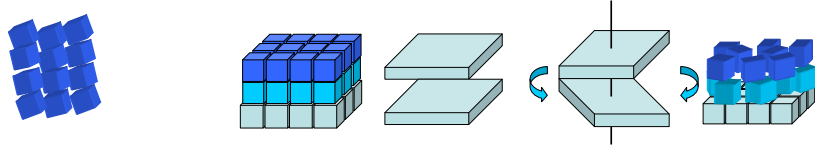
Oriented sample : aluminium foil,
iron plate
plastic bottle

Single crystal : silicon wafer, diamond, quartz



What is oriented sample?

The condition that a lattice plane faces to the same direction



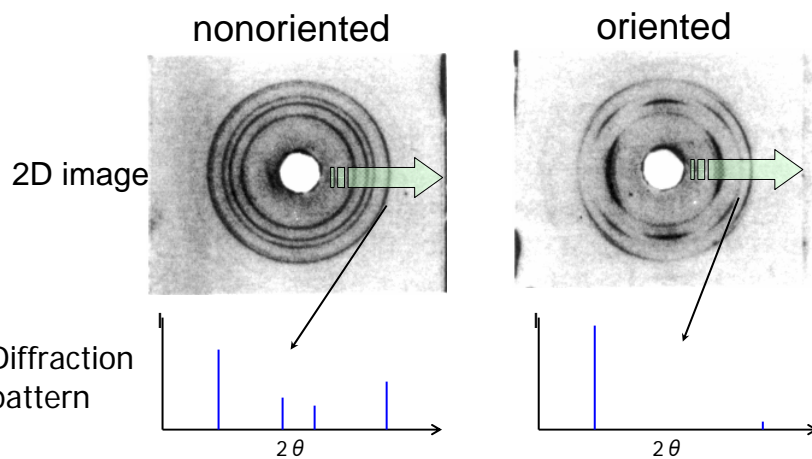
Metal orientation
(rolled sample)

Approximate equivalent
to single crystal
(Epitaxial film)

Uni-axial
orientation
(fiber orientation)

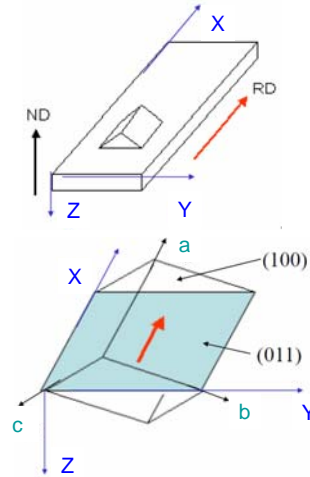
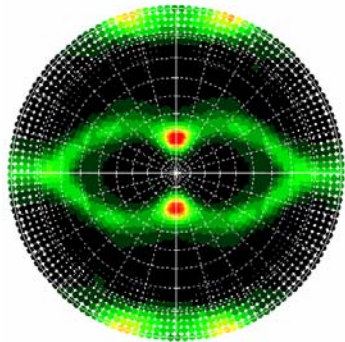


2D image and 2θ-I diffraction pattern



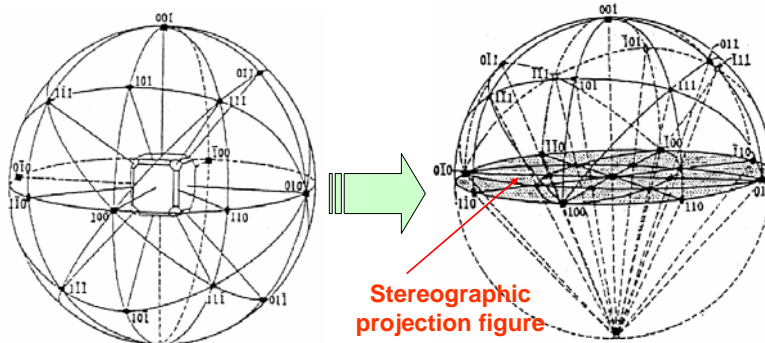
What is the purpose of texture?

Which plane is faced to Rolling direction and Normal direction?



Spherical projection method and Stereographic projection method

3D is described with 2D

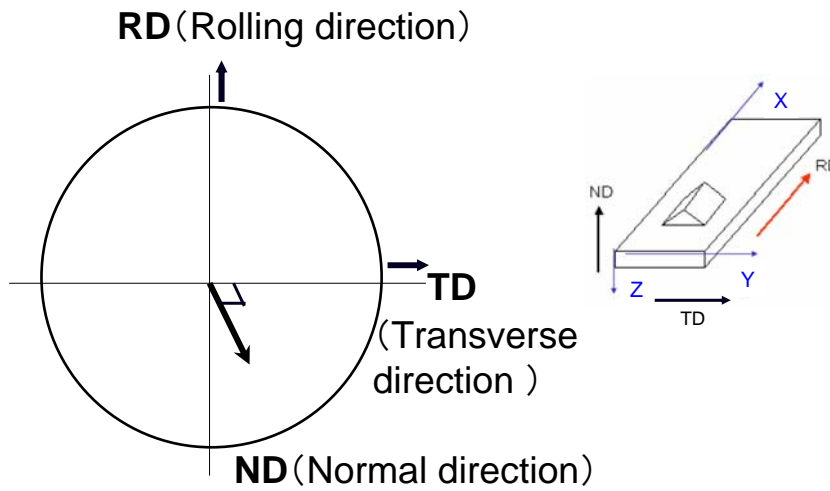


Spherical projection method

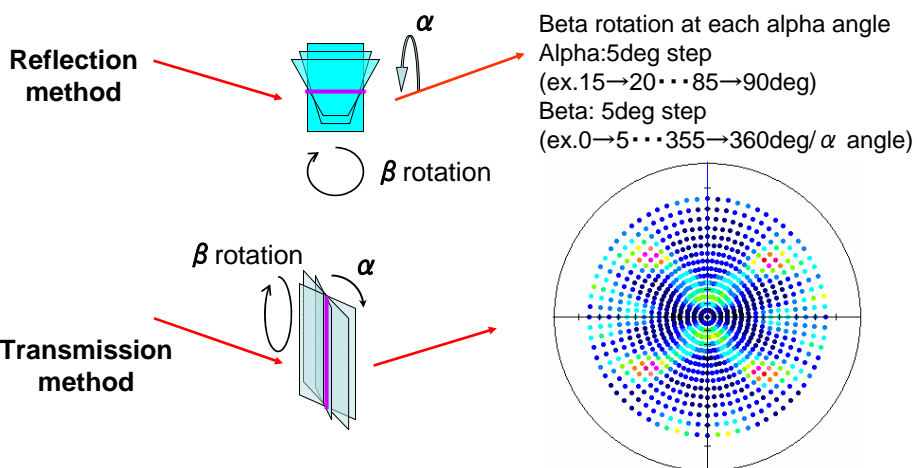
Stereographic projection method



Pole figure



Sample behavior in Reflection method and Transmission method

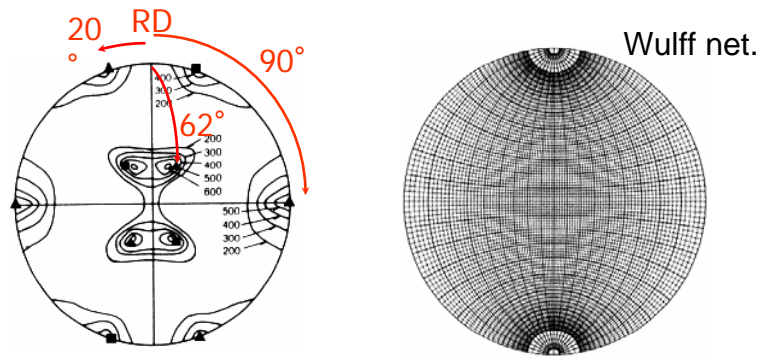


Sample is moved centering around purple line



Orientation analysis :step1

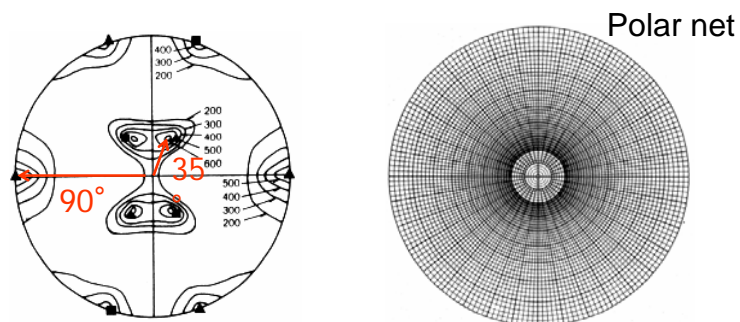
Pole figure of (111) in rolled Cu-Zn(70-30)



The angle between RD and each pole is estimated with Wulff net.



Orientation analysis :step2



The angle between ND and each pole is estimated with Polar net.



Orientation analysis :step3

Angle between plane in $(h_1k_1l_1)$ and $(h_2k_2l_2)$ of cubic crystal

$(h_1k_1l_1)$	ND		$(h_2k_2l_2)$		
	100	110	111	210	211
100	0 90				
110	45 90	0 60 90			
111	54.7	35.3 90	0 70.5 109.5		
210	26.6 63.4 90	18.4 50.8 71.5	39.2 75.0	0 36.9 53.1	
211	35.3 65.9	30 54.7 73.2 90	19.5 61.9 90	24.1 43.1 56.8	0 33.6 48.2



Orientation analysis :step4

Angle between plane of cubic

$(111)(110) = 35.5, 90^\circ$ ND

$(111)(211) = 19.5, 61.9, 90^\circ$ RD

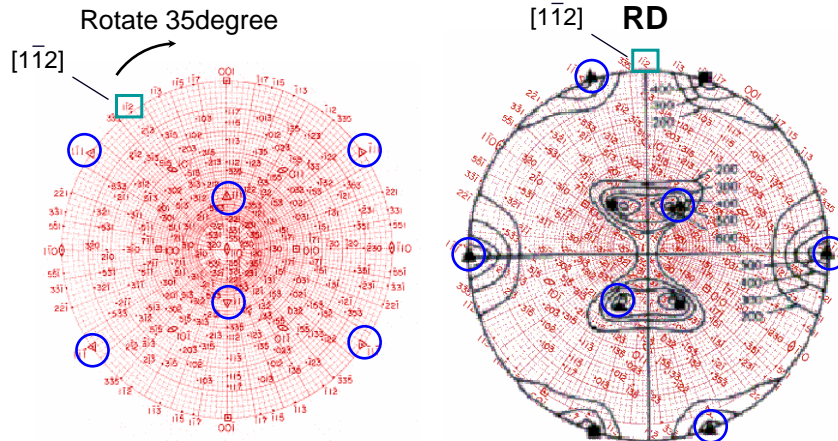
Rotate standard (110) projection of cubic crystal
35degree clockwise.

RD is $[1\bar{1}2]$

This texture is $(110)[1\bar{1}2]$. $(hkl)[uvw] = h*u + k*v + l*w = 0$



Process by stereographic objection figure



Standard (110)objection of cubic crystal



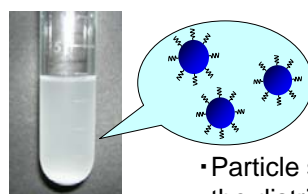
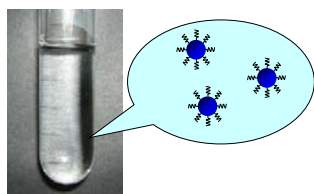
Small angle X-ray scattering
for nano-size sample



Purpose of SAXS

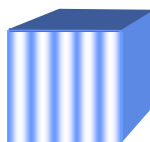
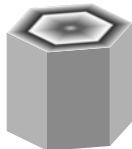
Small Angle X-ray Scattering

- Particle size estimation (X-ray scattering)



- Particle size
- the distribution

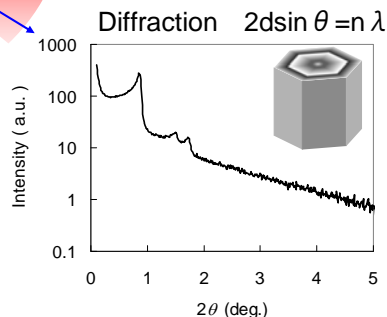
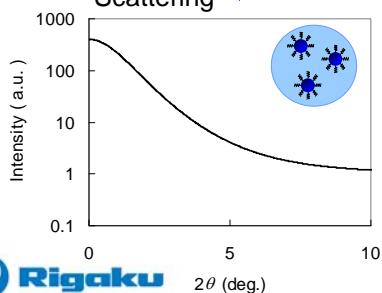
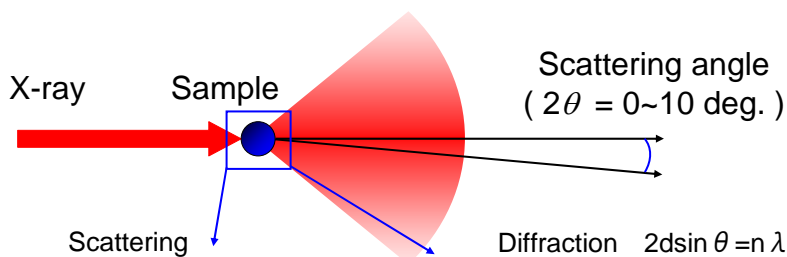
- Phase identification (X-ray diffraction)



- molecular structure

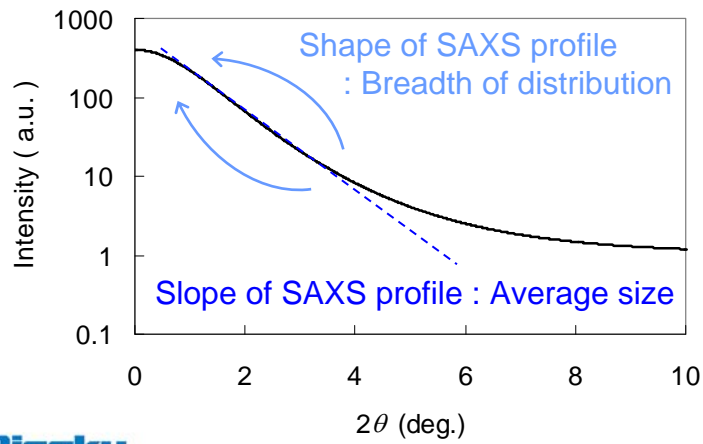


Principle of SAXS



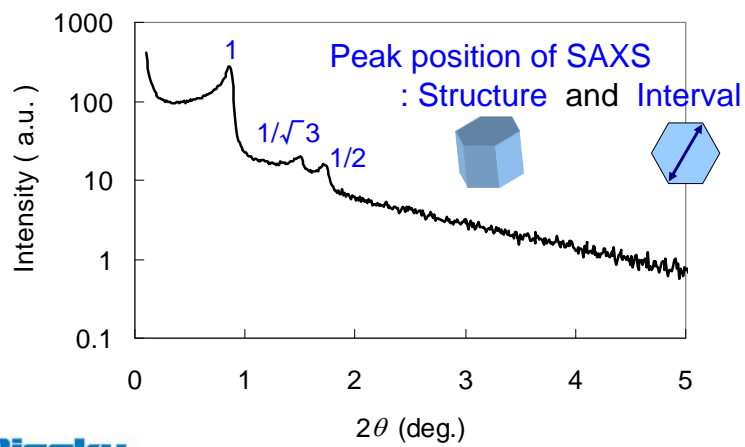
Particle information

- Particle size and particle distribution

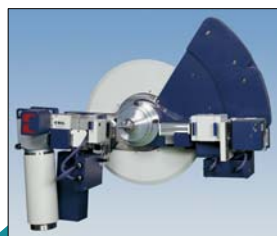


Phase information

- Long-period structure



Instrument for SAXS



Ultima IV



TTRAX III



NANO-Viewer



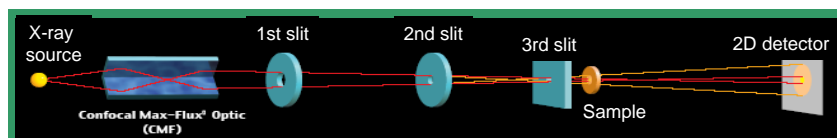
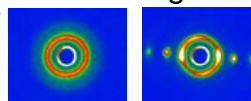
Point focus optics

- NANO-Viewer (2D-SAXS System)

Semiconductor
2D detector Pilatus100k



2D image

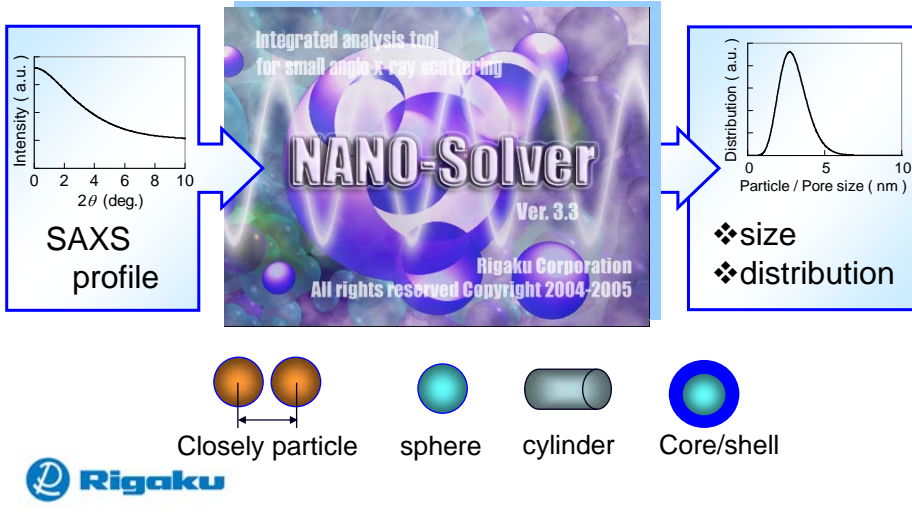


3slits optics



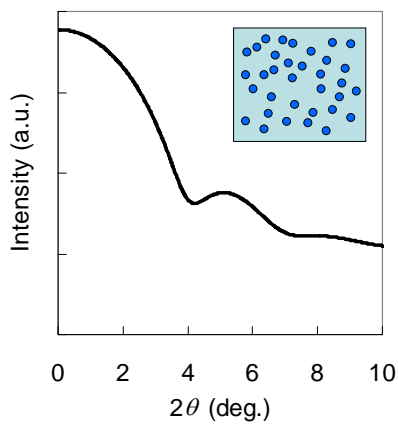
NANO-Solver

- Automatic particle size & distribution estimation !

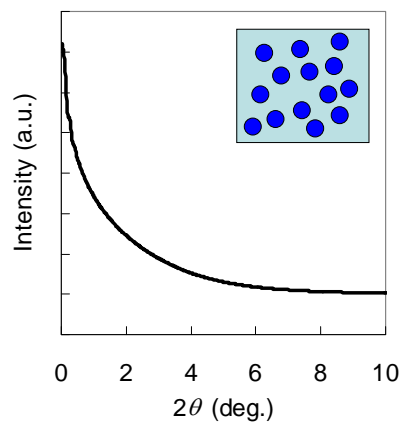


Relations of size and profiles

- Size : 3nm



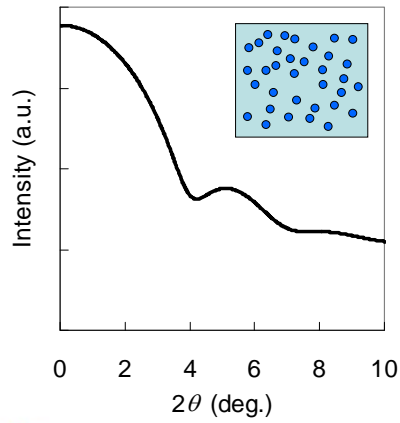
- Size : 60nm



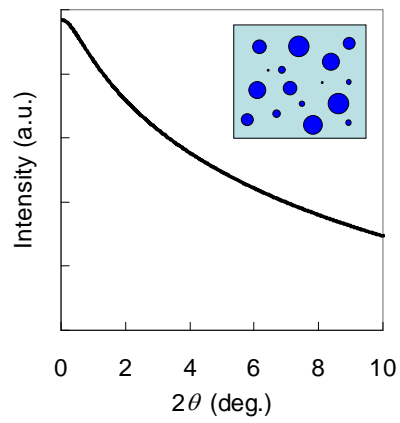
Normalized dispersion : 10 %

Relations of dispersion and profiles

● Dispersion : 10 %



● Dispersion : 90 %



Average diameter : 3 nm

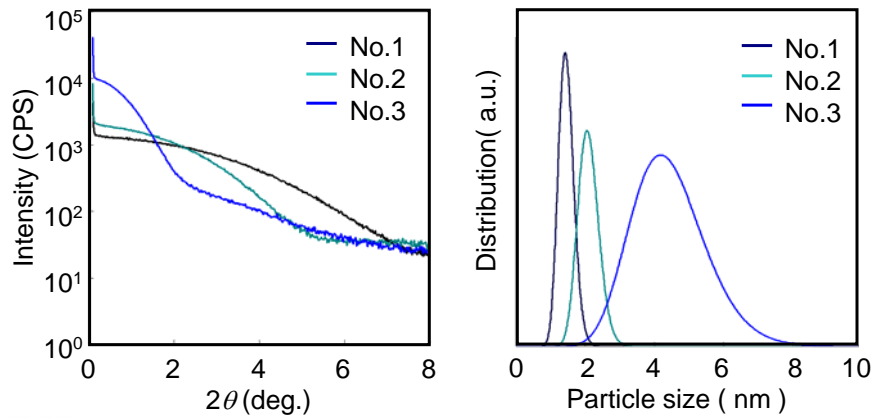
Applications of SAXS

Particle size estimation
(transmission mode)



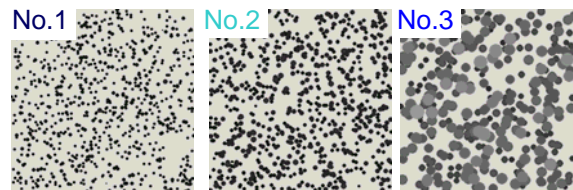
SAXS profiles and size distribution

● Au nanoparticles

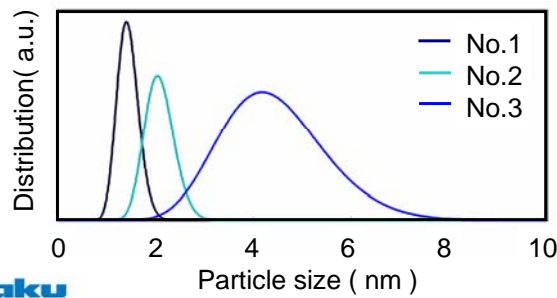


Comparison of TEM image

TEM image



SAXS



Nano size of porous silica

- Mesoporous silica

