Assignment 4

Price a lookback put with the binomial tree model. The payoff function of the lookback put is as follows.

Payoff_{τ} = max($S_{\max,\tau} - S_{\tau}, 0$), where $S_{\max,\tau} = \max S_u$, for $u = 0, \Delta t, 2\Delta t, ..., \tau$.

• Basic requirement (80 points):

(i) Implement the binomial tree model to price both European and American lookback puts.

(ii) Implement the Monte Carlo simulation to price European lookback puts.

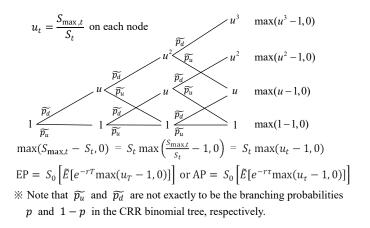
(Inputs: $S_t, r, q, \sigma, t, T, S_{\max,t}, n$, number of simulations, number of repetitions. Outputs: Option values for both methods and 95% confidence level for Monte Carlo simulation.)

• Bonus 1 (5 points):

Based on the same binomial tree framework, devise and implement a quick approach to determine the S_{max} list for each node and implement your approach to price lookback puts.

• Bonus 2 (10 points):

Implement the method in Cheuk and Vorst (1997) to price European and American lookback puts.



• Reference

Cheuk and Vorst (1997), "Currency lookback options and observation frequency: a binomial approach," *Journal of International Money and Finance* 16, pp. 173–187.