



# Eye Tracking Experiment Design

## Lecture 2

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# Outline

- Experiment Design
  - Face recognition
  - Web page usage
- Simulation Study
  - *How many trials are needed?*
- Develop Your Mini-Experiment

# Aim of the study

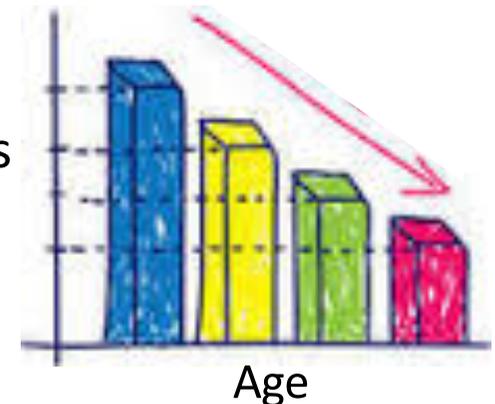
**Aging is associated with decline in..**

## **Cognitive ability**

- Impairment in various aspects such as memory, processing speed, attention, executive functions  
(Kail & Salthouse, 1994; Grady, 2002)

## **Face recognition performance**

- Older adults recognize faces **worse** than young adults  
(Fulton & Bartlett, 1991; Grady, McIntosh, Horwitz, & Rapoport, 2000; Lamont, Stewart-Williams, & Podd, 2005)
- The declined performance is mainly due to **high false alarm rates**, instead of low hit rates, produced by older adults  
(Crook & Larrabee, 1992; Lamont et al., 2005).

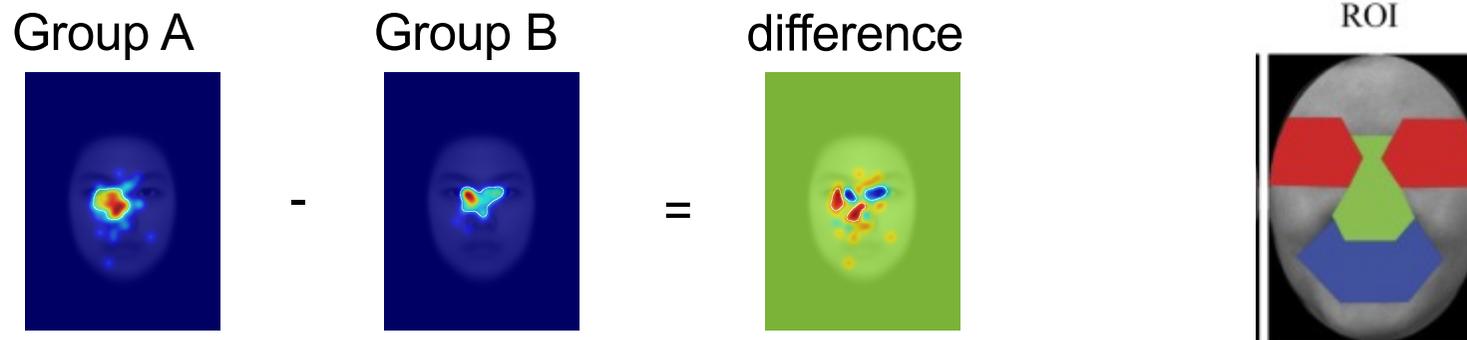


**Aim of study: Could they be reflected in eye movement pattern?**

# Background

Can we use eye movements to understand cognitive processes related to aging?

- However, existing methods **focused on group-level comparison** (e.g. Heat map and ROI approaches)



- It would largely **exclude individual differences**:
  - cognitive or face recognition performance can be different among older people
  - Eye movement can also be different among older people
- Use HMM-based approach, which **consider individual differences**, to examine the link between cognitive ability and eye movement pattern

# Research Questions

Investigate eye movement patterns of older adults in face recognition memory as compared with young adults via the HMM-based approach:

1. Do young and older adults have different eye movement patterns?
2. Is false alarm rate related to the eye movement pattern used?
3. Is cognitive ability of older adults associated with the eye movement pattern used?

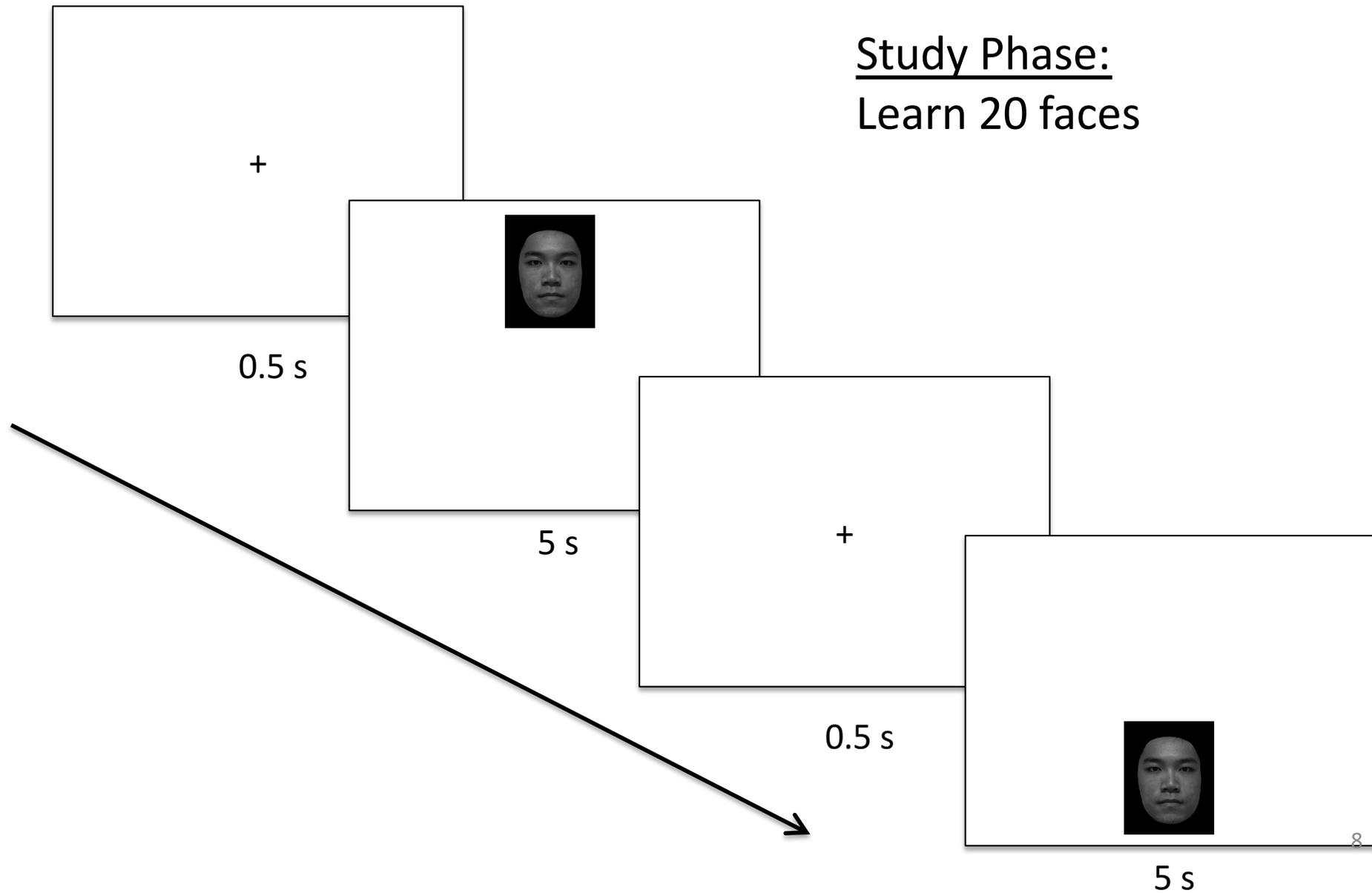
# Methods

- **2 participant groups**
  - 34 Young adults (18-24, M = 20, SD = 2)
  - 34 Older adults (65-81, M = 69, SD = 8)
  - All are Chinese, right-handedness, with normal or corrected vision
  - All older adults are within normal range of cognitive ability
    - as assessed by the Montreal Cognitive Assessment (MoCA) Hong Kong version (Wong et al., 2009)
- **Materials:**
  - Young Chinese frontal view face images, gray-scale
- **Apparatus:**
  - Eyelink 1000 eye-tracking system

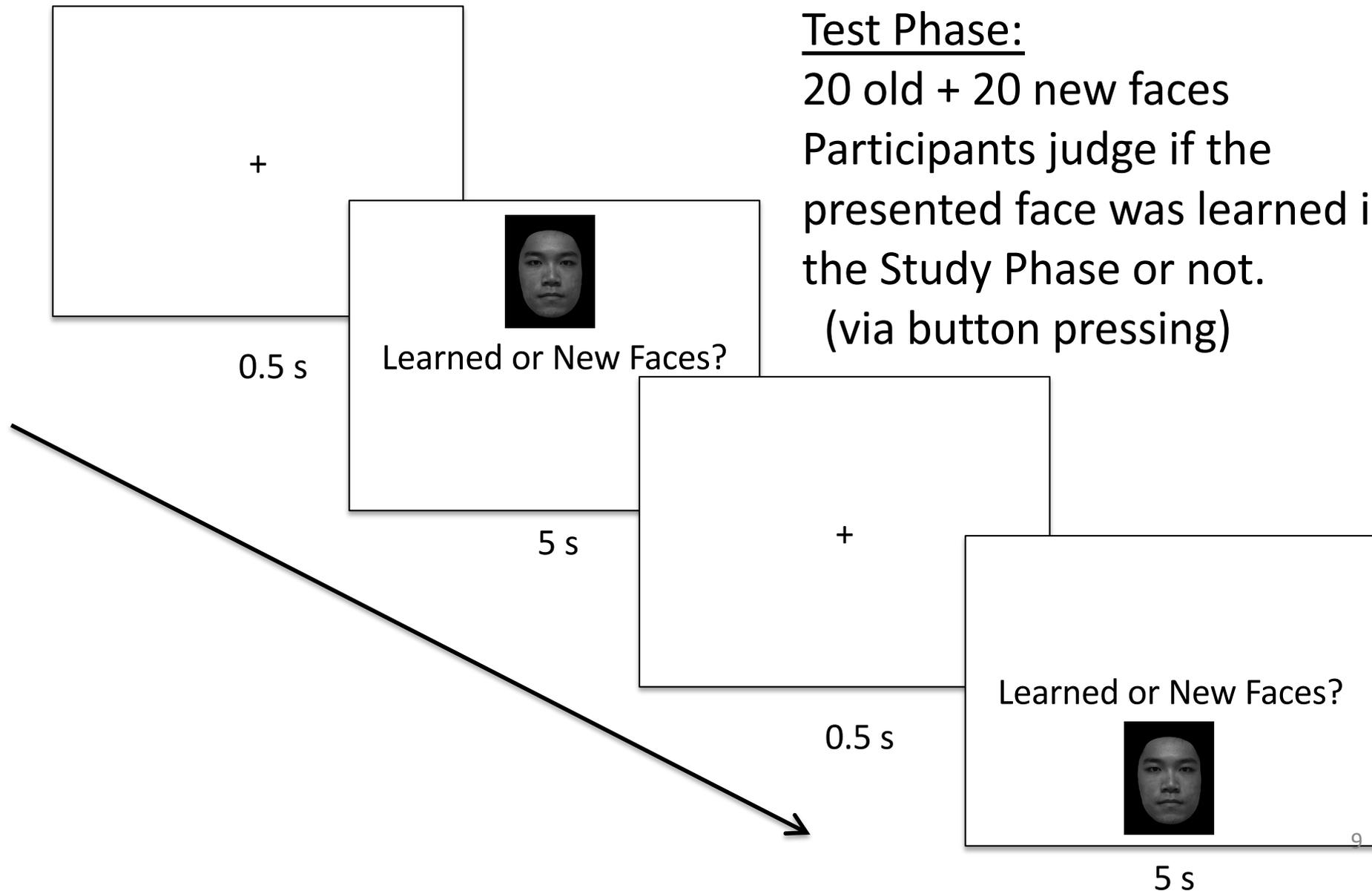




# Methods: Face Recognition task



# Methods: Face Recognition task



# Notes on Experiment Design

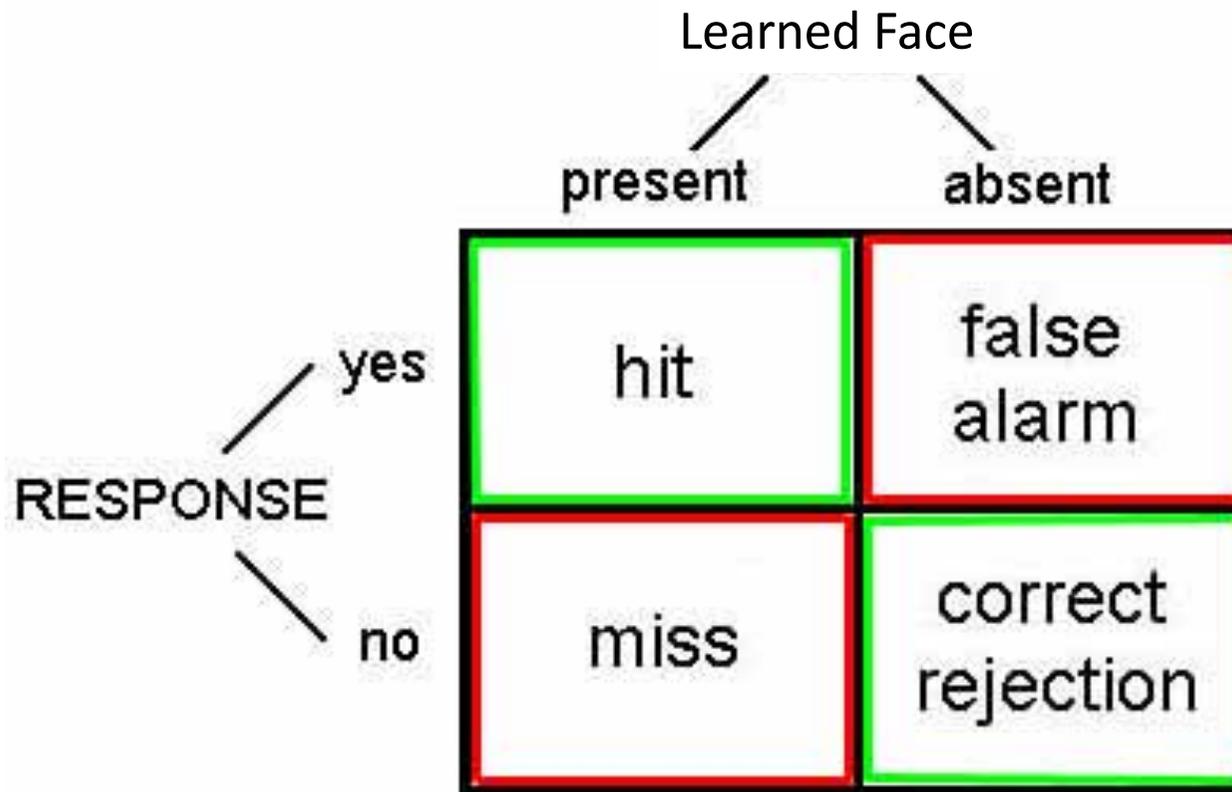
- Need to calibrate eye tracker for each subject
  - Fixation cross used for drift correction before each trial
- All stimuli are aligned by eyes-mouth triangle
  - Recorded eye gaze coordinates have the same semantic meaning over all stimuli.
- Counter-balancing experiment
  - Counter-balance or randomize the presentation of the faces on top and bottom halves. (or in the 4 quadrants)
  - Randomize order of faces.

# Data Analysis

- Pre-processing
  - convert *raw* eye gaze to eye fixations
    - use eye tracker's software
  - convert *raw* fixation locations into locations on stimuli
    - subtract the coordinates of the top-left corner of the stimuli
- Analysis
  - Learn an HMM for each individual
  - Cluster individuals' HMMs into groups
  - Analyze differences in groups (pre-defined or data-driven)
    - Group membership ( $\chi^2$  test)
    - Performance differences between groups (t-test)
    - Correlation between group similarity and behavioral data (linear regression)

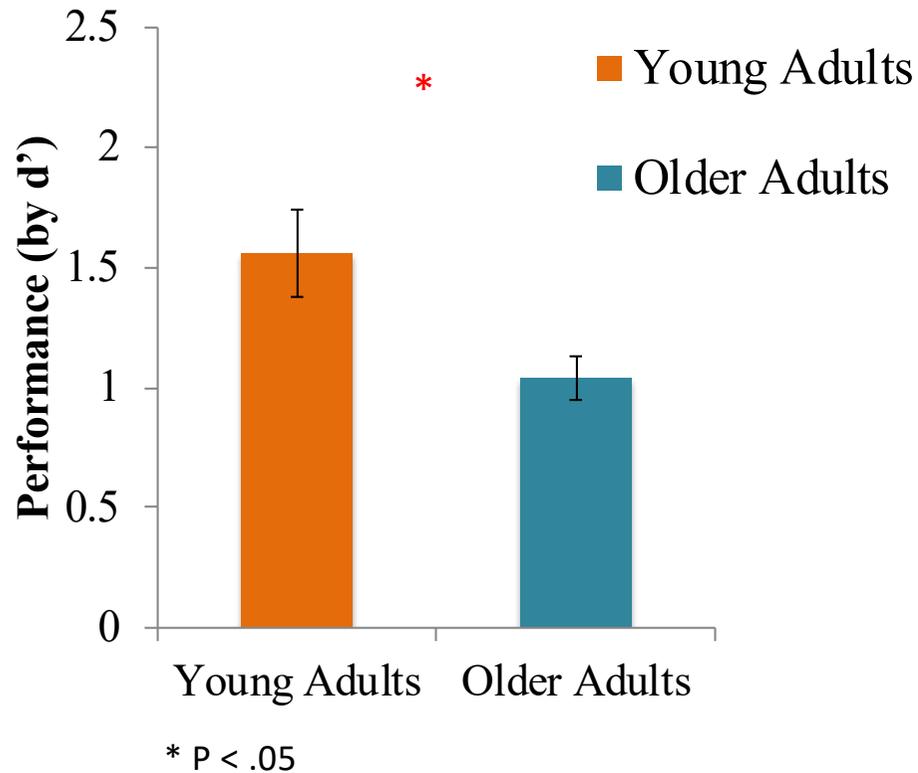
# Face Recognition Performance

- Signal detection theory
- Measured by Discrimination sensitivity measure  $d'$   
 $d' = Z(\text{hit}) - Z(\text{false alarm})$

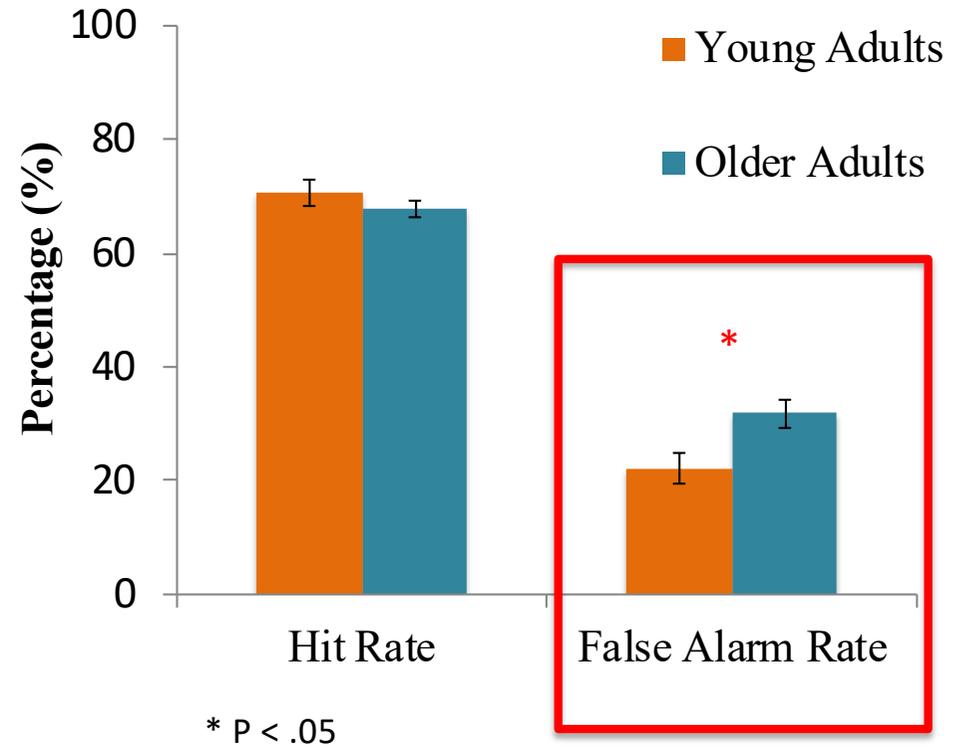


# Face Recognition Performance

Group Analysis of Young/Older Adults

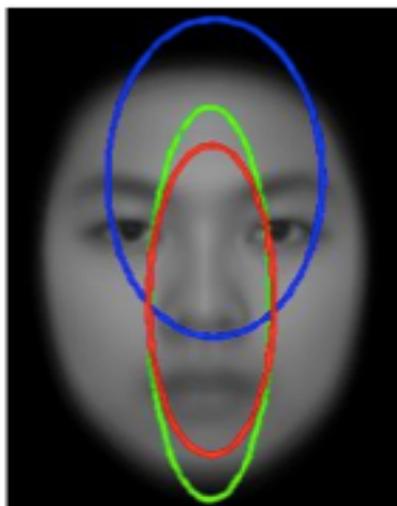


Young adults recognized faces better!



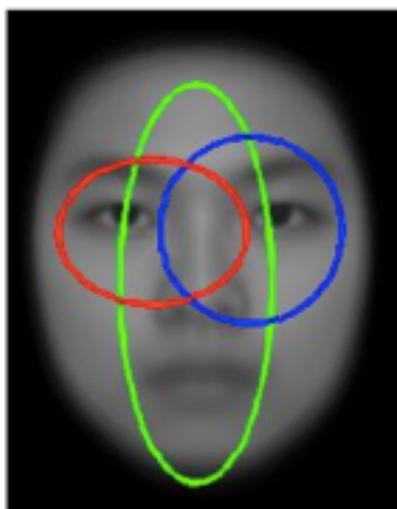
Older adults had significantly higher false alarm rates!

# Clustered HMM – by clustering all participant HMMs into subgroups



**Representative HMM of Holistic Pattern**

<b>Prior values</b>	<b>Red</b>	<b>Green</b>	<b>Blue</b>
	.16	.80	.04
<b>Transition probabilities</b>	<b>To Red</b>	<b>To Green</b>	<b>To Blue</b>
From <b>Red</b>	.82	.12	.06
From <b>Green</b>	.93	.02	.05
From <b>Blue</b>	.07	.00	.93

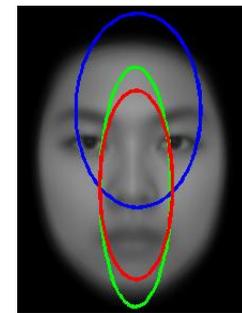
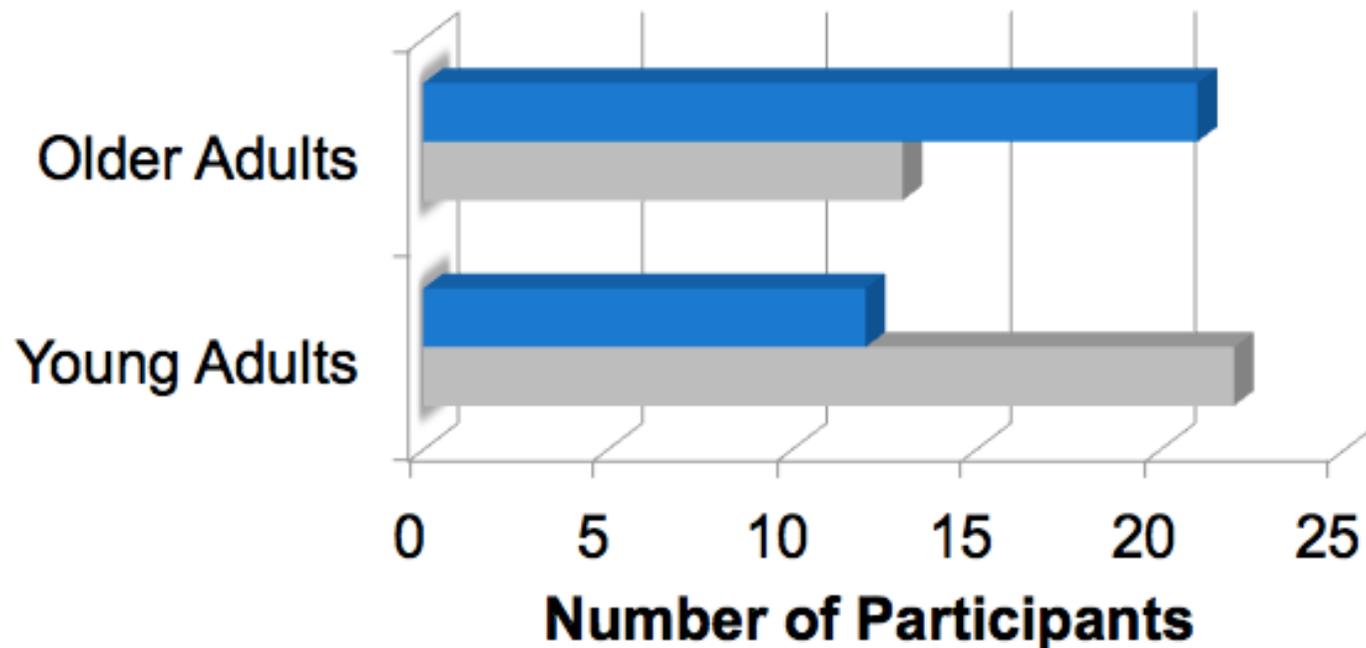


**Representative HMM of Analytic Pattern**

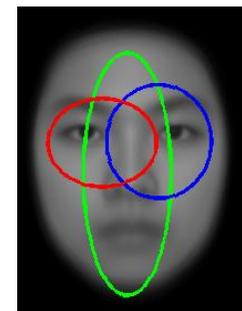
<b>Prior values</b>	<b>Red</b>	<b>Green</b>	<b>Blue</b>
	.03	.82	.15
<b>Transition probabilities</b>	<b>To Red</b>	<b>To Green</b>	<b>To Blue</b>
From <b>Red</b>	.21	.34	.45
From <b>Green</b>	.25	.36	.39
From <b>Blue</b>	.27	.26	.47

## Result: Different Eye movement patterns

- Look at group membership (2x2 contingency table)
- **More older adults adopted holistic patterns** while more young adults adopted analytic patterns,  $\chi^2(2) = 4.77, p = .03$  (Chi-square test)

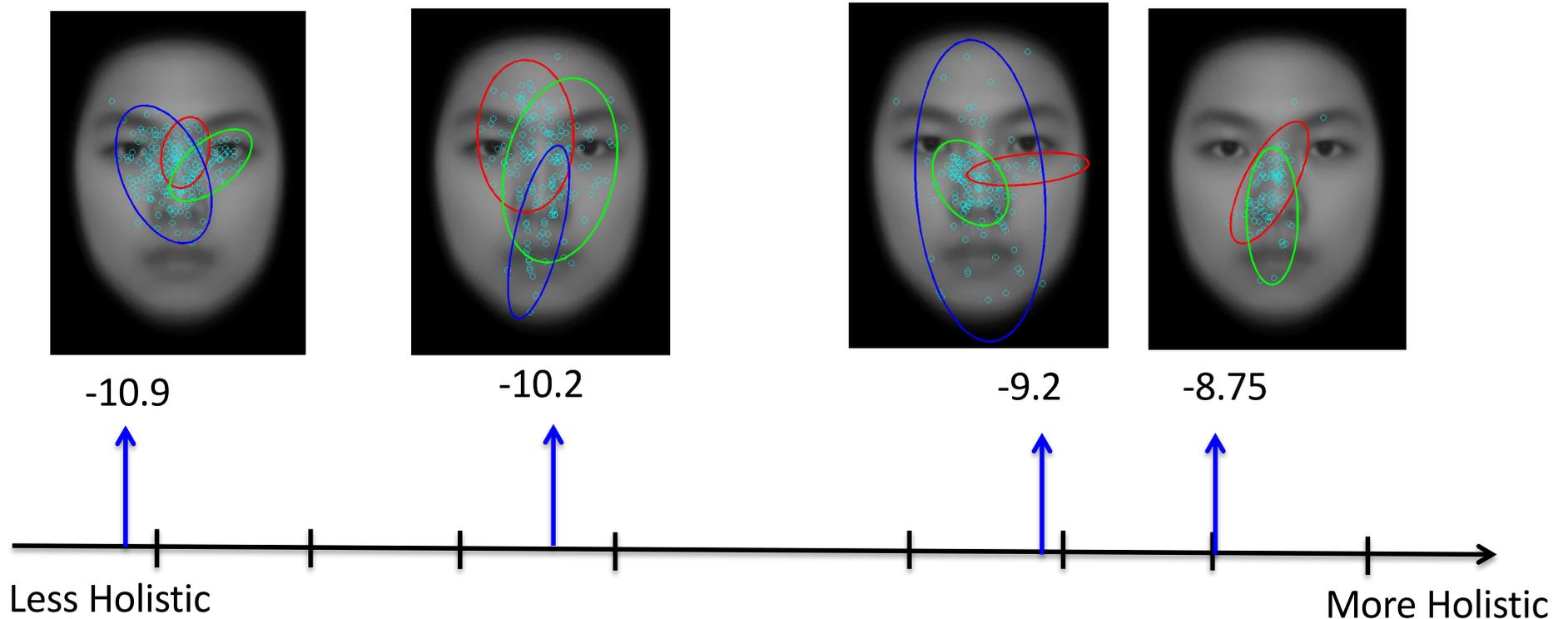


■ Holistic  
■ Analytic



# Results

- Compute the likelihood of each participant's eye fixations to the holistic or analytic group HMM.
- **Holistic likelihood:** degree of being classified to holistic pattern
- **Analytic likelihood:** degree of being classified to analytic pattern
- For example:



# Results: Relationship between eye movement pattern and performance

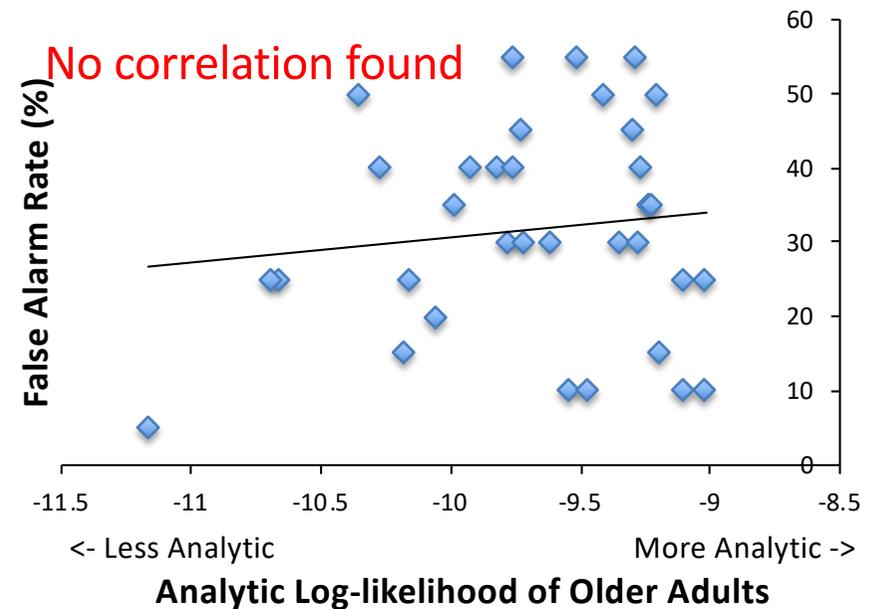
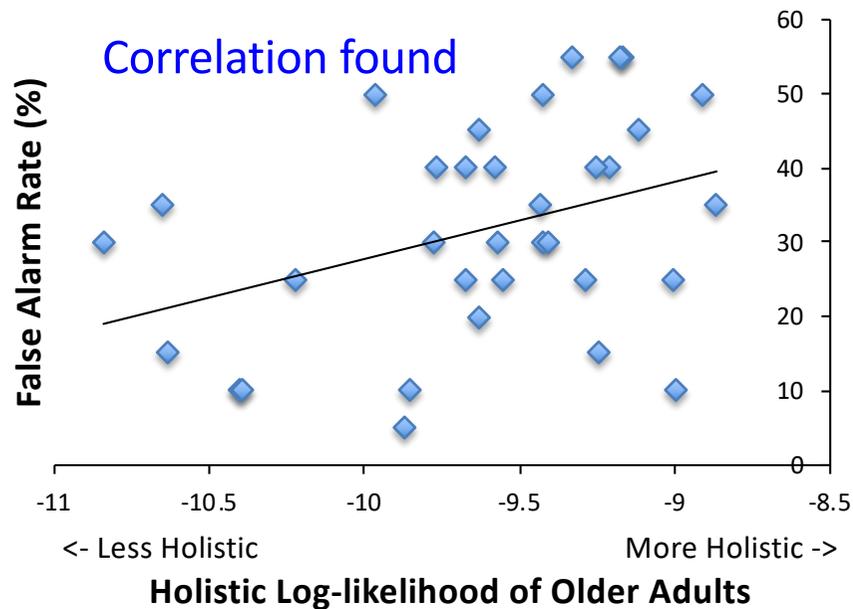
- Group analysis

- Analytic group scored higher ( $d'$ ) than the holistic group:

- lower false alarm rate
- No difference in the hit rate.

- Linear regression analysis

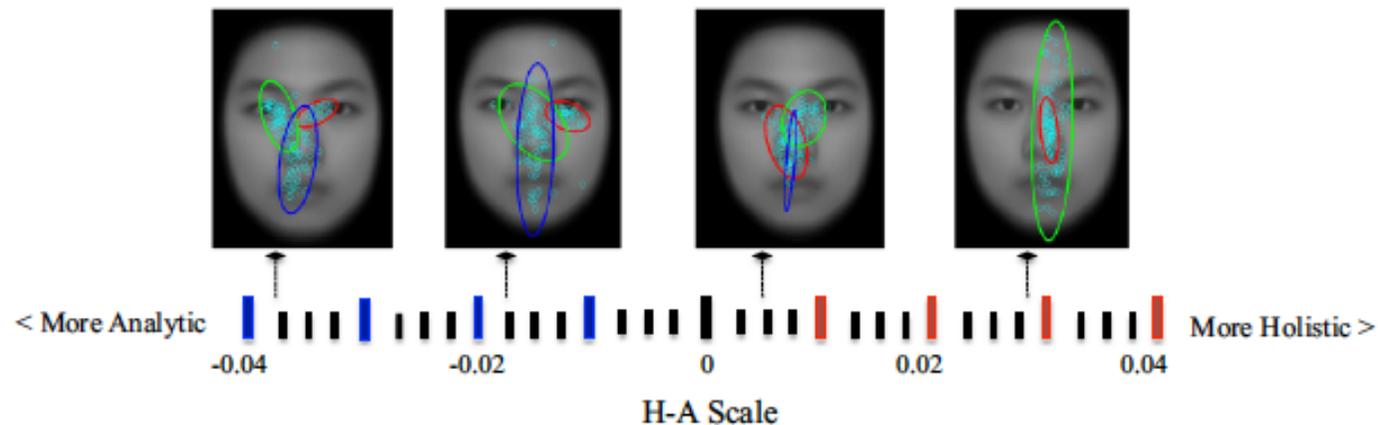
- Among older adults, the higher the log-likelihood of a holistic pattern, the higher the false alarm rate. This was not found in the analytic patterns.



# Relationship between eye movement patterns and cognitive ability in older adults

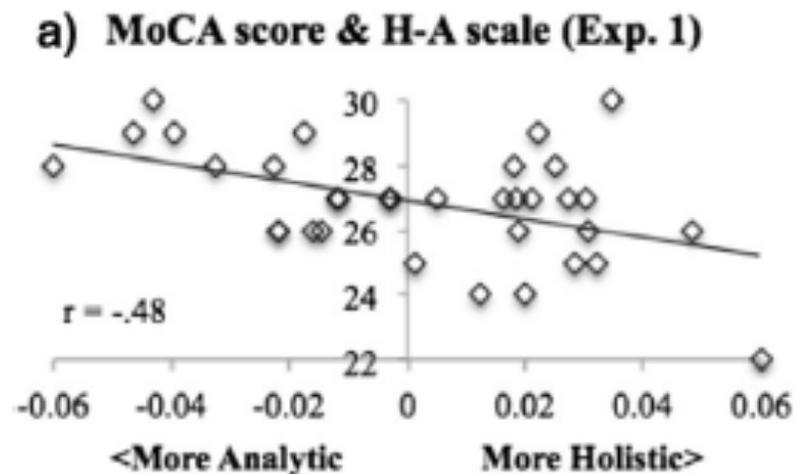
- Summarize similarity to the two groups using Holistic-Analytic (HA) scale:

$$H-A \text{ Scale} = \frac{\text{Holistic log-likelihood} - \text{Analytic log-likelihood}}{|\text{Holistic log-likelihood}| + |\text{Analytic log-likelihood}|}$$



- Linear regression analysis
  - In older adults, the lower the cognitive ability (by MoCA), the higher the H-A scale:

$$R = -.48, P = 0.004$$



# Eye movement & cognitive ability: Correlations

- **H-A scale was particularly correlated with executive and visual attention functions.**

		Correlation with H-A Scale	
		$r$	$p$
1.	General Cognitive assessment (MoCA)	-.44	.010*
2.	Executive Planning (TOL; Total moves)	.36	.043*
3.	Visual Attention (TMT)	.37	.034*
4.	Working Memory	-.35	.062
	- Verbal 2-back		
	- Spatial 2-back	-.35	.066
5.	Verbal Memory (CAVLT)	-.17	.337
6.	Verbal Fluency (CVFT)	-.15	.394

- Could also use a hierarchical regression analysis to determine the most important predictors

# Experiment Design for Web Pages

- Subjects were given a self-evaluation survey on their familiarity with technology.
  - Used to form groups of *experienced / inexperienced*
- Subjects were asked to perform a task on LinkedIn
  - “Ask your contact “Christian Maier” for a letter of recommendation.”
- Some given incentive to perform quickly.
  - Used to form groups of *pressure / no-pressure* to perform
- Recorded eye movements while performing the task.
  - discover the ROIs from data using GMMs / HMMs.

# Data Analysis and Webpage ROIs

- Learn one HMM for each group.
  - share ROIs among groups.
- Look at differences in eye gaze strategy among groups.

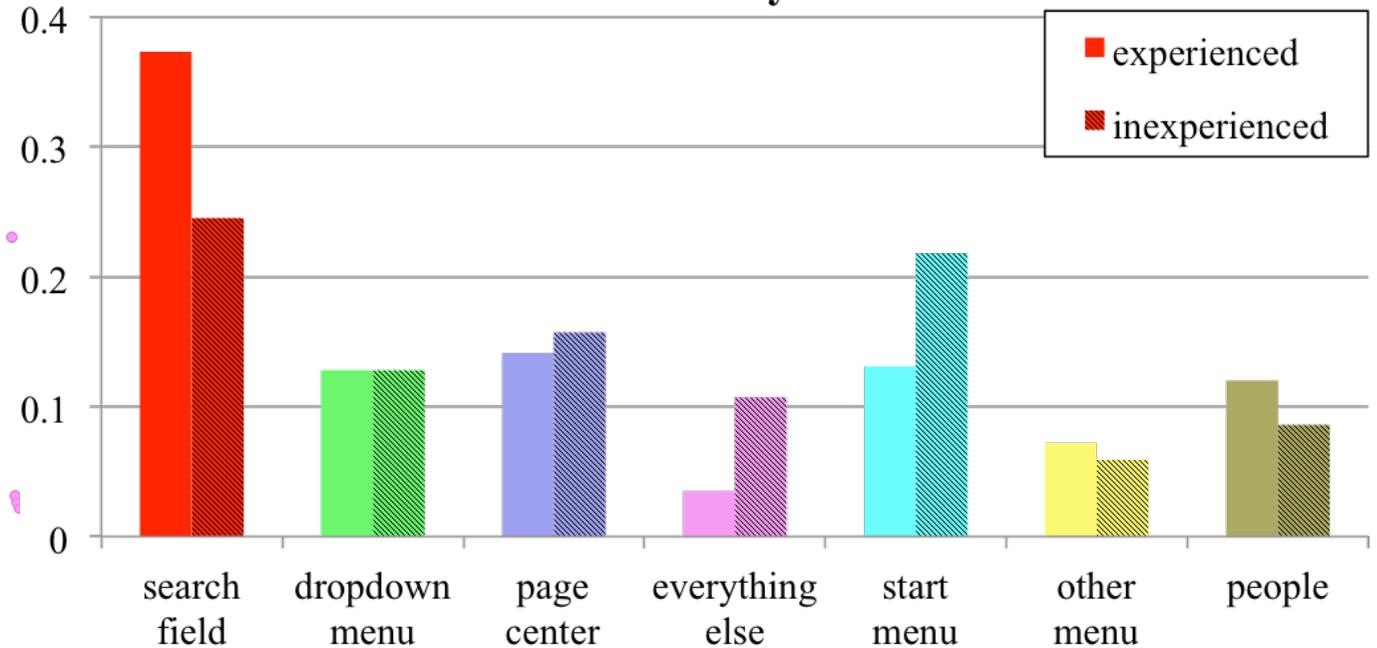


A. Eckhardt, C. Maier, JJ P.-A. Hsieh, T. Chuk, A.B. Chan, J.H. Hsiao, and R. Buettner (2013). “Objective Measures of IS Usage Behavior Under Conditions of Experience and Pressure Using Eye Fixation Data.” In: *International Conference on Information Systems*.

# Behavioral IS usage patterns of experienced and inexperienced users



ROI Fixation Probability

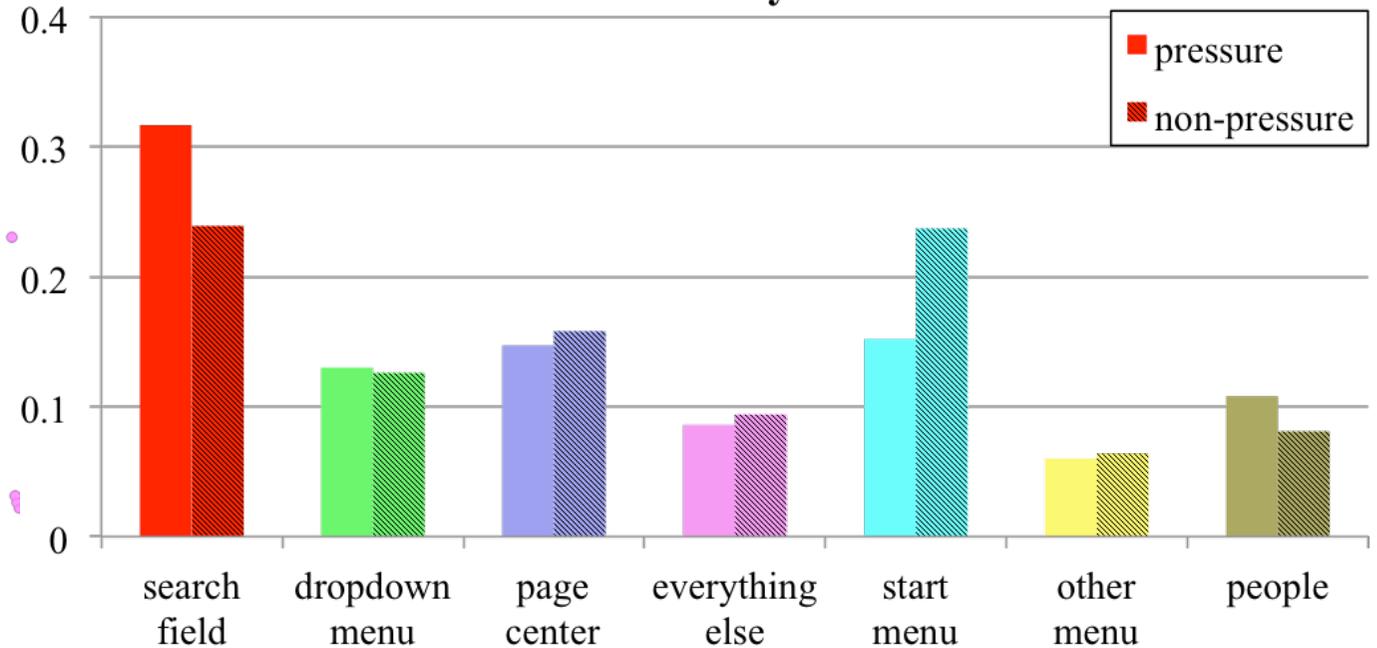


- Experienced users focus on search area.
- Inexperienced users use the start menu.
  - also get distracted by “everything else”

# Behavioral IS usage patterns with(out) pressure to perform



## ROI Fixation Probability



- Pressured users focus on search area.
- Non-pressured users use the start menu.

# Different Stimuli Layouts

- So far the stimuli have the same feature layouts
  - e.g., all faces are aligned by eyes and mouth
- **How to summarize a general eye movement strategy in tasks where stimuli's feature layouts differ significantly (e.g., scene perception, visual search, reading etc.)?**
  - **EMHMM with co-clustering**: 1 stimulus 1 model; use co-clustering to discover participants using the same pattern across stimuli.



*More details  
in next lecture*

# Outline

- Experiment Design
  - Face recognition
  - Web page usage
- Simulation Study
  - *How many trials are needed?*
- Develop Your Mini-Experiment
  - *PsychToolbox and Eyalink*



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# Simulation Study

*How many trials do we need?*

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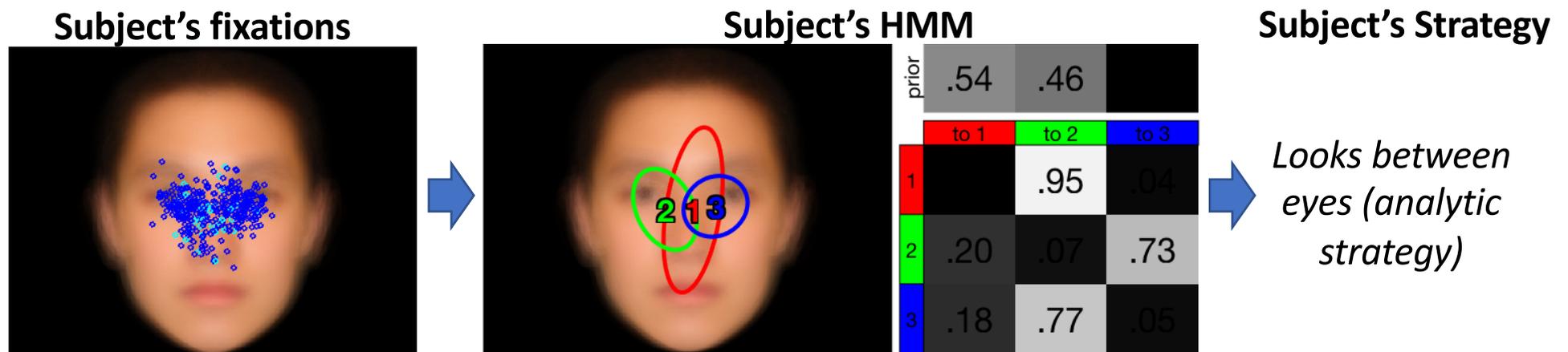
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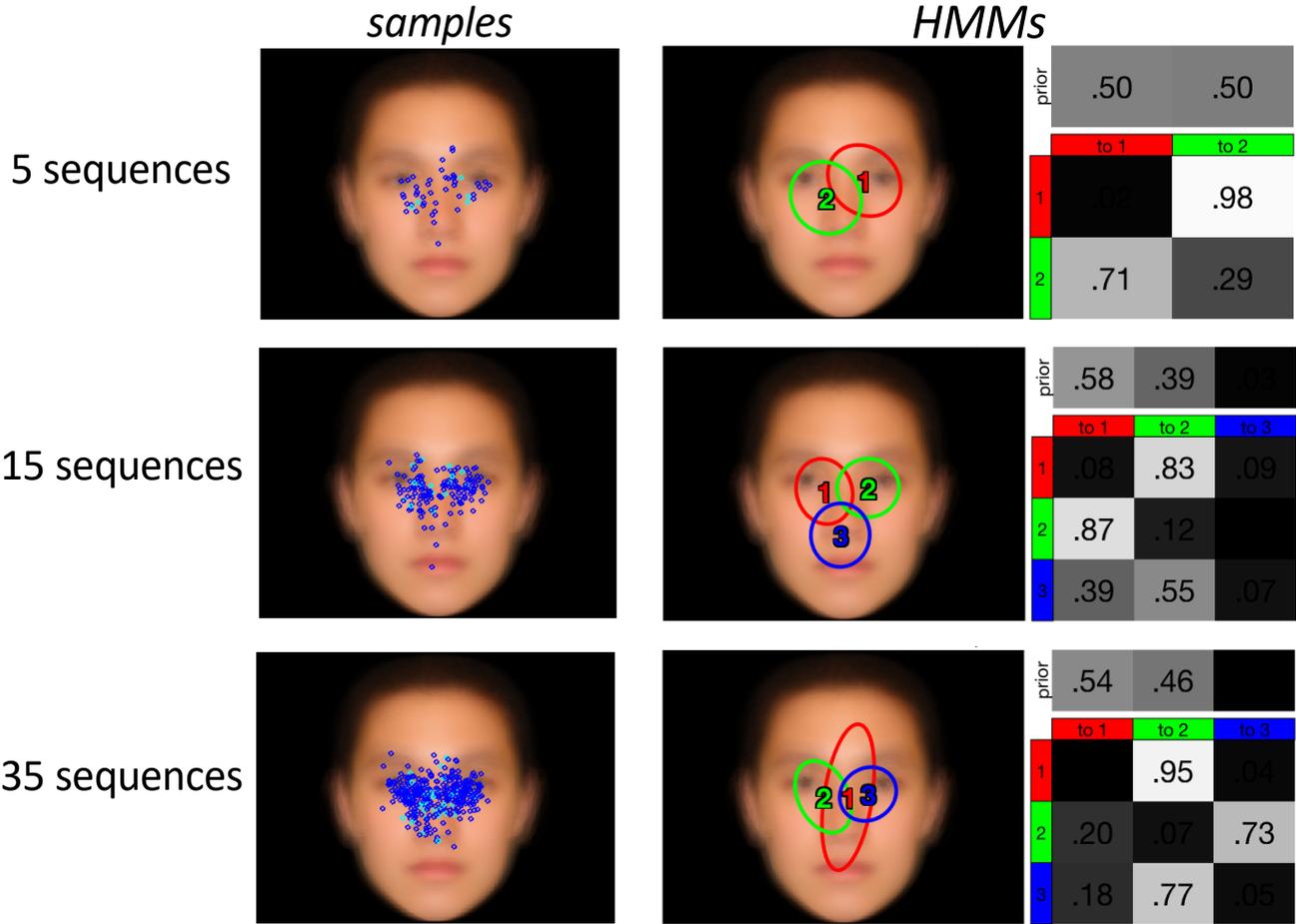
# Eye Tracking Experiment

- For each subject:
  - Collect eye fixations on set of stimuli (e.g., faces) while performing a task (e.g., recognition).
    - Typically 30-50 trials → 30-50 fixation sequences.
    - Depending on the task, 2-10 fixations per trial.
  - Estimate an individual HMM for the subject.
  - Interpret the estimated HMM as the subject's eye gaze strategy for this task.



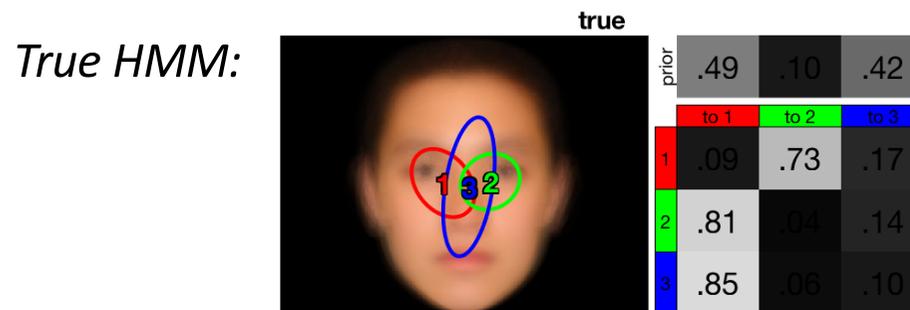
# How much data?

- **Question:** How much data do we need to ensure that the estimated HMM can well represent the subject's overall eye gaze strategy?



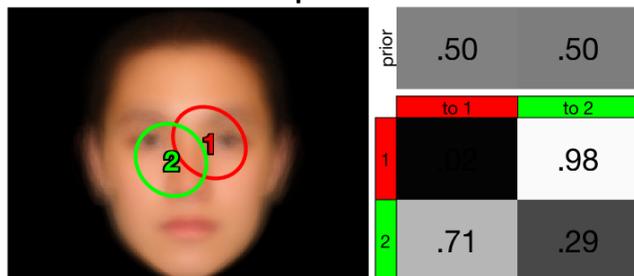
# How much data?

- Accuracy of the estimated HMM parameters, relative to the *true* underlying strategy (*true HMM*), depends on the amount of data used.
  - Analogously, the accuracy of a sample mean relative to the true mean depends on the sample size.

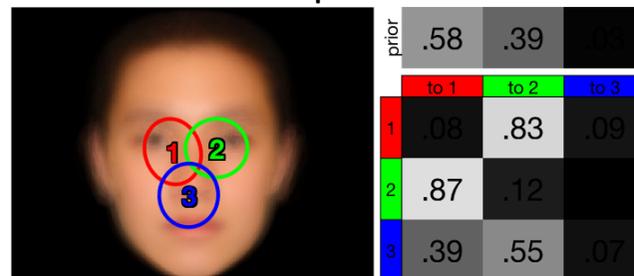


*HMMs estimated with...*

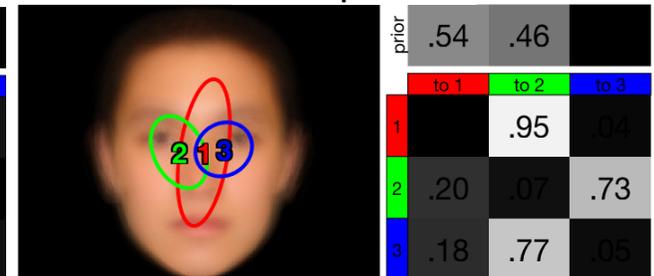
5 sequences



15 sequences



35 sequences



# How much data?

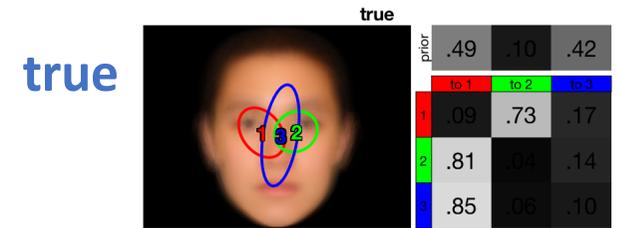
- **Question:** How much data do we need to ensure that the estimated HMM can well represent the subject's overall eye gaze strategy?
  - *i.e., Given samples from a true HMM, how much data is needed to estimate the HMM within some error tolerance?*
- Can claim that the estimated HMM represents the subject's **overall** eye gaze pattern on that type of stimuli.
- **Note:**
  - Using less data, then the estimated HMM only represents the eye gaze pattern over the **particular** stimuli.

# Simulation Study

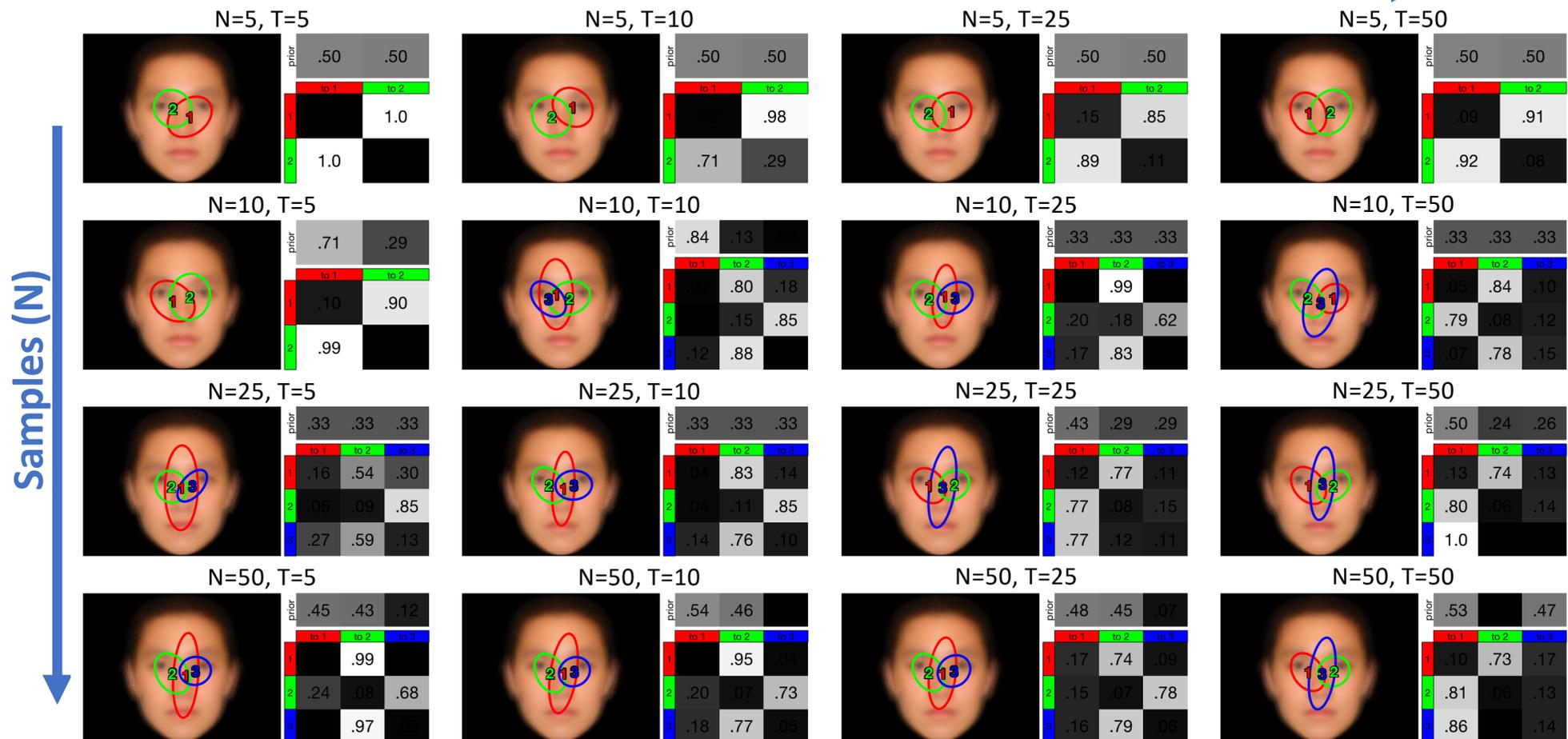
- **To quantify the error when estimating HMMs from limited samples**
- 10 ground-truth HMMs from 10 subjects.
  - Image size is 512x384 and face region is 300x350.
- Estimation quality depends on the number of samples
  - Consider different combinations of number of sequence samples  $N$  and sequence lengths  $T$ .
- For each combination  $(N, T)$  we run 500 trials:
  - Select a random ground-truth HMM.
  - Sample  $N$  sequences of length  $T$  from the true HMM.
  - Estimate an HMM from the samples using VBHMM with automatic hyperparameter selection.
  - Compute *error measure* between the estimated and true HMMs.
- Average error over trials.

# Example

- Estimated HMMs for different T, N



Sequence length (T)



more fixations → better quality

# Estimation Error for whole HMMs

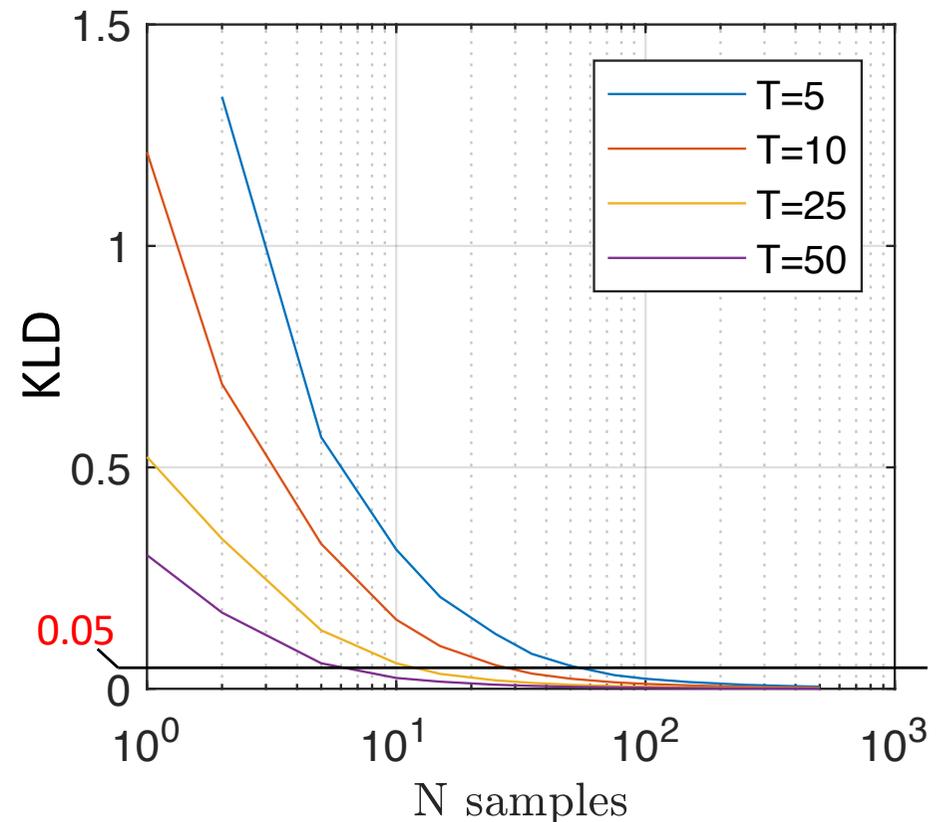
- Kullback-Leibler divergence (KLD) rate between probability distributions of the true and estimated HMM distributions.

$$\phi(p(y), \hat{p}(y)) = \int_y p(y) \log \frac{p(y)}{\hat{p}(y)} dy$$

- Zero when the two HMMs are the same.
  - Positive values indicate more dissimilarity.
- Intuitively, KLD is the amount of “information” that needs to be added to turn the estimated distribution into the true distribution.

# Estimation Error for whole HMMs

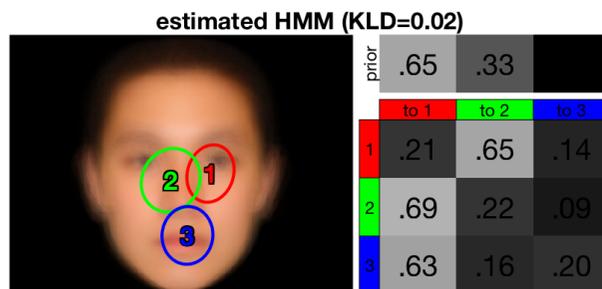
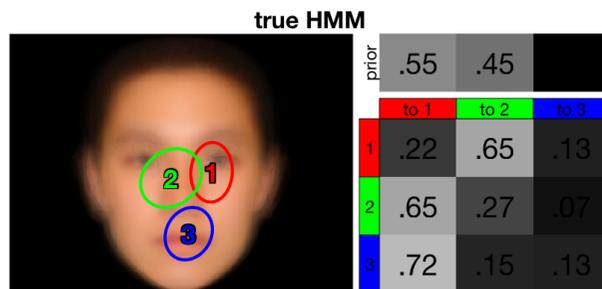
- KLD decreases to zero as number of samples increases or length of sequences increases.
- To obtain low KLD of 0.05 requires  $\sim 250$  fixations:
  - $N=52, T=5$
  - $N=26, T=10$
  - $N=11, T=25$
  - $N=6, T=50$



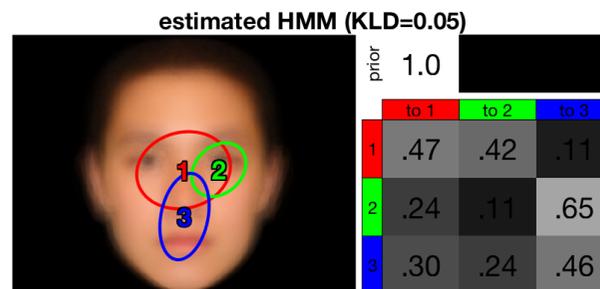
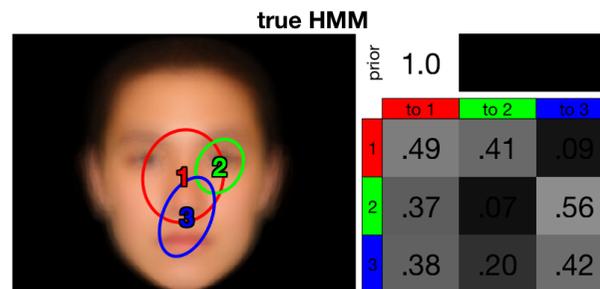
# HMM Examples

- True and estimated HMMs

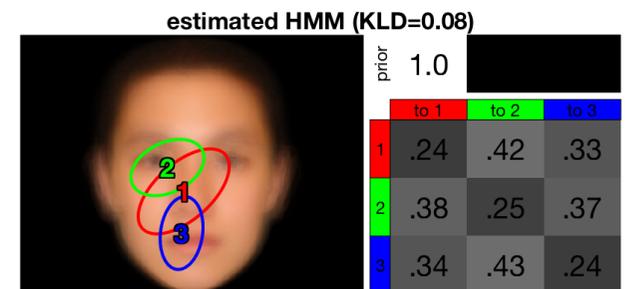
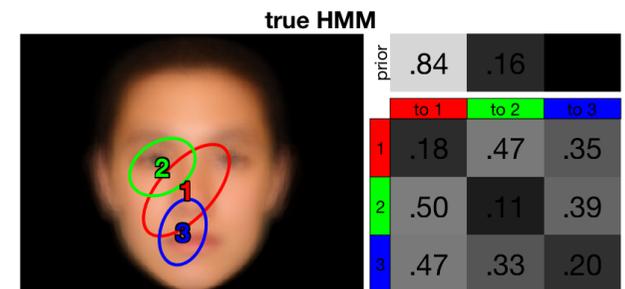
KLD=0.02



KLD=0.05

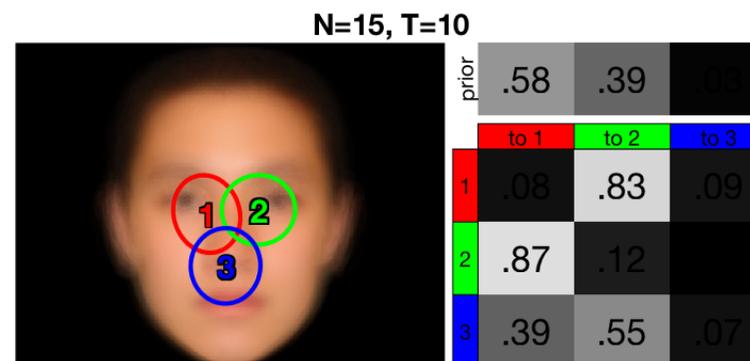
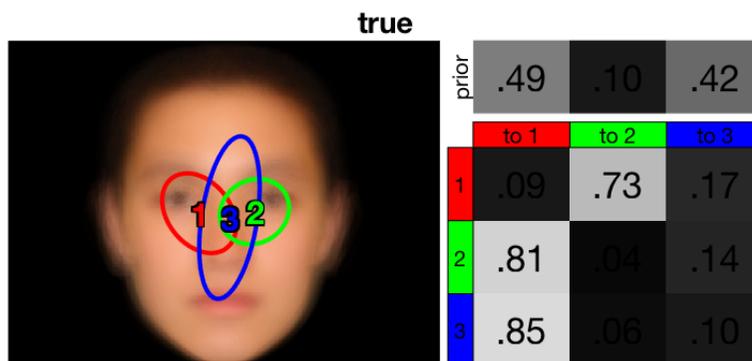


KLD=0.08



# Estimation Error of Components

- KLD measures the **overall** error between GT and estimated HMMs.
- We can also measure error of the estimated model components
  - ROIs
  - transition matrix
  - initial probabilities

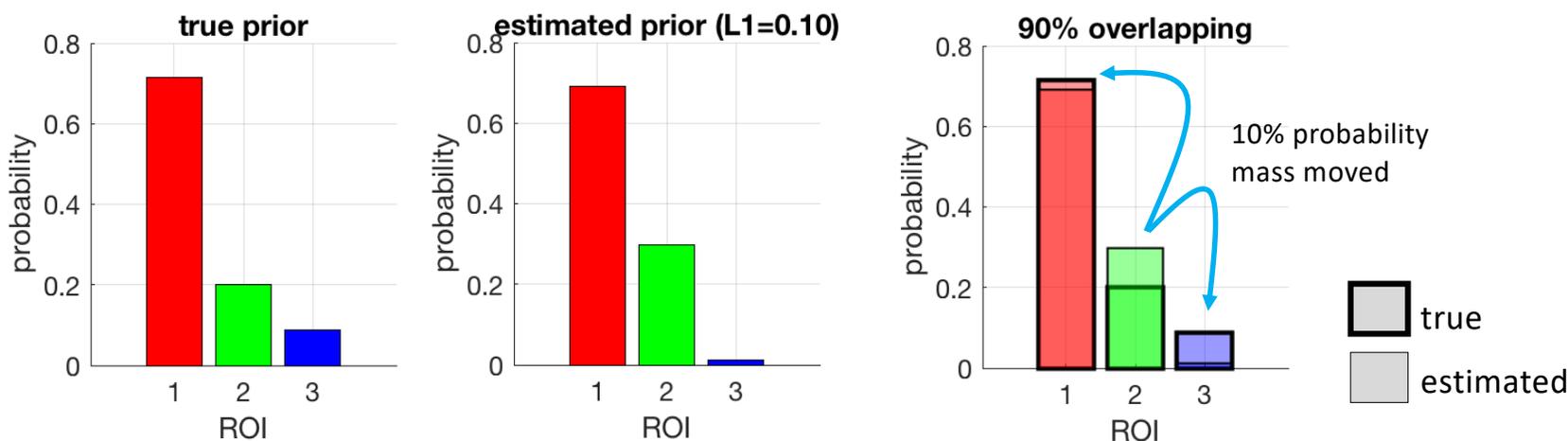


# L1-norm error

- L1-norm measures the absolute difference between two probability distributions.

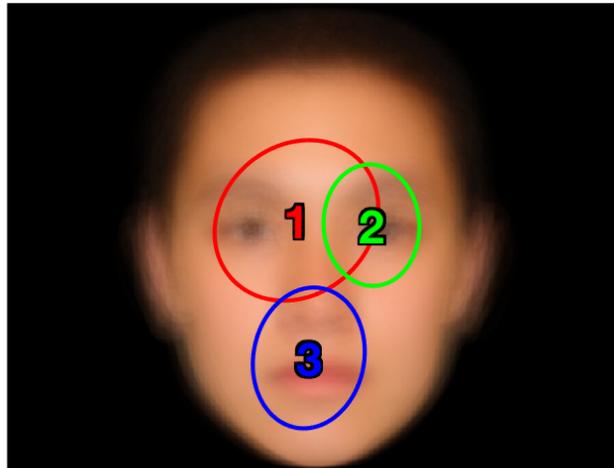
$$\psi(p(y), \hat{p}(y)) = \frac{1}{2} \int_y |p(y) - \hat{p}(y)| dy.$$

- Intuitively, it is the amount of probability that needs to be moved to turn one distribution into the other.
- Amount of non-overlapping between distributions.

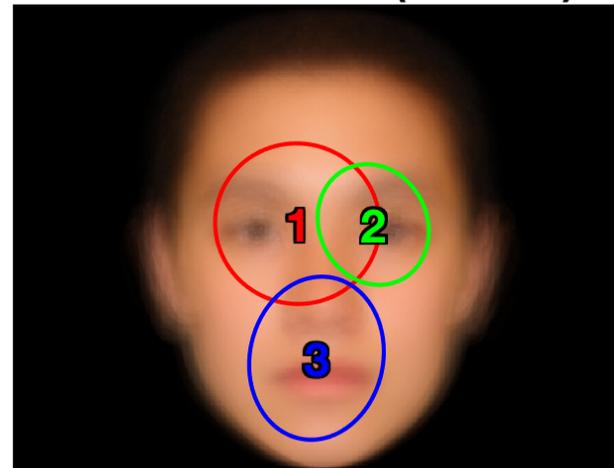


# ROI Example

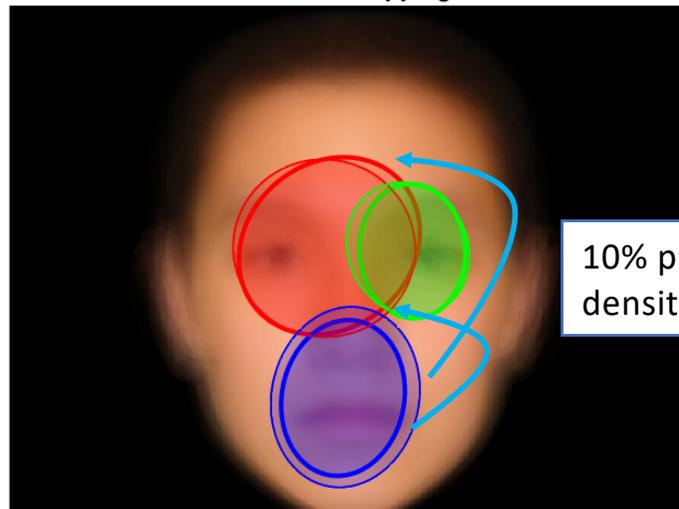
true ROIs



estimated ROIs (L1=0.10)



90% overlapping



 true  
 estimated

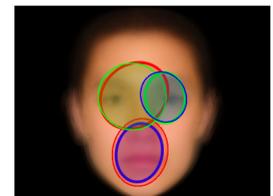
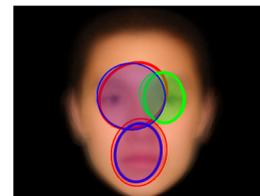
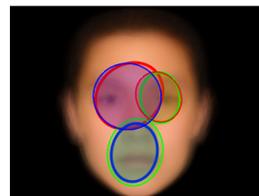
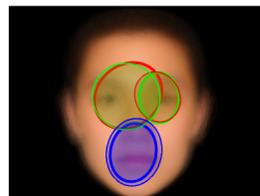
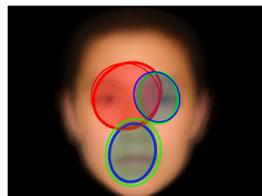
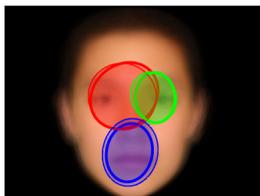
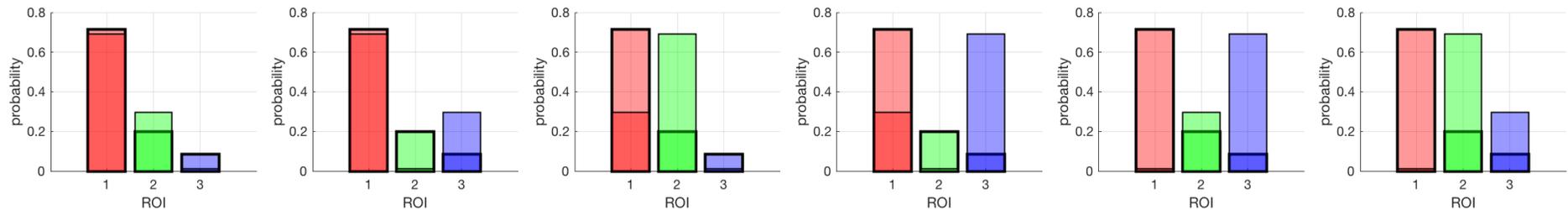
# Matched L1-norm error

- **Problem:**

- the order of the states in the GT and estimated HMMs may be different.

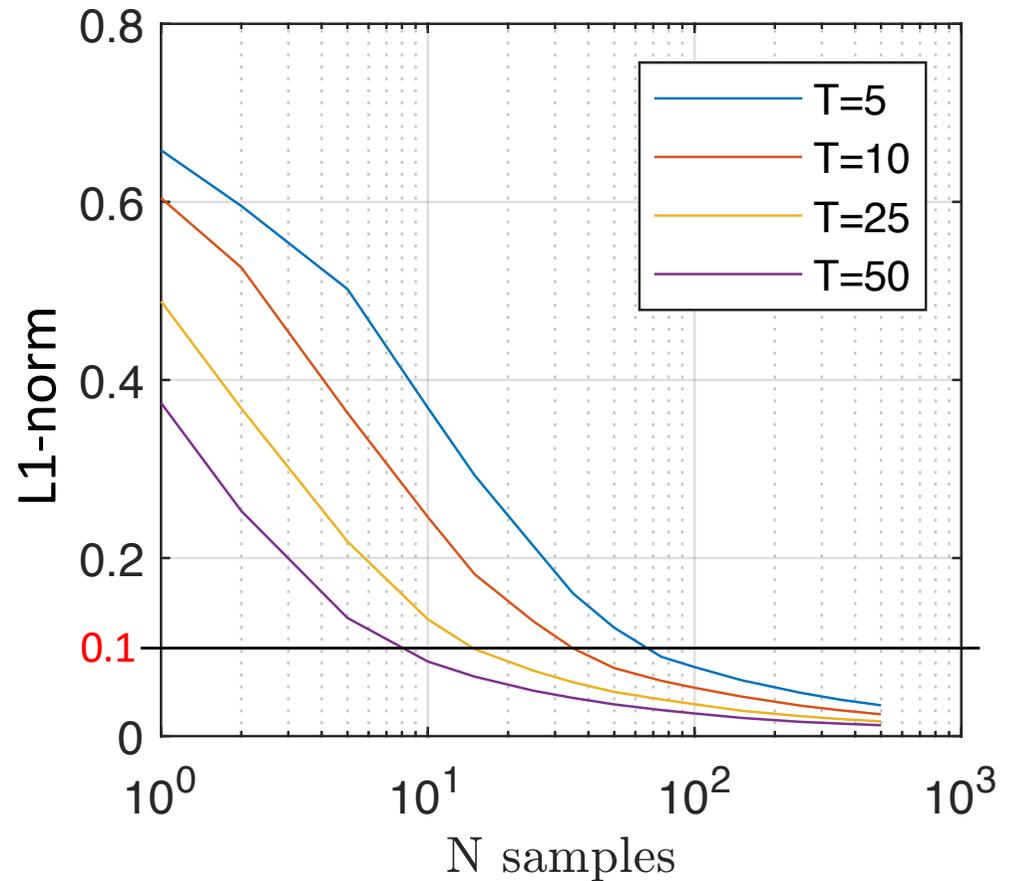
- **Solution:** align the states

- Matched L1-norm: the smallest L1-norm over all permutations of states.



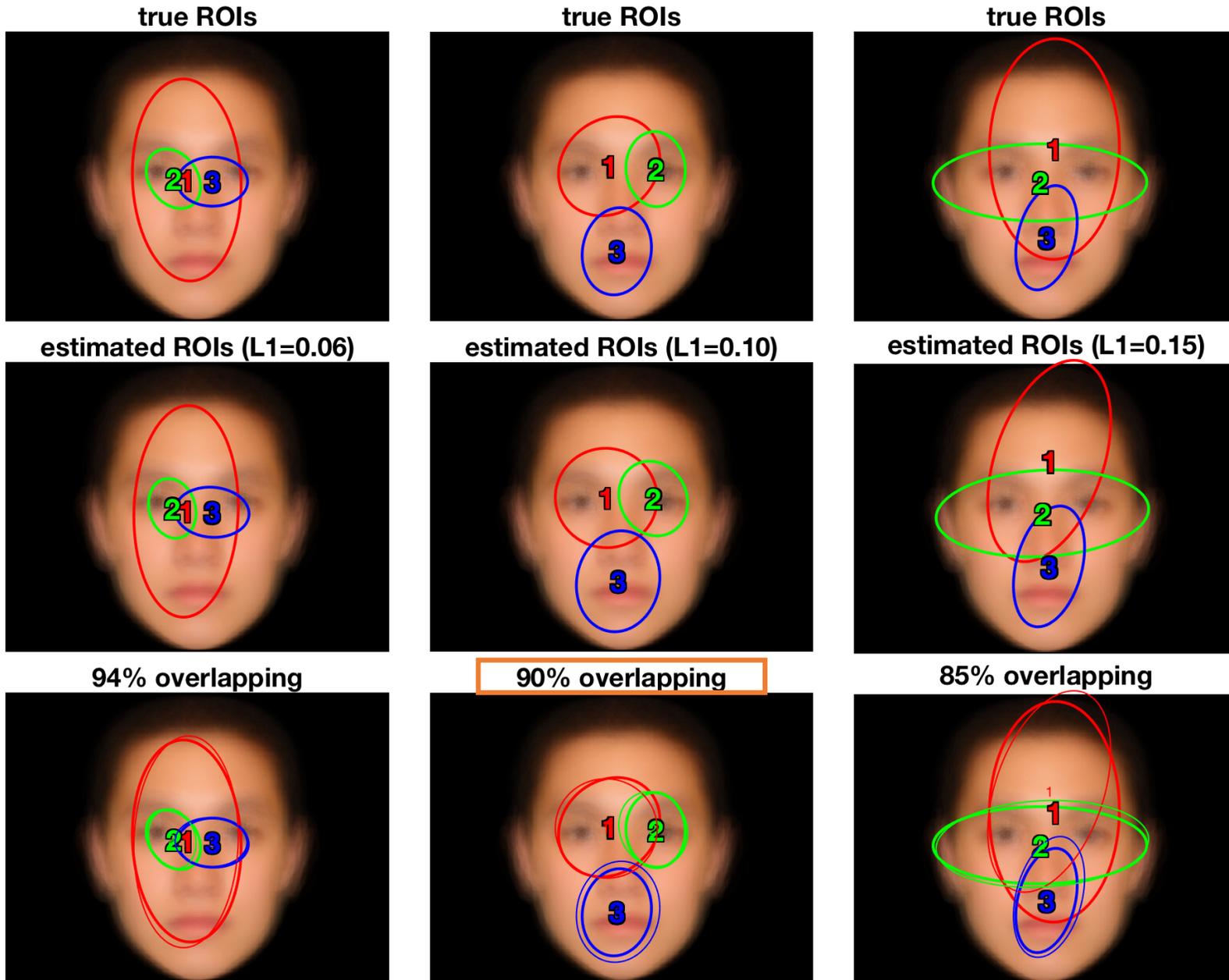
# Estimation Error for ROIs

- ROI overlap increases with number of fixations.
- For 90% overlap (L1-norm = 0.1) requires 350 total fixations:
  - $N=66, T=5$
  - $N=35, T=10$
  - $N=15, T=25$
  - $N=8, T=50$



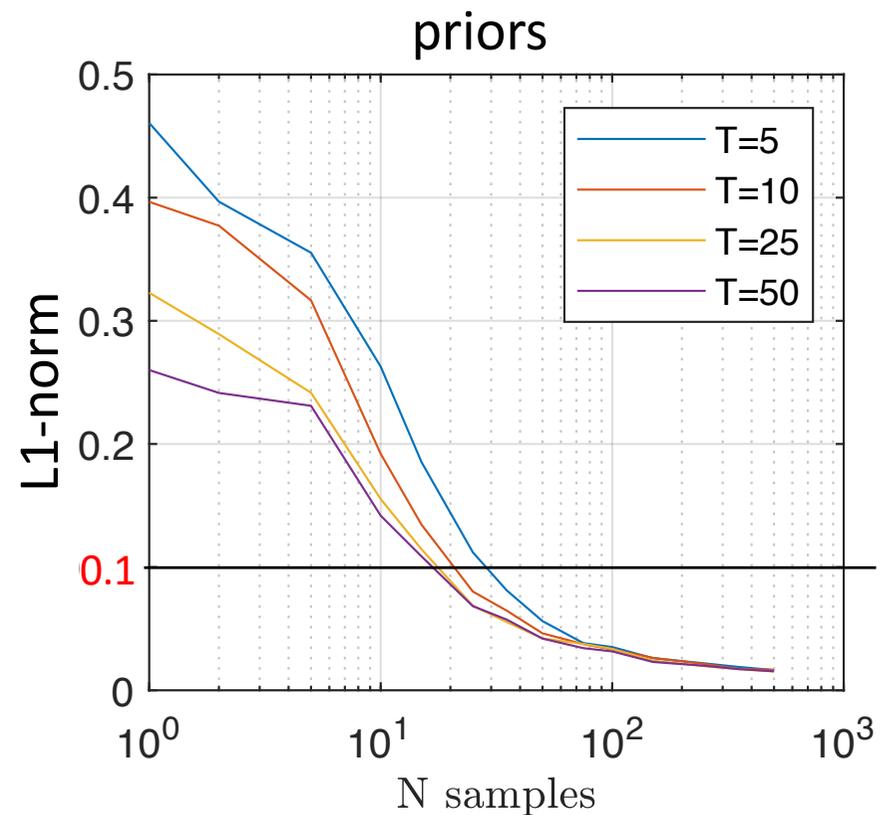
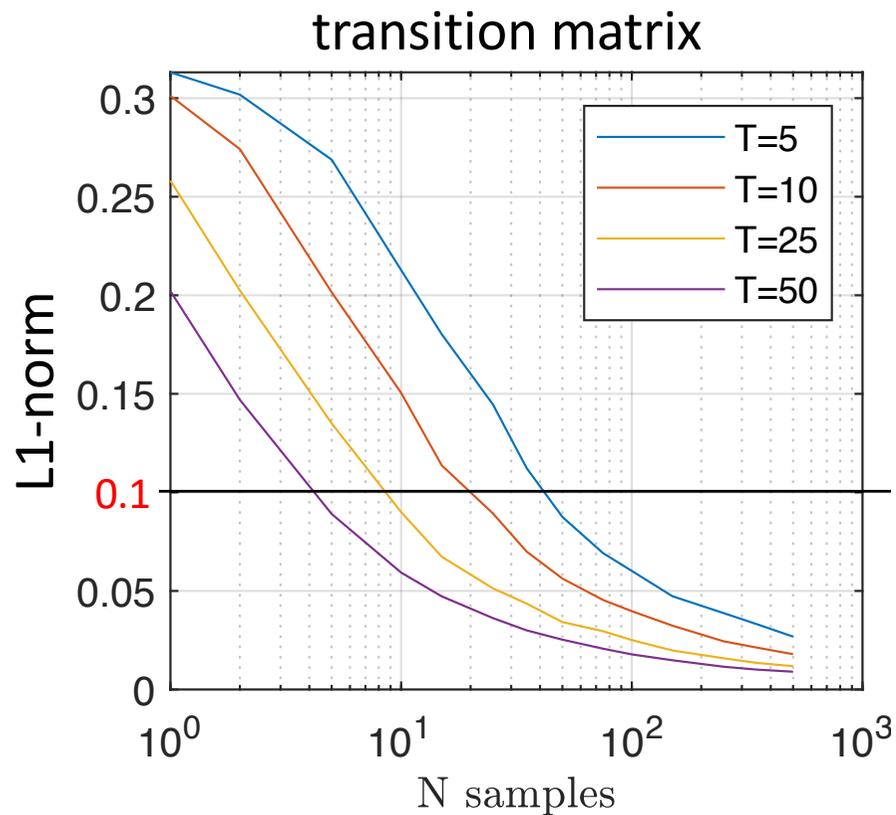
# ROI Examples

- 90% overlap of ROIs is equivalent to:
  - 4.7 pixel error in the ROI means
  - 4.5% change in the ROI sizes

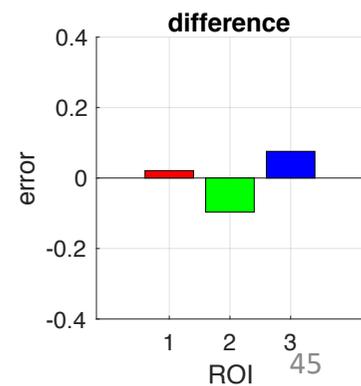
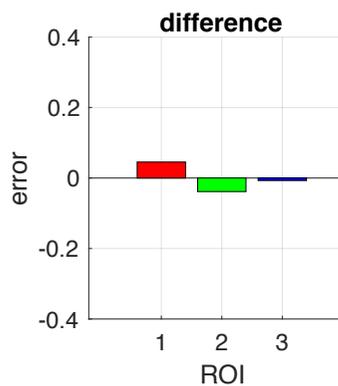
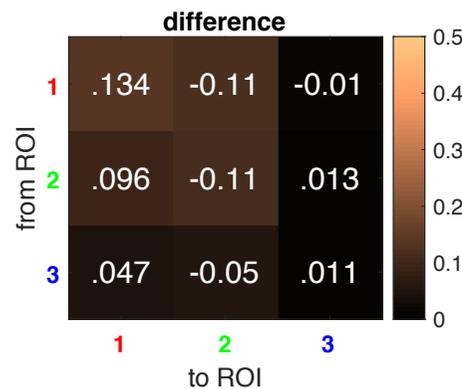
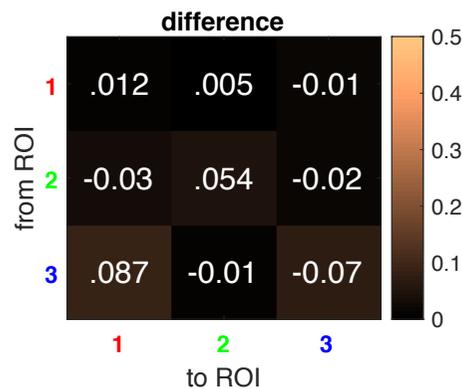
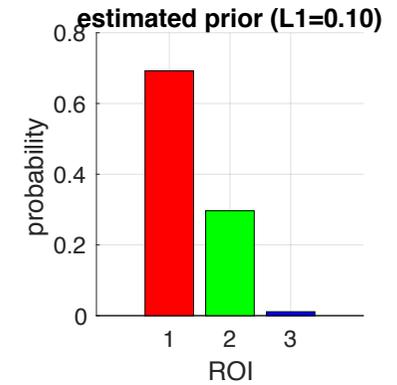
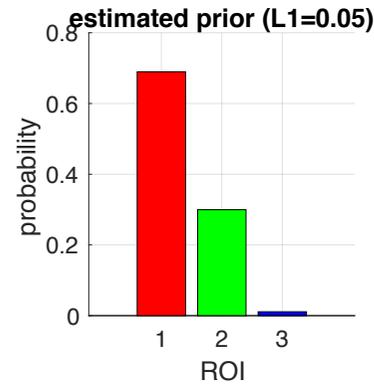
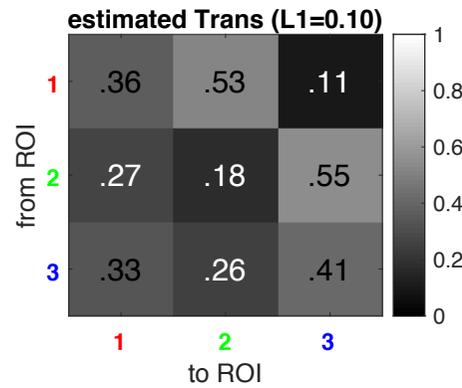
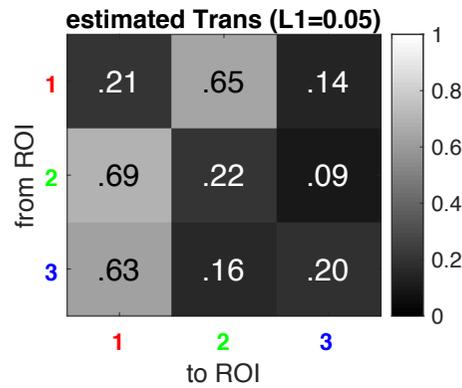
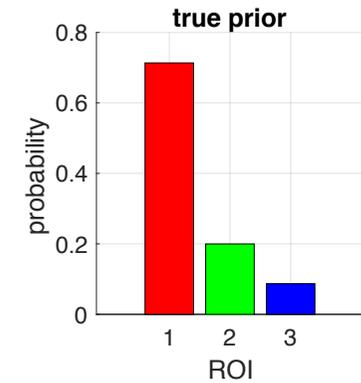
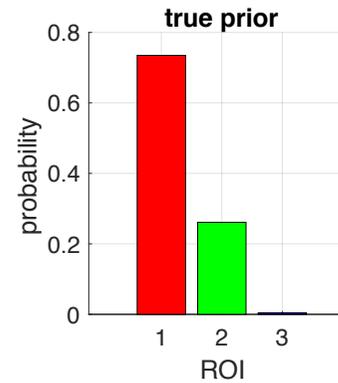
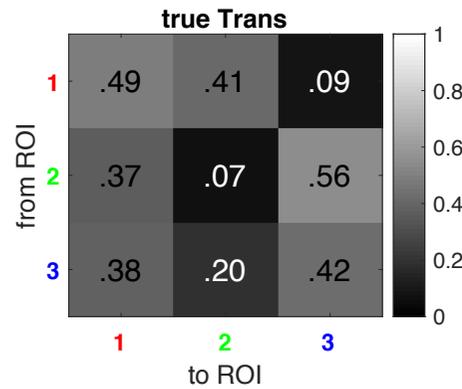
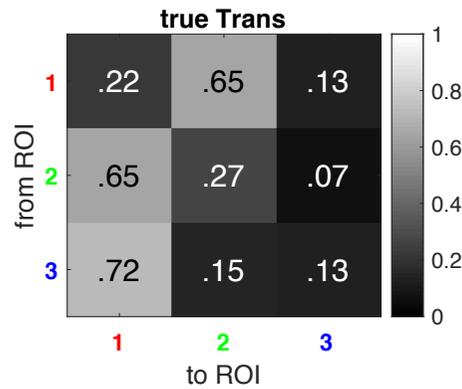


# Error for Transition/Prior

- 215 fixations for 90% overlap of transition matrices.
- ~25 sequences for 90% overlap of priors.



# Transition/Prior Examples



# Summary

- **Recommendations:**

- To estimate an HMM with 90% overlap with the *true* HMM:
  - at least 250-350 total fixations, at least 25 fixation sequences.
    - E.g., 25 fixation sequences of length 10
    - E.g., 50 fixation sequences of length 5
  - For 80% overlap:
    - at least 150 total fixations, 10 fixation sequences
- Estimated HMM is close to the true underlying strategy of the subject.
  - For interpreting *overall* eye gaze strategy of the person.

- **Note:**

- For less data, still okay to use estimated HMMs.
  - Estimated HMM represents eye gaze pattern on the *particular stimuli*, not the subject's underlying strategy.
  - Still valid for analysis, e.g., a classification/regression task.

# Questions?

- EMHMM toolbox:
  - <http://visal.cs.cityu.edu.hk/research/emhmm/>



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# Outline

- Experiment Design
  - Face recognition
  - Web page usage
- Simulation Study
  - *How many trials are needed?*
- Develop Your Mini-Experiment

# Mini-Experiment and Analysis

- 1) collect your own data
  - Psych Toolbox and EyeLink
  - Try to find a sample script that collects eye gaze data for similar tasks
- 2) use data available online (published papers)
- 3) use data you already collected
- 4) use data we collected
  - Scene perception: Use co-clustering to summarize eye movement patterns for animal and vehicle images separately, and see whether participants use consistent patterns across the two image types.
  - Website viewing: co-clustering across webpages; analyze other tasks.