

# Equilibrium refinement vs. level-k analysis: An experimental study of cheap-talk games with private information

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- 1.Introduction
- 2.Theory and hypotheses
- 3.Experimental procedures and results
- 4.Conclusion

# 1. Introduction

- 1. Cheap-talk games with complete information
  - Farrell (1987, 1988).
- 2. Cheap-talk games with incomplete information
  - Crawford and Sobel (1982)
- 3. “truth bias”
  - McCornack and Parks (1986).
- 4. “truth-detection bias”
  - Burgoon et al. (1994)

# Cheap-talk Game

- Senders: {A, B }
- Receiver = {X, Y, Z}.
- The payoffs for both players are then determined according to the combination of the sender's true type and the receiver's action.

# Payoff

Table 1  
Sender–receiver game payoff

## Game 1

		Action		
		<i>X</i>	<i>Y</i>	<i>Z</i>
Type	<i>A</i>	4, 4	1, 1	3, 3
	<i>B</i>	1, 1	4, 4	3, 3

## Game 2

		Action		
		<i>X</i>	<i>Y</i>	<i>Z</i>
Type	<i>A</i>	3, 4	2, 1	4, 3
	<i>B</i>	2, 1	3, 4	4, 3

## Game 3

		Action		
		<i>X</i>	<i>Y</i>	<i>Z</i>
Type	<i>A</i>	4, 4	1, 1	2, 3
	<i>B</i>	3, 1	2, 4	4, 3

## 2. Theory and hypotheses

- 2.1 Theories
- Separating equilibria
- Babbling equilibria
- AQRE(agent quantal response equilibrium)
- Level-k
- Refinements
- Sequential equil

- Babbling equilibrium :
  - sender's strategy is independent of type
  - receiver's strategy is independent of signal.
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- Separating equilibrium :
  - sender types sent signals from disjoint subsets of the set of available signals

## Predictions by Level-K

- - (1) In Games 1 and 2, the sender tells her type truthfully and the receiver believes the sender's messages.
  - (2) In Game 3, both sender types say they are type A, and the receiver plays Z upon receiving a and Y upon receiving b.



# Predictions by Level-K

Table 2

Level- $k$  predictions for Games 1, 2, and 3 when the  $L0$  sender is the truth-teller and the  $L0$  receiver is the randomizer

## Game 1

	Sender	Receiver
$L1$	$(a, b)$	$(X, Y)$
$L2$	$(a, b)$	$(X, Y)$
$L3$	$(a, b)$	$(X, Y)$

## Game 2

	Sender	Receiver
$L1$	$(a, b)$	$(X, Y)$
$L2$	$(a, b)$	$(X, Y)$
$L3$	$(a, b)$	$(X, Y)$

## Game 3

	Sender	Receiver
$L1$	$(a, b)$	$(X, Y)$
$L2$	$(a, a)$	$(X, Y)$
$L3$	$(a, a)$	$(Z, Y)$

# Predictions of play by various theories

Table 3

Predictions of play for Games 1, 2, and 3 by various theories

	Game 1	Game 2	Game 3
Sequential equil.	S.E and B.E.	S.E and B.E.	B.E.
Refinements	S.E.*	B.E.	B.E.
Level- $k^+$	$(ab, XY)$	$(ab, XY)$	$(aa, ZY)$

*Note:* S.E. means separating equilibria and B.E. means babbling equilibria.

\* AQRE predicts B.E. in this case.

+ Predicted play of higher levels is shown.

## 2.2 Hypotheses

- 1 (Equilibrium prediction).
- Most play conforms to a separating equilibrium in Game 1, a babbling equilibrium in Games 2 and 3.
- 2 (Overcommunication).
- Overcommunication occurs in games with conflicting interests. The more aligned the interests, the more frequently the sender tells the truth.

- 3 (Truth bias).
- Receivers tend to believe senders' messages to be truthful even in games with conflicting interests.
  
- 4 (Truth-detection bias).
- The receiver guesses the sender's true type more correctly when the sender tells the truth than when she tells a lie.

## 3.1 Experimental procedures

- 26 subjects  $\Rightarrow$  12+1 each sections
- 2 sections
- 13 rounds
- Payoff table(which game) and their roles
- Senders: {A, B } & Receiver : {X, Y, Z}
- Practice 3 rounds previously

# What's more?

- Randomly
- An envelope with written instructions, a recording sheet, and questionnaire.
- Instructors other than the authors read the instructions aloud and conducted the experiment manually.
- The instructors knew nothing about the equilibria of the games.

## 3.2. Experimental results

### 3.2.1. Aggregate data

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Table 4  
Aggregate data

#### Game 1

		<i>X</i>	<i>Y</i>	<i>Z</i>	Total
<i>A</i>	<i>a</i>	99	0	13	112
	<i>b</i>	0	4	1	5
<i>B</i>	<i>a</i>	3	0	1	4
	<i>b</i>	1	92	20	113
Total		103	96	35	234

#### Game 2

		<i>X</i>	<i>Y</i>	<i>Z</i>	Total
<i>A</i>	<i>a</i>	20	1	10	31
	<i>b</i>	1	5	2	8
<i>B</i>	<i>a</i>	3	1	0	4
	<i>b</i>	5	19	11	35
Total		29	26	23	78

#### Game 3

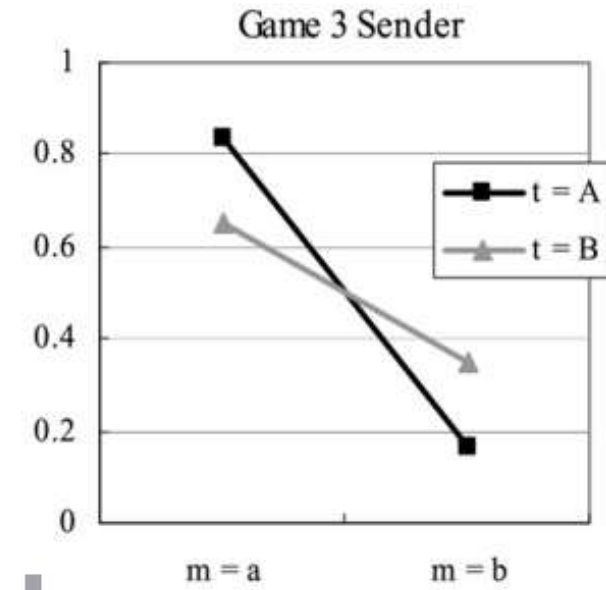
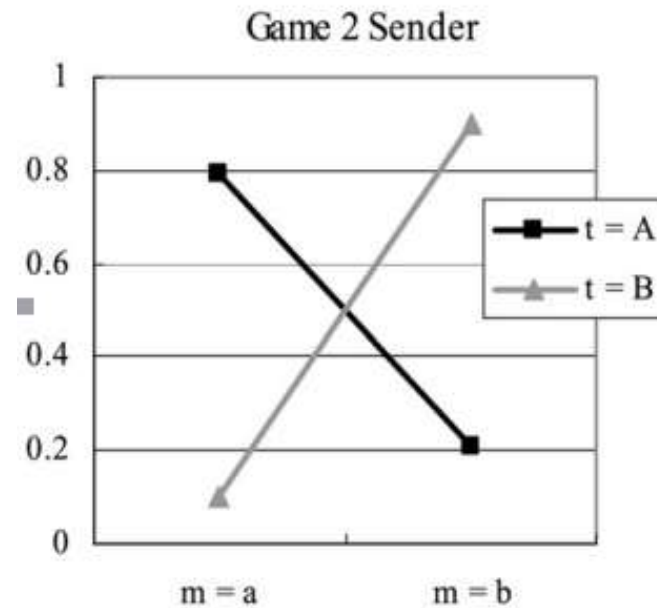
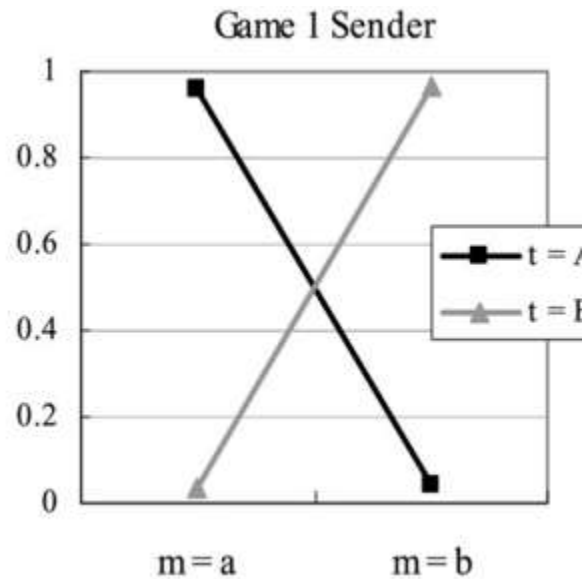
		<i>X</i>	<i>Y</i>	<i>Z</i>	Total
<i>A</i>	<i>a</i>	45	9	43	97
	<i>b</i>	1	9	10	20
<i>B</i>	<i>a</i>	26	12	40	78
	<i>b</i>	6	19	14	39
Total		78	49	107	234

- **Result 1.**
- The majority of play in Games 1 and 2 was separating equilibria, and a notable proportion of play was separating in Game 3 even though it has only babbling equilibria.
- (Hypothesis 1 is rejected)

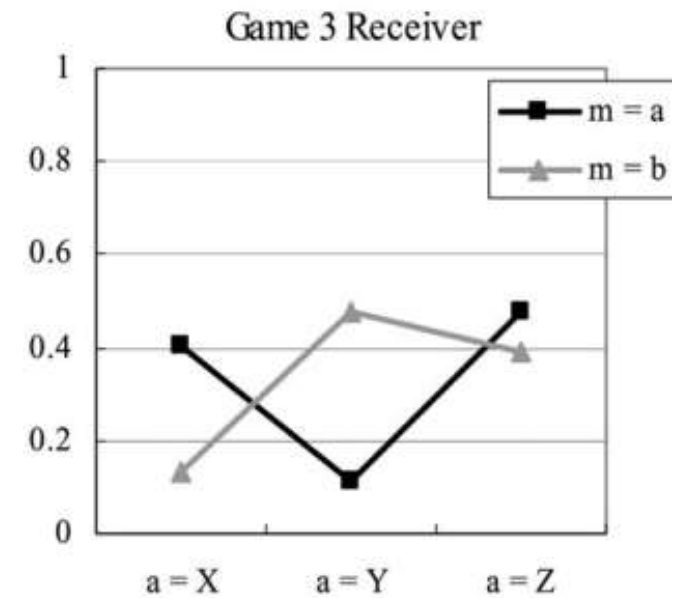
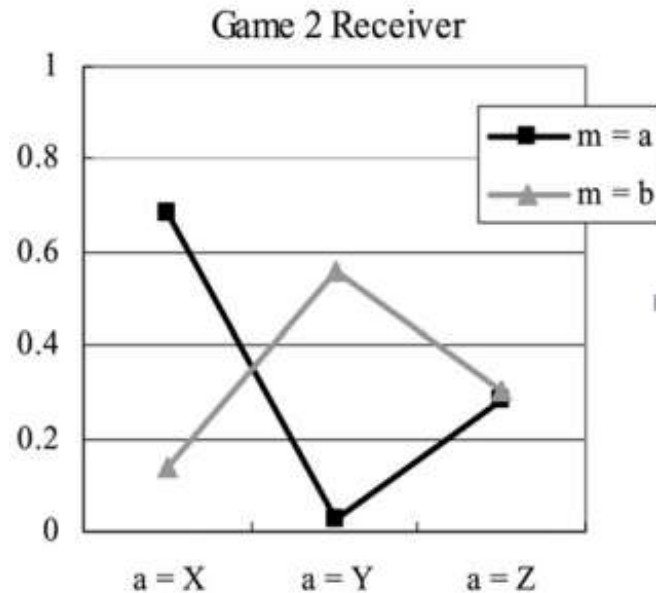
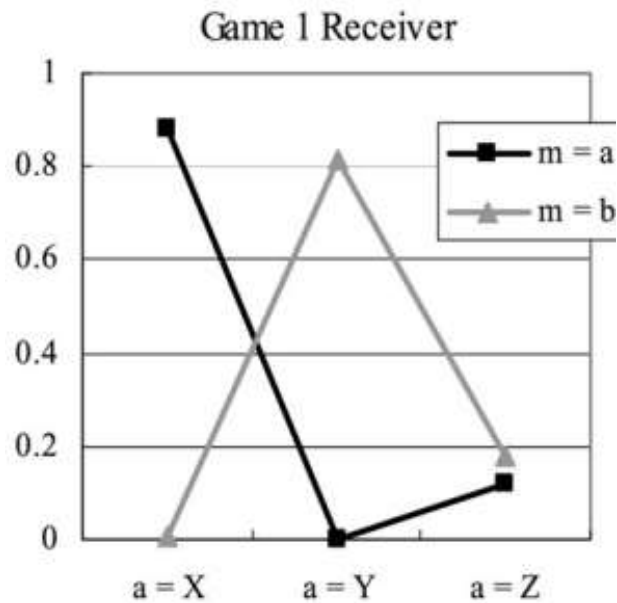


- **Result 2.**

- Overcommunication is observed in Games 2 and 3. The more aligned the interests are between sender and receiver, the more frequently the sender tells the truth.



- **Result 3.**
- Truth bias is observed. Furthermore, the more aligned the interests are between sender and receiver, the more frequently receiver believes the sender's message to be truthful.



- **Result 4.**
- Truth-detection bias is observed.
- The receiver guesses the sender's true type more correctly when the sender tells the truth than when she tells a lie.

## 3.2.2. Individual data

- level-k analysis can explain our experimental data better than any other theories.

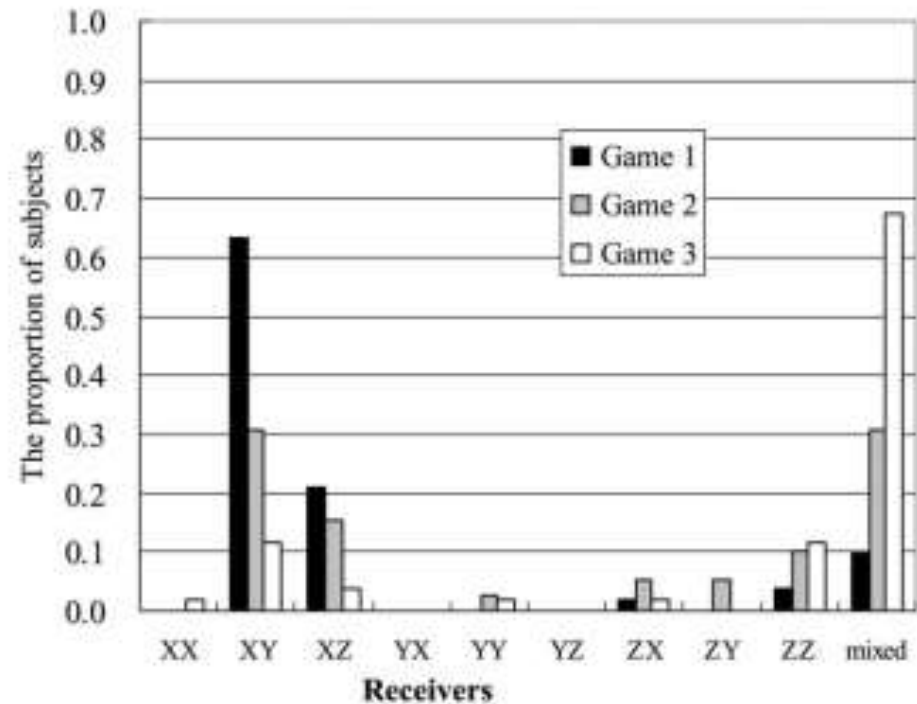
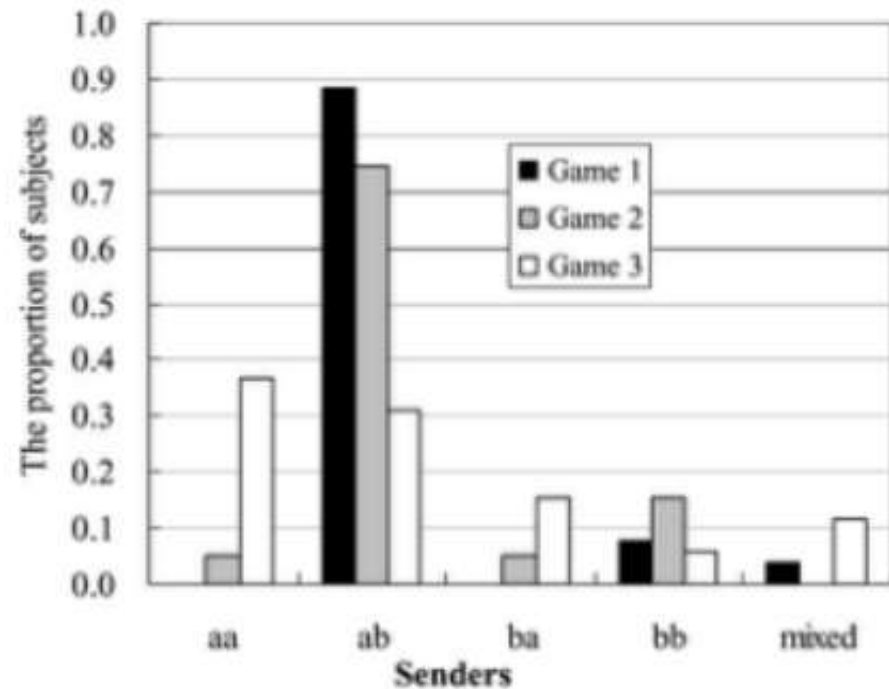


Fig. 3. The distribution of each behavioral type.

## 4. Conclusion

- 1.The less aligned the interests===» » » the more frequently babbling equilibrium play.
- 2.Refinement theories only work in the case of aligned interests, **level-k analysis works well in conflicting interest cases as well as in aligned interest cases.**
- 3.Confirm the existence of “truth bias” and “truth-detection bias.”
- 4.**Truth-telling and truth-guessing are more intrinsic to human communication than is supposed in game theory.**

# •Thanks

- Sishi Lin