

SPRING 2010

即時控制系統設計 Design of Real-Time Control Systems

Lecture 21 Fundamentals of Digital Control

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NTU-EE

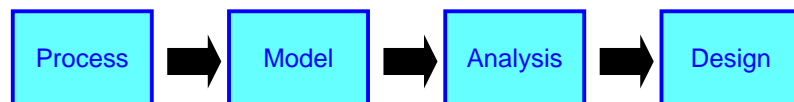
Feb10 – Jun10

Digital Control Systems

- Study in Digital Control Systems
 - Introduction
 - Mathematical model of digital control systems
 - Dynamic analysis of digital control systems
 - Controller design of digital control systems
- Digitalization
 - Control system block diagram
 - Sampling rate
 - Time delay

The Design Philosophy of Control Science

▪ The Research Procedure in Control Science



- | | | | |
|-----------------|---------------------|-------------------|--------------------|
| ▪ Plant | ▪ Differential eqn | ▪ Root locus | ▪ Estimator |
| ▪ Sensor | ▪ Laplace transform | ▪ Bode diagram | ▪ Identification |
| ▪ Actuator | ▪ Transfer function | ▪ Nyquist plot | ▪ Regulation |
| ▪ Computer | ▪ State space form | ▪ Stability | ▪ Tracking |
| ▪ Communication | | ▪ Robustness | ▪ PID |
| ▪ Noise | ↓ | ▪ Sensitivity | ▪ Pole placement |
| ▪ Disturbance | ▪ Difference eqn | ▪ Controllability | ▪ Optimal Control |
| | ▪ z transform | ▪ Observability | ▪ LQR/LQG |
| | ▪ Transfer function | | ▪ Adaptive control |
| | ▪ State space form | | ▪ Robust control |

Digital Control Systems

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- Study in Digital Control Systems
 - Introduction:
 - Systems:
 - > continuous-time systems
 - > discrete-time systems
 - > sampled-data systems
 - > digital systems
 - Controls:
 - > analog/continuous control
 - > digital/discrete control
 - > classical control
 - > modern control
 - Design Issues:
 - > hardware
 - > software

Study in Digital Control Systems

– Characteristics of DT Control Systems

- > open-loop systems
- > A/D converters
- > D/A converters
- > Resolver/synchror-to-digital converters
- > closed-loop systems

- > computer
- > microcontroller
- > DSP
- > microprocessor

Study in Digital Control Systems

• Mathematical Model of Digital Control Systems

- Discrete-time systems
- Linear difference equations
 - > Derivative approximation:
 - » With a forward difference (Euler's method)
 - » With a backward difference
 - » With a trapezoidal method (Tustin's approximation)
- Unit pulse function, unit step function, etc.,
 - > discrete convolution
 - > the z-transform
 - » Definition
 - » Properties
 - » Convergence

Study in Digital Control Systems

• Mathematical Model of Digital Control Systems

- From analog to digital
 - > sampling/sampling times
 - > time & frequency characteristics
- DT transfer functions
 - > via Numerical Integration
 - » Forward rule (Euler's method)
 - » Backward rule
 - » Trapezoidal rule (Tustin's method, bilinear transformation)
 - » Bilinear transformation with pre-warping
 - > via Zero-Pole Matching
 - > via Hold equivalents
- DT frequency response
- Relationship between s and z domains

Study in Digital Control Systems

• Dynamic Analysis of Digital Control Systems

- By Transform methods (by transfer function)
 - > poles, zeros
 - > stability
 - > transient response
 - > steady-state response
 - > impulse/step response
 - > root locus
 - > Bode plot
- By State-Variable methods (by state-space model)
 - > CT \rightarrow DT
 - > linear
 - > nonlinear
 - > stability analysis
 - > sensitivity analysis
 - > controllability
 - > observability

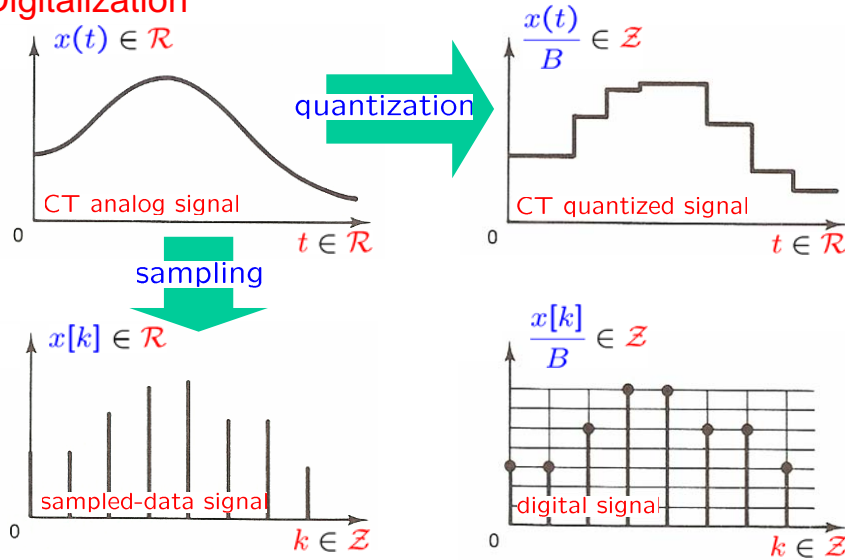
- Study in Digital Control Systems
 - Controller Design of Digital Control Systems
 - Design Process
 - > Emulation:
 - » CT plant -> CT controller -> DT controller
 - > Discrete Design:
 - » CT plant -> DT plant -> DT controller
 - > Direct Design: (B.D.O. Anderson, 1992 Bode Prize Lecture)
 - » CT plant -> DT controller

- Study in Digital Control Systems
 - Controller Design of Digital Control Systems
 - Transfer Function Design Methods
 - > Dynamic parameters
 - » peak time
 - » overshoot
 - » settle time
 - » rise time
 - > Steady-state parameters
 - » steady-state error
 - > Design tools
 - » root-locus in z-domain
design specifications
 - » frequency response methods
design specifications
gain & phase margins
tracking error, stability robustness in terms of sensitivity function
Bode plots, Nyquist stability criterion
compensator design

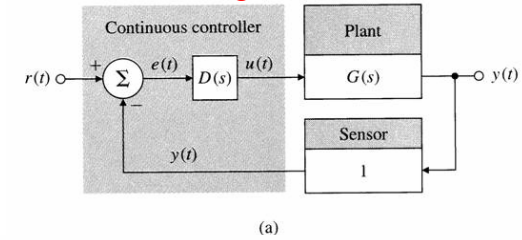
- Study in Digital Control Systems
 - Controller Design of Digital Control Systems
 - Transfer Function Design Methods
 - > Design techniques:
 - » Tustin's Method or bilinear approximation
 - » Matched Pole-Zero method (MPZ)
 - » Modified Matched Pole-Zero method (MMPZ)
 - > Compensator/controller
 - » pole placement & model matching
 - » phase-lead & phase lag compensators
 - » PID controller
 - » deadbeat controller

- Study in Digital Control Systems
 - Controller Design of Digital Control Systems
 - State-Space Design Methods
 - > Analysis
 - > Design
 - » state feedback (controllability)
 - » state estimation (observability)
 - » regulator: controller + estimator
 - » linear quadratic optimal control (LQR, LQG)
 - » nonlinear control

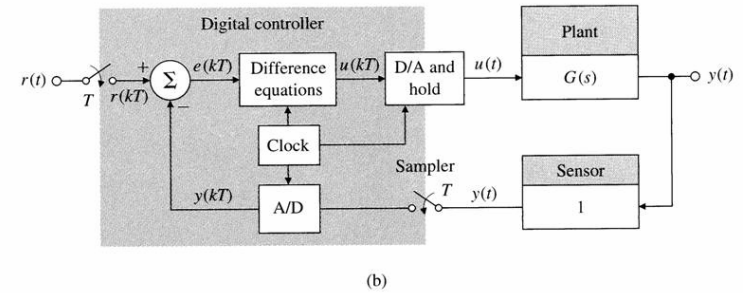
▪ Digitalization



▪ Control System Block Diagram

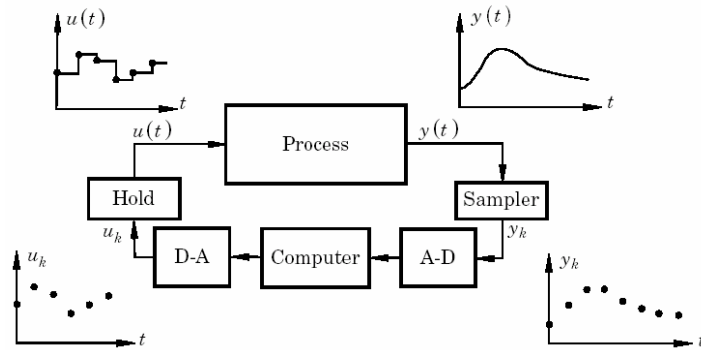


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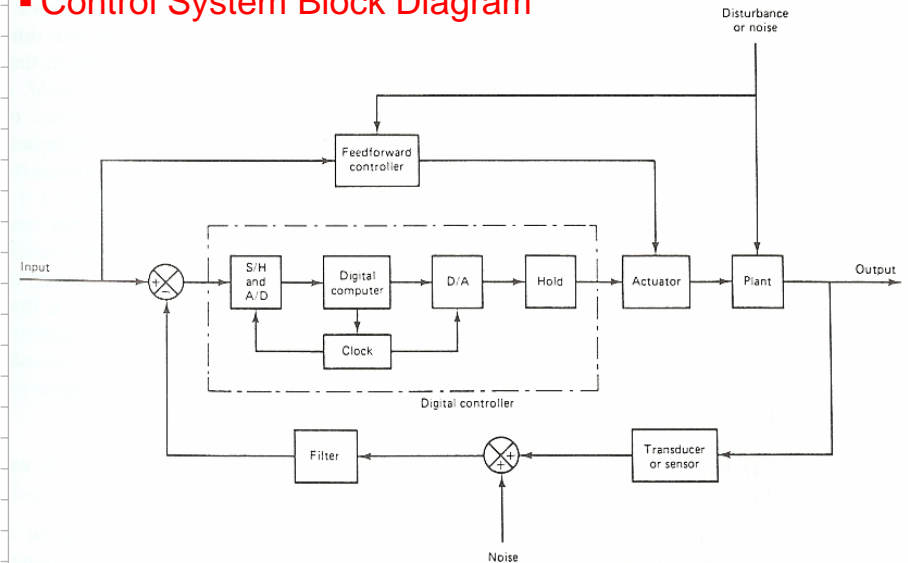


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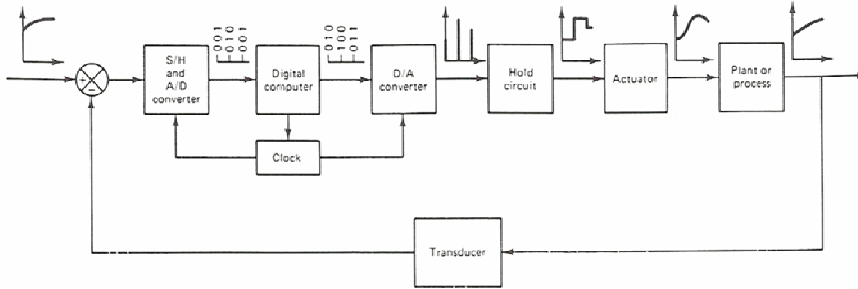
▪ Control System Block Diagram



▪ Control System Block Diagram



Control System Block Diagram



Ogata 1995

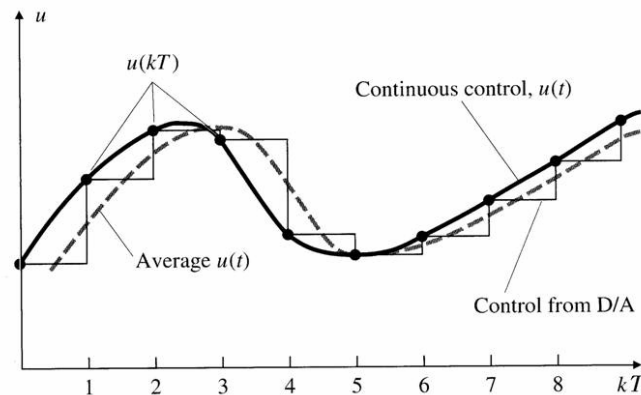
Sample Rate:

- The **sample rate** required depends on the **closed-loop bandwidth** of the system
- Generally, **sample rates** should be about **20 times** the bandwidth or faster in order to assure that the digital controller will **match the performance** of the CT controller

Franklin, Powell & Emami-Naeini 2002

Time Delay:

- The **delay** associated with the hold
- On average**, continuous signals are delayed by $T/2$



Franklin, Powell & Emami-Naeini 2002