Homework 3: z Transform & Sampling

- Problem 3-1:
 - Consider the system described by the difference equation:

$$y[k+2] - 1.5y[k+1] + 0.5y[k] = u[k+1]$$

- When u[k] is a step at k = 0 and when y[0] = 0.5 and y[-1] = 1.
- a) Use the z-transform to determine the pulse-transfer function and the poles and zeros of the system (Done in HW02: 2-3).
- b) Determine the output sequence of the difference equation
- c) Find the relationship between its poles/zeros and the kernel (or basis) functions of the output sequence.

Problem 3-2:

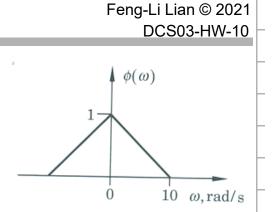
- Consider the system: $\frac{z+b}{(1+b)(z^2-1.1z+a)}$
- The pole location corresponds to a continuous-time system with damping $\zeta = 0.7$.
- Simulate the system and determine the overshoot for different values of a and b: $a \in [0.3, 0.5], b \in [-0.75, 0.75]$

3/23/21

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Problem 3-3:

- Assume that the magnitude of the spectrum of a signal is:
- Sketch the magnitude of the spectrum when the signal has been sampled with:
 (a) h = 2π/10 (s); (b) h = 2π/20 (s); (c) h = 2π/50 (s).



• You need to identify as many important frequency locations as possible and describe the reason of determining the locations.

Problem 3-4:

- Watch the following plenary speech (by either video, slide, or paper):
 - Signal Processing via Sampled-Data Control A Challenge to Go Beyond Shannon
 - By Prof. Yutaka Yamamoto (Kyoto University, Japan)
 - http://www.ieeecss-oll.org/lecture/signal-processing-sampled-data-control-challenge-go-beyond-shannon
 - http://archive.dimacs.rutgers.edu/Workshops/ControlTheory/Slides/Yamamoto.pdf
 - https://ieeexplore.ieee.org/document/6072311
- Please describe the key information of the speech and summarize the idea delivered in the speech.