Fall 2021 (110-1)

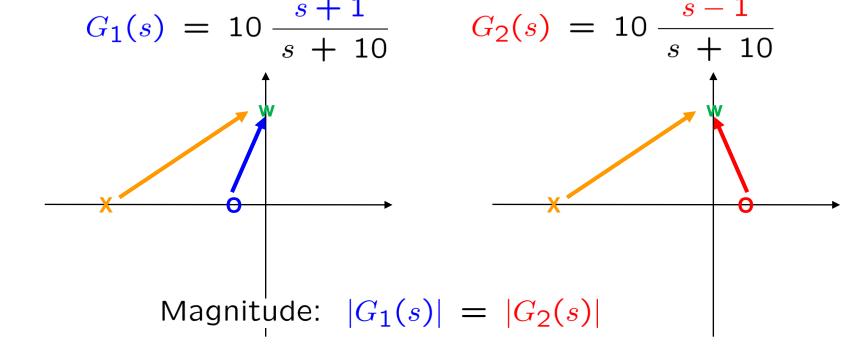
## 控制系統 Control Systems

Unit 6C Non-Minimum Phase and Steady-State Errors

> Feng-Li Lian NTU-EE Sep 2021 – Jan 2022

NI. NATALANA

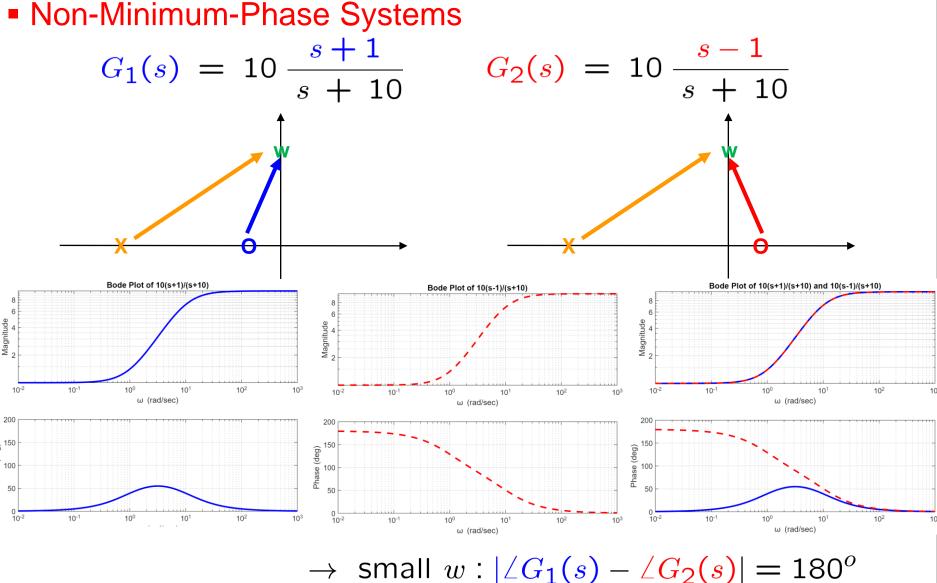
## Non-Minimum-Phase Systems



Phase:  $\angle G_1(s), \angle G_2(s)$ : different

For this example,

$$ightarrow$$
 small  $w: |\angle G_1(s) - \angle G_2(s)| = 180^o$   
ightarrow large  $w: |\angle G_1(s) - \angle G_2(s)| = 0^o$ 



$$\rightarrow$$
 large  $w: | \angle G_1(s) - \angle G_2(s) | = 0^o$ 

In Section 4.2,

| Type Input | Step (position)   | Ramp (velocity)   | Parabola (acceleration) |
|------------|-------------------|-------------------|-------------------------|
| Type 0     | $\frac{1}{1+K_p}$ | $\infty$          | $\infty$                |
| Type 1     | 0                 | $\frac{1}{K_{V}}$ | $\infty$                |
| Type 2     | 0                 | 0                 | $\frac{1}{K_a}$         |

**Errors as a Function of System Type** 

- As the gain of the open-loop transfer function increases,
- Steady-State Error of a feedback system decreases.
- In Section 6.1.1,  $KG(jw) = K_0 (jw)^n \frac{(jw\tau_1 + 1)(jw\tau_2 + 1)\cdots}{(jw\tau_a + 1)(jw\tau_b + 1)\cdots}$ 
  - At very low frequencies, OL TF is approximated by

$$K G(jw) \approx K_0 (jw)^n$$

- Larger the magnitude on low-frequency asymptote,
- Lower steady-state errors

## Steady-State Errors

$$K G(jw) \approx K_0 (jw)^n$$

For n = 0, a Type 0 system,

$$e_{ss} = \frac{1}{1 + K_p}$$

Errors as a Function of System Type

 Type Input
 Step (position)
 Ramp (velocity)
 Parabola (acceleration)

 Type 0
 
$$\frac{1}{1+K_p}$$
 $\infty$ 
 $\infty$ 

 Type 1
 0
  $\frac{1}{K_v}$ 
 $\infty$ 

 Type 2
 0
 0
  $\frac{1}{K_a}$ 

- For n = -1, a Type 1 system,
  - The low-frequency asymptote has a slope of -1.
  - The gain =  $K_o/\omega$  and the velocity-error constant is:

$$K_v = K_o$$

- For a unity-feedback system with a unit-ramp input,
- The steady-state error is:

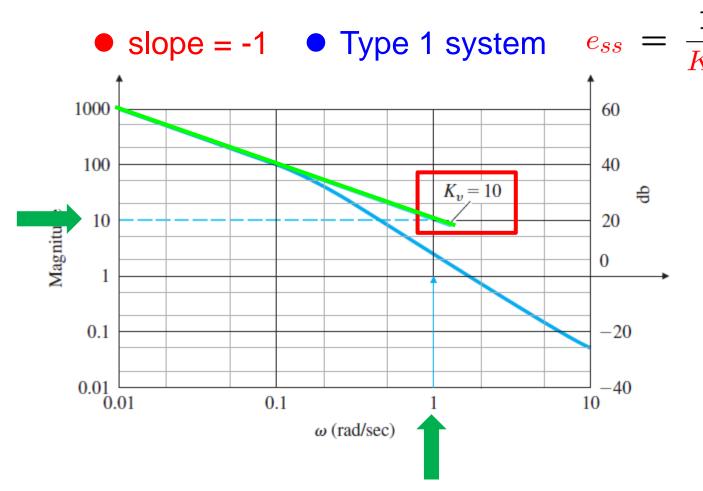
$$= \frac{1}{K_v}$$

- The easiest way of determining  $K_v$  in a Type 1 system
- is to read the magnitude of the low-frequency asymptote at  $\omega = 1$  rad/sec,
- because this asymptote is  $A(\omega) = K_v / \omega$ .

- In some cases, the lowest-frequency break point
   will be below ω = 1 rad/sec;
- Therefore, the asymptote needs to extend to  $\omega = 1$  rad/sec in order to read  $K_v$  directly.

**Example 6.7: Computation of**  $K_v$ 

$$KG(s) = \frac{10}{s(s+1)}$$



• Or, by  $A(\omega) = K_v / \omega \rightarrow 1000 = K_v / 0.01 \rightarrow K_v = 10$