Spring 2020

控制系統 Control Systems

Unit 6K PID Compensation

Feng-Li Lian & Ming-Li Chiang

NTU-EE

Mar 2020 – Jul 2020

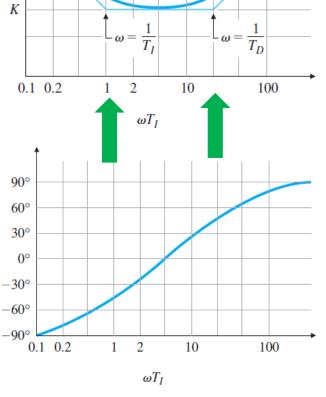
- PID Compensation
 - \triangleright Need PM improvement at ω_c
- ➤ Need low-frequency gain improvement
- A common transfer function:

$$D_c(s) = k_P + \frac{k_I}{s} + k_D s$$

$$D_c(s) = \frac{K}{s} \left[\left(T_D s + 1 \right) \left(s + \frac{1}{T_I} \right) \right]$$

Roughly equivalent to

combining lead and lag compensations referred to as a lead-lag compensator



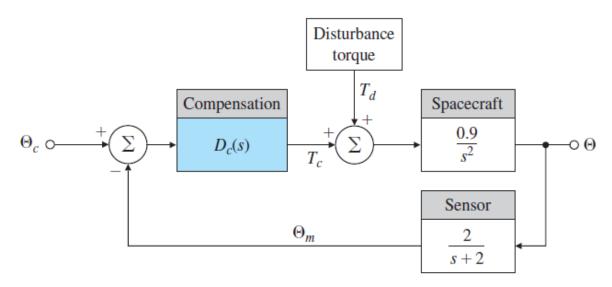
10K

2K

 $|D_c(s)|$

 $\angle D_c(s)$

for Spacecraft Attitude Control



- Design PID controller for:
 - Zero steady-state error
 - $PM = 65^{\circ}$
 - As high a bandwidth as possible
 - Torque disturbance $\omega = 0.001 \text{ rad/sec}$

for Spacecraft Attitude Control

For Final Steady Value

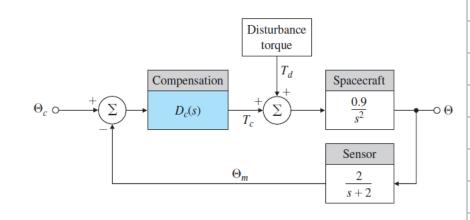
$$\rightarrow T_d + T_c = 0$$

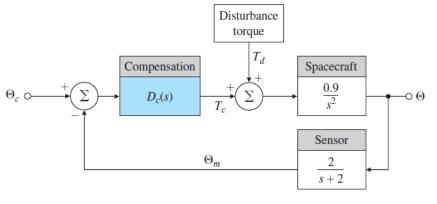
• Therefore, if $T_d = /= 0$

$$\rightarrow$$
 $T_c = - T_d$

for $D_c(s)$ to contain an integral term.

■ The only way this can be true with no error (e = 0) is:



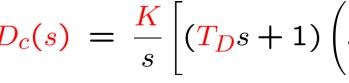


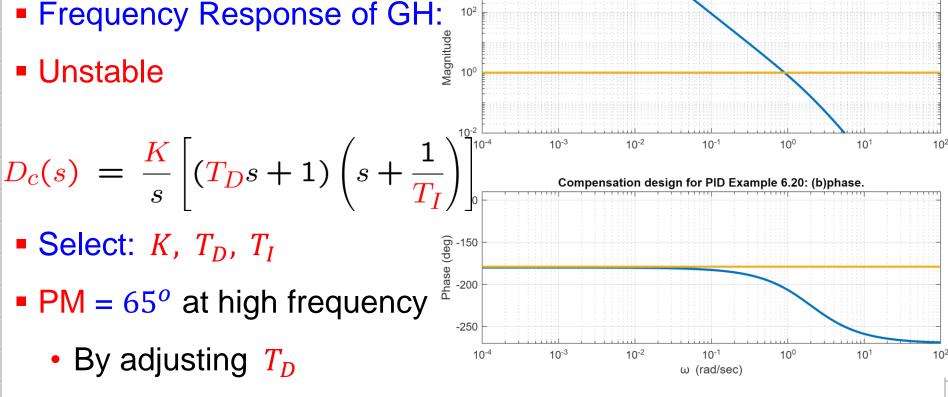
for Spacecraft Attitude Control

Compensation for PID design Example 6.20: (a) magnitude.

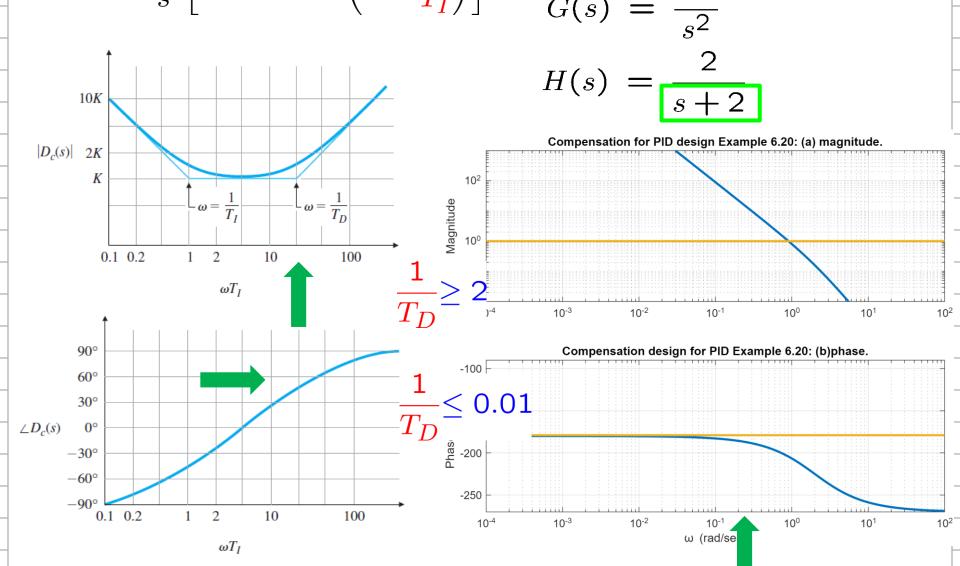
$$H(s) = \frac{2}{s^2}$$

$$H(s) = \frac{2}{s+2}$$



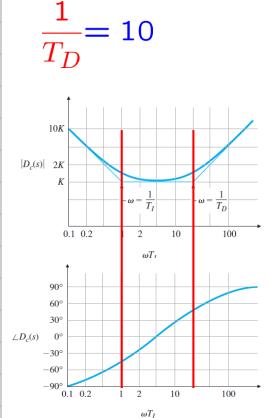


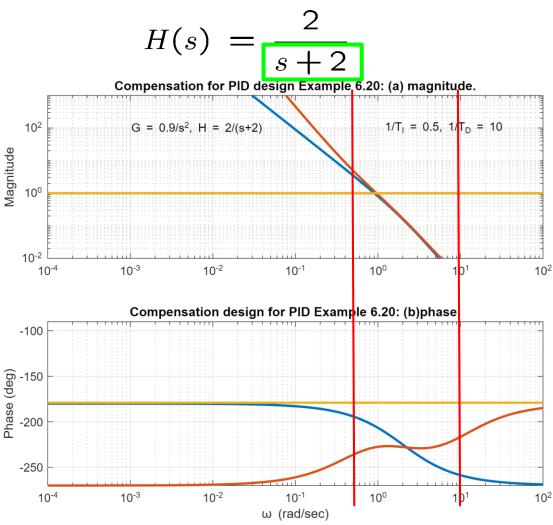
$$D_c(s) = \frac{K}{s} \left[(T_D s + 1) \left(s + \frac{1}{T_I} \right) \right]$$
 for Spacecraft Attitude Control



$$D_c(s) = \frac{K}{s} \left[(T_D s + 1) \left(s + \frac{1}{T_I} \right) \right]$$
 for Spacecraft Attitude Control $G(s) = \frac{0.9}{s^2}$

$$D_c(s) = rac{K}{s} \left[(T_D s + 1) \left(s + rac{1}{T_I}
ight)
ight]$$
 $rac{1}{T_I} = 0.5$ $rac{1}{T_D} = 10$





Magnitude

-250

10-4

10⁻³

10⁻²

Example 6.20: PID Compensation

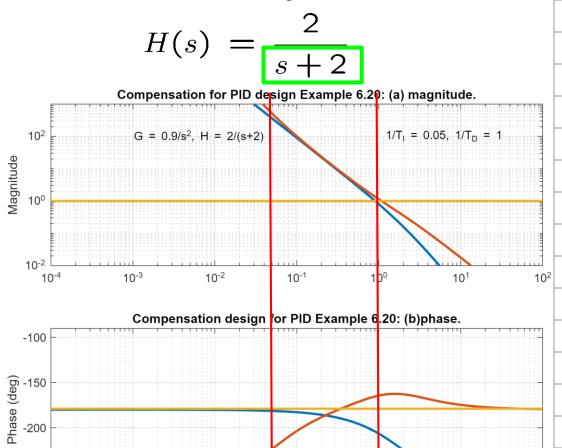
$$D_c(s) = \frac{K}{s} \left[(T_D s + 1) \left(s + \frac{1}{T_I} \right) \right]$$
 for Spacecraft Attitude Control $G(s) = \frac{0.9}{s^2}$

$$\frac{1}{T_{I}} = 0.05$$

$$\frac{1}{T_{D}} = 1$$

$$\frac{1}{T_$$

 ωT_I



10⁻¹

ω (rad/sec)

10⁰

10¹

 10^{2}

10⁻³

10-4

10⁻²

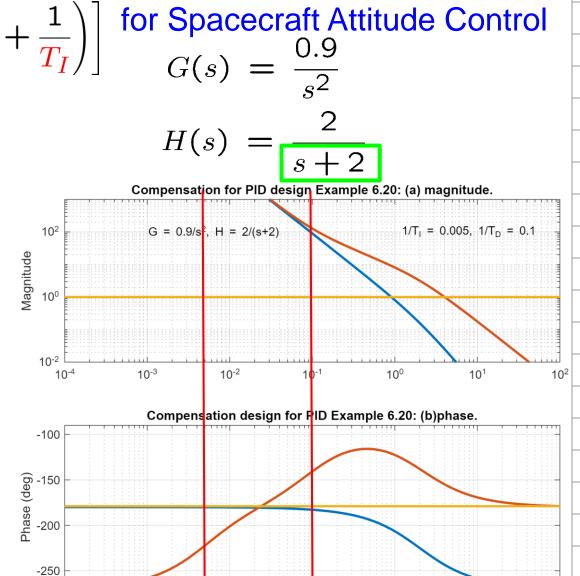
Example 6.20: PID Compensation

$$D_c(s) = rac{K}{s} \left[(T_D s + 1) \left(s + rac{1}{T_I}
ight) \right]$$
 fo

$$\frac{1}{T_I} = 0.005$$

$$\frac{1}{T_D} = 0.1$$

$$\frac{1}{T_D$$



10⁻¹

ω (rad/sec)

10⁰

10¹

 10^{2}

CS6K-CLFreqResp - 10

Example 6.20: PID Compensation

$$D_c(s) = rac{K}{s} \left[(T_D s + 1) \left(s + rac{1}{T_I}
ight) \right]$$
 for Spacecraft Attitude Control $G(s) = rac{0.9}{s^2}$

$$c(s) = \frac{R}{s} \left[(T_D s + 1) \left(s + \frac{1}{T_I} \right) \right]^{100}$$

Aagnitude

-100

-150

-200

-250

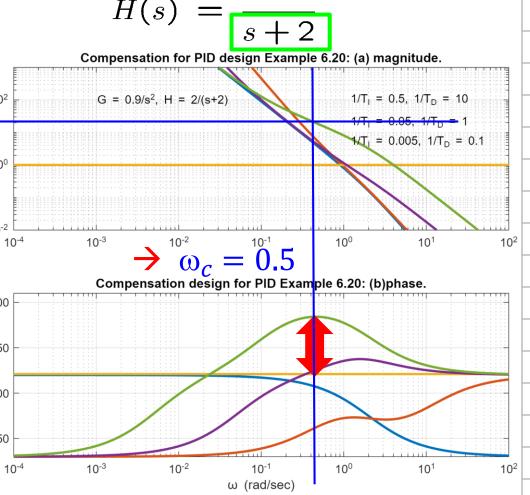
Phase (deg)

$$\frac{1}{T_I} = 0.5$$
 $\frac{1}{T_D} = 10$ $\frac{1}{T_I} = 0.05$ $\frac{1}{T_D} = 1$ $\frac{1}{T_D} = 1$

$$\frac{1}{T_D} = 1$$
 $\frac{1}{T_D} = 0.1$



 $PM = 65^{\circ}$



$$D_c(s) = rac{K}{s} \left[(T_D s + 1) \left(s + rac{1}{T_I}
ight) \right]$$
 for

$$\begin{aligned} \mathcal{D}_{\boldsymbol{c}}(s) &= \frac{K}{s} \left[(T_D s + 1) \left(s + \frac{1}{T_I} \right) \right] & \text{for Spacecraft Attitude Control} \\ G(s) &= \frac{0.9}{s^2} \end{aligned}$$

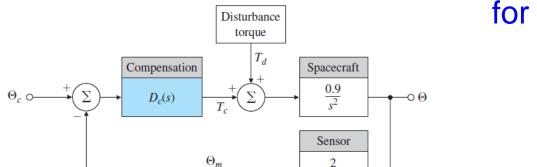
$$= \frac{0.05}{s} \left[(10s + 1) \left(s + \frac{1}{0.005} \right) \right] & H(s) &= \frac{2}{s + 2}$$

$$= \frac{0.05}{s} \left[(10s + 1) \left(s + \frac{1}{0.005} \right) \right] & G_{\text{compensation for PID design Example 6.20: (a) magnitude.}$$

$$= \frac{100}{s} \left[(10s + 1) \left(s + \frac{1}{0.005} \right) \right] & G_{\text{compensation design for PID Example 6.20: (b) phase.}$$

$$= \frac{100}{s} \left[(10s + 1) \left(s + \frac{1}{0.005} \right) \right] & G_{\text{compensation design for PID Example 6.20: (b) phase.}$$

$$= \frac{100}{s} \left[(10s + 1) \left(s + \frac{1}{0.005} \right) \right] & G_{\text{compensation design for PID Example 6.20: (b) phase.}$$

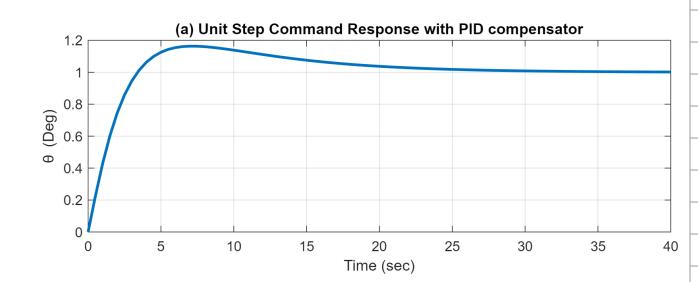


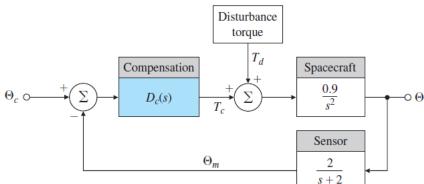
s+2

for Spacecraft Attitude Control

■ Response of the system for a unit step θ_{com} is found from:

$$\mathcal{T}(s) = \frac{\Theta}{\Theta_{com}} = \frac{D_c G}{1 + D_c G H}$$

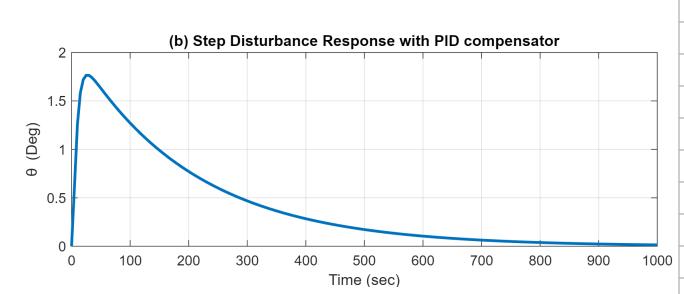


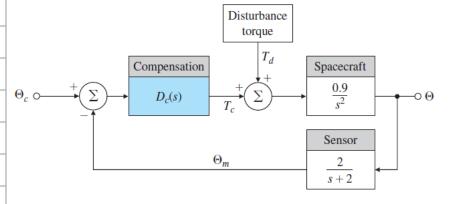


for Spacecraft Attitude Control

Response for a step disturbance torque of T_d is found from:

$$\frac{\Theta}{T_d} = \frac{G}{1 + D_c G H}$$





for Spacecraft Attitude Control

• Frequency Response of T(s) and S(s) are shown:

