Spring 2020

控制系統 Control Systems

Unit 54 Design Using Dynamic Compensation

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- Three categories of Particularly Simple and Effective Designs:
- Lead Compensation:
 - Approximates the function of PD control and
 - Acts mainly to speed up a response

by lowering rise time and decreasing the transient overshoot

Lag Compensation:

- Approximates the function of PI control and
- Is usually used to improve the steady-state accuracy

Notch Compensation:

• To achieve stability for systems with lightly damped flexible modes

Design Using Dynamic Compensation





$$D_c(s) = K$$

$$G(s) = \frac{1}{s(s+1)}$$

$$> 1 + K \frac{1}{s(s+1)} = 0$$

$$\Rightarrow s(s+1) + K = 0$$

$$D_c(s) = K (s+2)$$

$$G(s) = \frac{1}{s(s+1)}$$

$$\Rightarrow 1 + K (s+2) \frac{1}{s(s+1)} =$$

$$\Rightarrow s(s+1) + K(s+2) = 0$$

0







Example 5.11: Design Using Lead Compensation



Example 5.11: Design Using Lead Compensation



2nd-Order Position Control System

$$G(s) = \frac{1}{s(s+1)}$$
$$D_c(s) = \frac{s+z}{s+p}, \quad z > p$$

$$D_c(0) = \frac{z}{p} = 3 \text{ to } 10$$

Lead Compensation:

$$KD_{c1}(s) = 91 \frac{s+2}{s+13}$$

$$K_{v} = \lim_{s \to 0} s K D_{c1}(s) G(s)$$

= $\lim_{s \to 0} s (91) \frac{s+2}{s+13} \frac{1}{s(s+1)}$

$$= 14$$

 $D_{c2}(s) = \frac{s + 0.05}{s + 0.01}$

IF
$$K_v = 70 \, \text{sec}^{-1}$$

Reduce the velocity error

by a factor of 5

$$\Rightarrow \frac{z}{p} = 5$$
$$\Rightarrow z = 0.05$$
$$\Rightarrow p = 0.01$$

• 2nd-Order Position Control System $G(s) = \frac{1}{s(s+1)}$

$$KD_{c1}(s) = 91 \frac{s+2}{s+13}$$

 $KD_{c2}(s) = 91 \frac{s + 0.05}{s + 0.01}$



Design Using Notch Compensation

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Suppose the design with lead and lag compensation

$$KD_c(s) = 91 \frac{s+2}{s+13} \frac{s+0.05}{s+0.01}$$

Has a substantial oscillation at about 50 rad/sec

 $G(s) = \frac{2500}{s(s+1)(s^2+s+2500)}$

Notch Compensation (Phase Stabilization)

$$D_{notch}(s) = \frac{s^2 + 2\zeta w_0 s + w_0^2}{(s + w_0)^2}$$
$$= \frac{s^2 + 0.8s + 3600}{(s + 60)^2}$$

Design Using Notch Compensation

Suppose the design with lead and lag compensation

