

105-2: EE4052
計算機程式設計
Computer Programming

Unit 13: 資料間的相關性

連 豐 力

臺大電機系

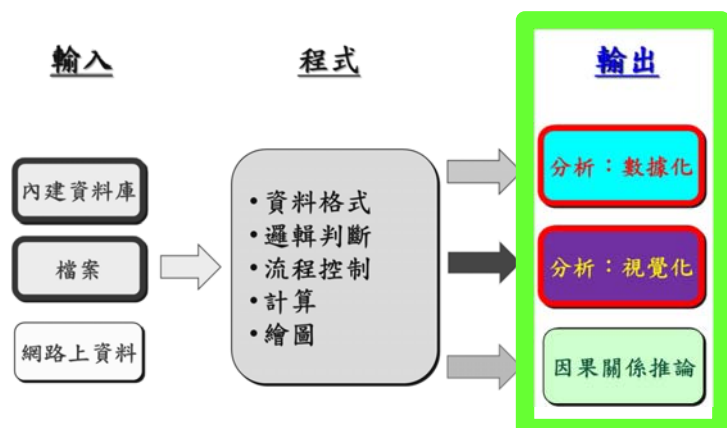
Feb 2017 - Jun 2017

課程主題進度

計算機程式設計 - 2017S
U13: 資料間的相關性
Feng-Li Lian @ NTU-EE

- **U01:** 課程介紹：討論主題，作業，報告，進行方式
- **U02:** 設定軟體 R 與 Rstudio
- **U03:** 數據處理與繪圖指令功能
- **U04:** 資料類別與基本運算
- **U05:** 邏輯判斷與流程控制
- **U06:** 函數：計算與排序
- **U07:** 多維度資料格式
- **U08:** 檔案資料輸入與輸出
- **U09:** 繪圖功能與文字
- **U10:** 多重繪圖與顏色
- **U11:** 函數：動畫與動作

- **U12:** 探索性資料分析
- **U13:** 資料間的相關性
- **U14:** 資料連結分析



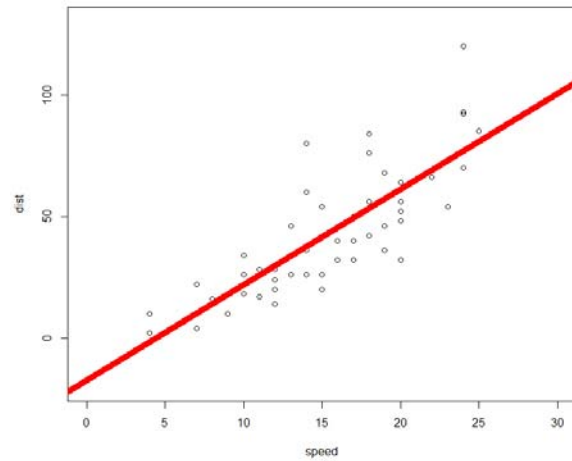
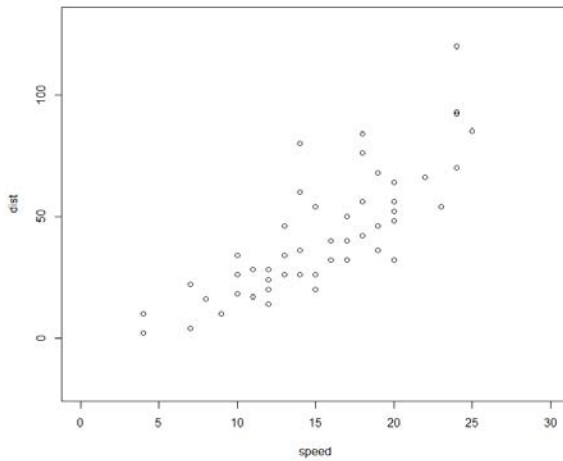
- 資料間的線性關係
- lm: Linear Model
- nhanes2, cars, iris 的線性回歸模型
- 資料間的相關性
- 多維關係繪圖

資料間的線性關係

資料庫：cars

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- cars
- `plot(cars, xlim = c(0, 30), ylim = c(-20, 130))`



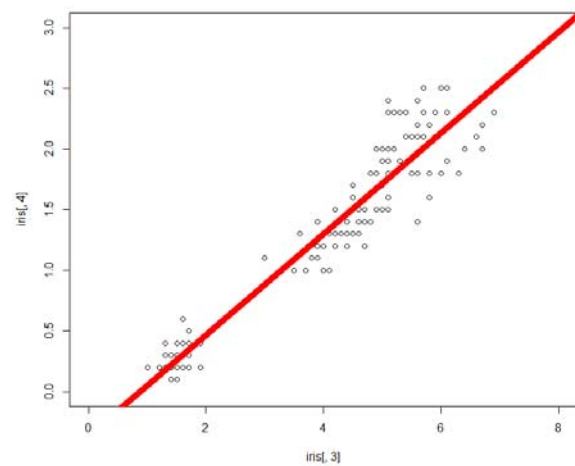
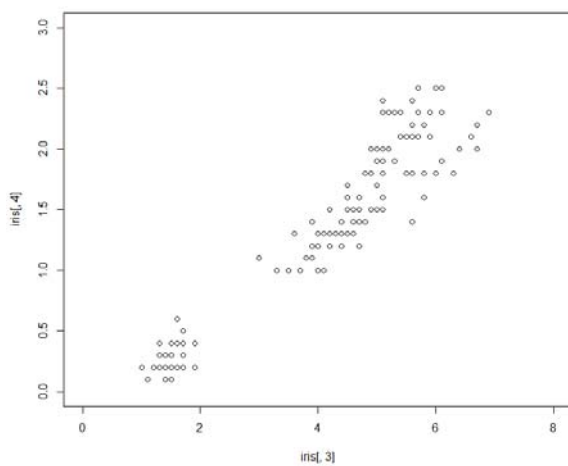
- `abline(a = -17.579, b = 3.932, col = "red", lwd = 8)`

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資料庫：iris

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- iris
- `plot(iris[, 3], iris[, 4], xlim = c(0, 8), ylim = c(0, 3))`



- `abline(a = -0.3631, b = 0.4158, col = "red", lwd = 8)`

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Im: Linear Model

Least Squares Approximation

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Least Squares Approximation

- 參考資料：http://www.ms.uky.edu/~ma138/Spring15/Curve_fitting.pdf

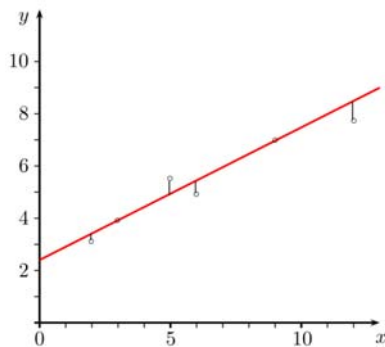


FIGURE 1: Fitting a straight line to data by the method of least squares

$$y = ax + b$$

$$\begin{cases} ax_1 + b = y_1 \\ ax_2 + b = y_2 \\ \vdots \\ ax_n + b = y_n \end{cases} \rightsquigarrow \begin{bmatrix} x_1 & 1 \\ x_2 & 1 \\ \vdots & \vdots \\ x_n & 1 \end{bmatrix} \begin{bmatrix} a \\ b \end{bmatrix} = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{bmatrix}$$

$$\delta_1 = (ax_1 + b) - y_1, \quad \delta_2 = (ax_2 + b) - y_2, \quad \dots, \quad \delta_n = (ax_n + b) - y_n.$$

$\sqrt{\delta_1^2 + \delta_2^2 + \dots + \delta_n^2}$ is as small as possible.

$$\hat{a} = \frac{n \left(\sum_{i=1}^n x_i y_i \right) - \left(\sum_{i=1}^n x_i \right) \left(\sum_{i=1}^n y_i \right)}{n \left(\sum_{i=1}^n x_i^2 \right) - \left(\sum_{i=1}^n x_i \right)^2} \quad \hat{b} = \frac{1}{n} \left(\sum_{i=1}^n y_i - \hat{a} \sum_{i=1}^n x_i \right),$$

$$y = \hat{a}x + \hat{b}$$

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Least Squares Approximation

- 參考資料：http://www.ms.uky.edu/~ma138/Spring15/Curve_fitting.pdf

t (sec)	0.5	1.1	1.5	2.1	2.3
T (°C)	32.0	33.0	34.2	35.1	35.7

$$T = at + b.$$

$$\begin{cases} 0.5a + b = 32.0 \\ 1.1a + b = 33.0 \\ 1.5a + b = 34.2 \\ 2.1a + b = 35.1 \\ 2.3a + b = 35.7 \end{cases} \iff \begin{bmatrix} 0.5 & 1 \\ 1.1 & 1 \\ 1.5 & 1 \\ 2.1 & 1 \\ 2.3 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \end{bmatrix} = \begin{bmatrix} 32.0 \\ 33.0 \\ 34.2 \\ 35.1 \\ 35.7 \end{bmatrix}.$$

$$A^T A = \begin{bmatrix} 0.5 & 1.1 & 1.5 & 2.1 & 2.3 \\ 1 & 1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 0.5 & 1 \\ 1.1 & 1 \\ 1.5 & 1 \\ 2.1 & 1 \\ 2.3 & 1 \end{bmatrix} = \begin{bmatrix} 13.41 & 7.5 \\ 7.5 & 5 \end{bmatrix}$$

$$A^T \mathbf{b} = \begin{bmatrix} 0.5 & 1.1 & 1.5 & 2.1 & 2.3 \\ 1 & 1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 32.0 \\ 33.0 \\ 34.2 \\ 35.1 \\ 35.7 \end{bmatrix} = \begin{bmatrix} 259.42 \\ 170 \end{bmatrix}$$

$$\begin{bmatrix} 13.41 & 7.5 \\ 7.5 & 5 \end{bmatrix} \begin{bmatrix} a \\ b \end{bmatrix} = \begin{bmatrix} 259.42 \\ 170 \end{bmatrix}$$

$$\left[\begin{array}{cc|c} 13.41 & 7.5 & 259.42 \\ 7.5 & 5 & 170 \end{array} \right] \text{ is equivalent to } \left[\begin{array}{cc|c} 1 & 0 & 2.0463 \\ 0 & 1 & 30.93 \end{array} \right]$$

$$\hat{a} = 2.0463 \text{ and } \hat{b} = 30.93.$$

$$T(t) = 2.0463t + 30.93$$

year	1980	1985	1990	1995
population	227	237	249	262

$$P(t) = at + b.$$

$$\begin{bmatrix} 0 & 1 \\ 5 & 1 \\ 10 & 1 \\ 15 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \end{bmatrix} = \begin{bmatrix} 227 \\ 237 \\ 249 \\ 262 \end{bmatrix}$$

$$A^T A = \begin{bmatrix} 0 & 5 & 10 & 15 \\ 1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 0 & 1 \\ 5 & 1 \\ 10 & 1 \\ 15 & 1 \end{bmatrix} = \begin{bmatrix} 350 & 30 \\ 30 & 4 \end{bmatrix}$$

$$A^T \mathbf{b} = \begin{bmatrix} 0 & 5 & 10 & 15 \\ 1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 227 \\ 237 \\ 249 \\ 262 \end{bmatrix} = \begin{bmatrix} 7605 \\ 975 \end{bmatrix}$$

$$\begin{bmatrix} 350 & 30 \\ 30 & 4 \end{bmatrix} \begin{bmatrix} a \\ b \end{bmatrix} = \begin{bmatrix} 7605 \\ 975 \end{bmatrix}$$

$$\left[\begin{array}{cc|c} 350 & 30 & 7605 \\ 30 & 4 & 975 \end{array} \right] \text{ is equivalent to } \left[\begin{array}{cc|c} 1 & 0 & 117/50 \\ 0 & 1 & 1131/5 \end{array} \right]$$

$$P(t) = 117/50 \cdot t + 1131/5.$$

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大綱

三個資料庫

nhanes2, cars, iris

- `install.packages("mice")` # 安裝 mice 軟體套件
- `library(mice)` # 載入 mice 軟體套件
- `data(nhanes2)`
- `nrow(nhanes2)` # nhanes2 資料集的橫列數
- `ncol(nhanes2)` # nhanes2 資料集的直行數
- `summary(nhanes2)` # nhanes2 資料集的概括資訊
- `head(nhanes2)`

```
> head(nhanes2)
  age  bmi  hyp chl
1 20-39 NA <NA> NA
2 40-59 22.7 no 187
3 20-39 NA no 187
4 60-99 NA <NA> NA
5 20-39 20.4 no 113
6 60-99 NA <NA> 184
```

```
> summary(nhanes2)
  age          bmi          hyp          chl
20-39: 12  Min.   :20.40  no   : 13  Min.   :113.0
40-59:  7  1st Qu.:22.65  yes  :  4  1st Qu.:185.0
60-99:  6  Median :26.75  NA's :  8  Median :187.0
      Mean   :26.56          Mean   :191.4
      3rd Qu.:28.93          3rd Qu.:212.0
      Max.   :35.30          Max.   :284.0
      NA's   :  9           NA's   : 10
```

線性回歸模型預測數值

- `data0 <- nhanes2` # 針對第2, 4組數據
- `subNA <- which(is.na(nhanes2[, 4]) == TRUE | is.na(nhanes2[, 2]) == TRUE)`

- `dataOK <- nhanes2[-subNA,]`
- `dataOK`
- `dataNA <- nhanes2[subNA,]`
- `dataNA`

```
> lm_chl_bmi
Call:
lm(formula = chl ~ bmi, data = dataOK)

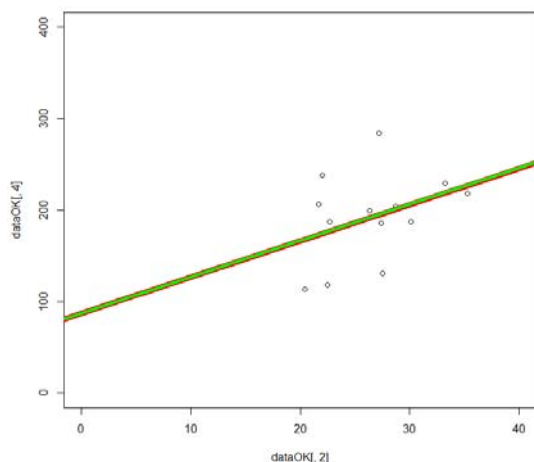
Coefficients:
(Intercept)          bmi
      87.130         3.963
```

$$chl = 3.963 * bmi + 87.130$$

- `lm_chl_bmi <- lm(chl ~ bmi, data = dataOK)`
 - # 利用 dataOK 中 bmi 為引數，chl 為因變數，建構線性回歸模型

畫 $y = b x + a$ 的直線

- `abline()` # 畫 $y = b x + a$ 的直線
- `plot(dataOK[, 2], dataOK[, 4], xlim = c(0, 40), ylim = c(0, 400))`
- `abline(a = 87.130, b = 3.963, col = "red", lwd = 8)`
- `abline(lm_chl_bmi, col = "green", lwd = 4)`



$$\text{chl} = 3.963 * \text{bmi} + 87.130$$

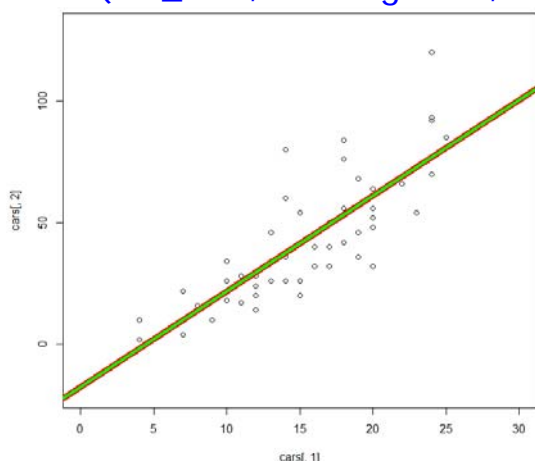
```
> lm_chl_bmi
Call:
lm(formula = chl ~ bmi, data = dataOK)

Coefficients:
(Intercept)      bmi
    87.130         3.963
```

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另一個資料：cars

- `cars`
- `plot(cars[, 1], cars[, 2], xlim = c(0, 30), ylim = c(-20, 130))`
- `lm_cars <- lm(dist ~ speed, data = cars)`
- `lm_cars`
- `abline(a = -17.579, b = 3.932, col = "red", lwd = 8)`
- `abline(lm_cars, col = "green", lwd = 4)`



$$\text{chl} = 3.932 * \text{speed} - 17.579$$

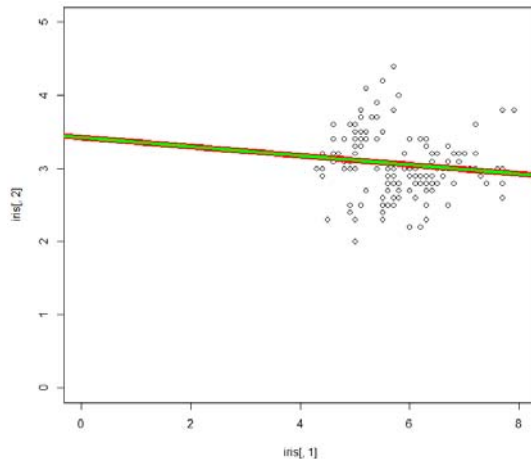
```
> lm_cars
Call:
lm(formula = dist ~ speed, data = cars)

Coefficients:
(Intercept)      speed
   -17.579         3.932
```

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另一個資料：iris

- iris
- `plot(iris[, 1], iris[, 2], xlim = c(0, 8), ylim = c(0, 5))`
- `lm_iris_1 <- lm(Sepal.Width ~ Sepal.Length, data = iris)`
- `lm_iris_1`
- `abline(a = 3.41895, b = -0.06188, col = "red", lwd = 8)`
- `abline(lm_iris_1, col = "green", lwd = 4)`



$$\text{Sepal.Width} = -0.06188 * \text{Sepal.Length} + 3.41895$$

```
> lm_iris_1
```

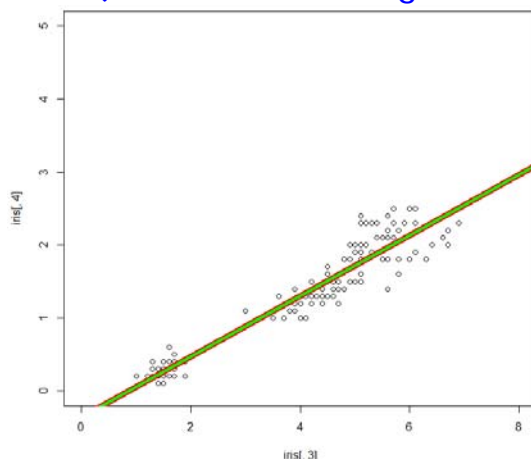
```
Call:  
lm(formula = Sepal.Width ~ Sepal.Length,  
data = iris)
```

```
Coefficients:  
(Intercept) Sepal.Length  
3.41895      -0.06188
```

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另一個資料：iris

- iris
- `plot(iris[, 3], iris[, 4], xlim = c(0, 8), ylim = c(0, 5))`
- `lm_iris_2 <- lm(Petal.Width ~ Petal.Length, data = iris)`
- `lm_iris_2`
- `abline(a = -0.3631, b = 0.4158, col = "red", lwd = 8)`
- `abline(lm_iris_2, col = "green", lwd = 4)`



$$\text{Petal.Width} = 0.4158 * \text{Petal.Length} - 0.3631$$

```
> lm_iris_2
```

```
Call:  
lm(formula = Petal.Width ~ Petal.Length,  
data = iris)
```

```
Coefficients:  
(Intercept) Petal.Length  
-0.3631      0.4158
```

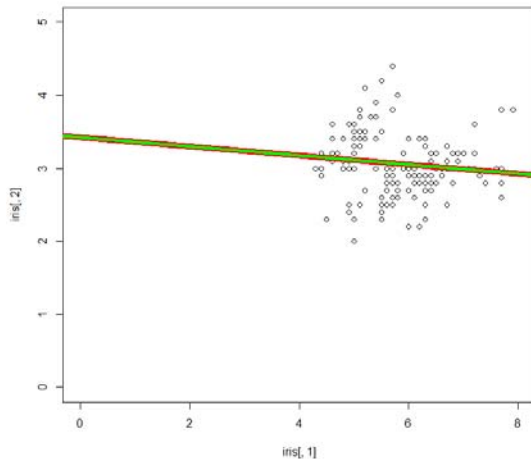
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另一個資料：iris

■ iris

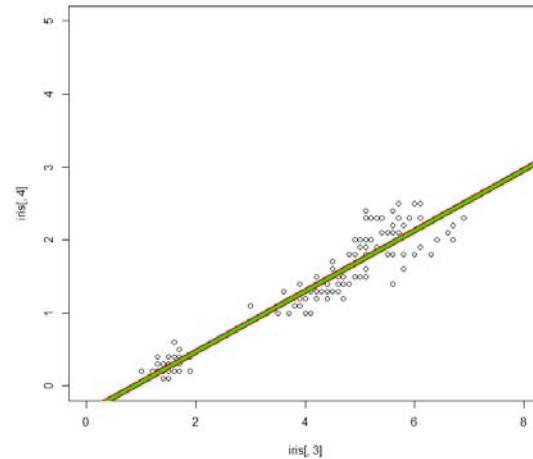
```
> lm_iris_1  
Call:  
lm(formula = Sepal.Width ~ Sepal.Length,  
data = iris)  
Coefficients:  
(Intercept) Sepal.Length  
3.41895 -0.06188
```

$\text{Sepal.Width} = -0.06188 * \text{Sepal.Length} + 3.41895$



```
> lm_iris_2  
Call:  
lm(formula = Petal.Width ~ Petal.Length,  
data = iris)  
Coefficients:  
(Intercept) Petal.Length  
-0.3631 0.4158
```

$\text{Petal.Width} = 0.4158 * \text{Petal.Length} - 0.3631$

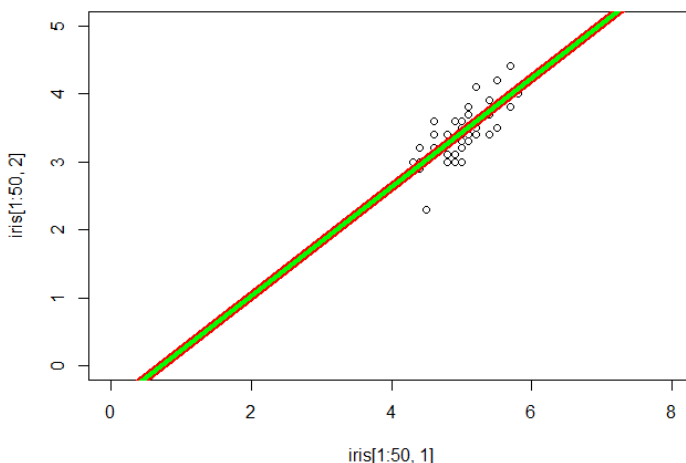


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另一個資料：iris, 依照種類

■ iris

- `plot(iris[1:50, 1], iris[1:50, 2], xlim = c(0, 8), ylim = c(0, 5))`
- `lm_iris_11 <- lm(Sepal.Width ~ Sepal.Length, data = iris[1:50,])`
- `abline(a = -0.5694, b = 0.7985, col = "red", lwd = 8)`
- `abline(lm_iris_11, col = "green", lwd = 4)`



$\text{Sepal.Width} = 0.7985 * \text{Sepal.Length} - 0.5694$

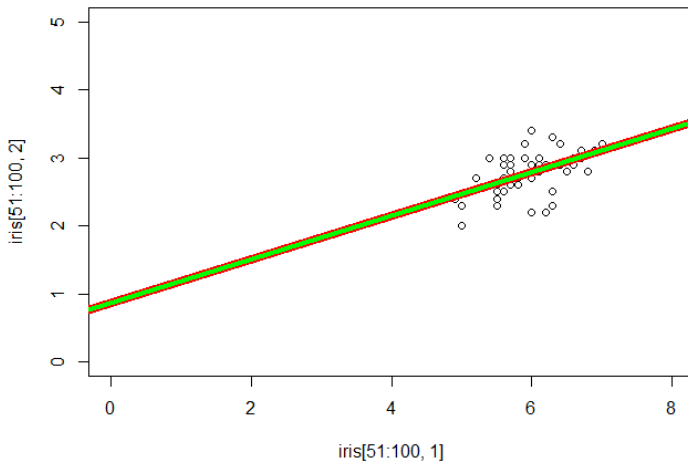
```
> lm_iris_11  
Call:  
lm(formula = Sepal.Width ~ Sepal.Length,  
data = iris[1:50, ])  
Coefficients:  
(Intercept) Sepal.Length  
-0.5694 0.7985
```

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另一個資料：iris, 依照種類

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- iris
- `plot(iris[51:100, 1], iris[51:100, 2], xlim = c(0, 8), ylim = c(0, 5))`
- `lm_iris_12 <- lm(Sepal.Width ~ Sepal.Length, data = iris[51:100,])`
- `abline(a = 0.8721, b = 0.3197, col = "red", lwd = 8)`
- `abline(lm_iris_12, col = "green", lwd = 4)`



$$\text{Sepal.Width} = 0.3197 * \text{Sepal.Length} + 0.8721$$

```
> lm_iris_12
```

```
Call:  
lm(formula = Sepal.Width ~ Sepal.Length,  
    data = iris[51:100, ])
```

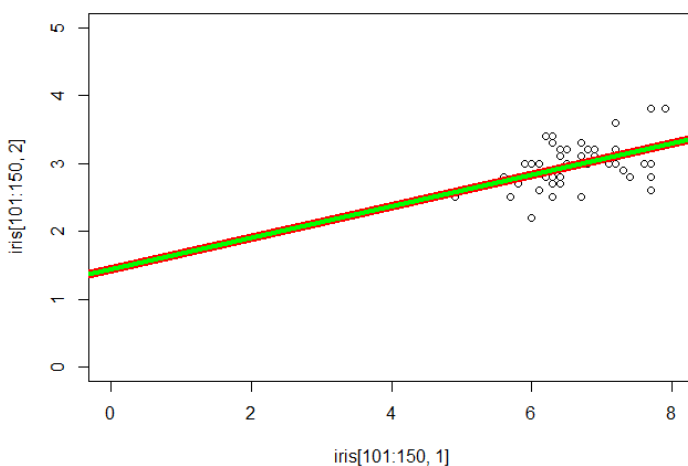
```
Coefficients:  
(Intercept) Sepal.Length  
0.8721      0.3197
```

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另一個資料：iris, 依照種類

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- iris
- `plot(iris[101:150, 1], iris[101:150, 2], xlim = c(0,8), ylim = c(0,5))`
- `lm_iris_13 <- lm(Sepal.Width ~ Sepal.Length, data = iris[101:150,])`
- `abline(a = 1.4463, b = 0.2319, col = "red", lwd = 8)`
- `abline(lm_iris_13, col = "green", lwd = 4)`



$$\text{Sepal.Width} = 0.3197 * \text{Sepal.Length} + 1.4463$$

```
> lm_iris_13
```

```
Call:  
lm(formula = Sepal.Width ~ Sepal.Length,  
    data = iris[101:150, ])
```

```
Coefficients:  
(Intercept) Sepal.Length  
1.4463      0.2319
```

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另一個資料：iris, 依照種類

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- `lm_iris_11 <- lm(Sepal.Width ~ Sepal.Length, data = iris[1:50,])`
- `lm_iris_12 <- lm(Sepal.Width ~ Sepal.Length, data = iris[51:100,])`
- `lm_iris_13 <- lm(Sepal.Width ~ Sepal.Length, data = iris[101:150,])`
- `lm_iris_21 <- lm(Petal.Width ~ Petal.Length, data = iris[1:50,])`
- `lm_iris_22 <- lm(Petal.Width ~ Petal.Length, data = iris[51:100,])`
- `lm_iris_23 <- lm(Petal.Width ~ Petal.Length, data = iris[101:150,])`

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另一個資料：iris, 依照種類

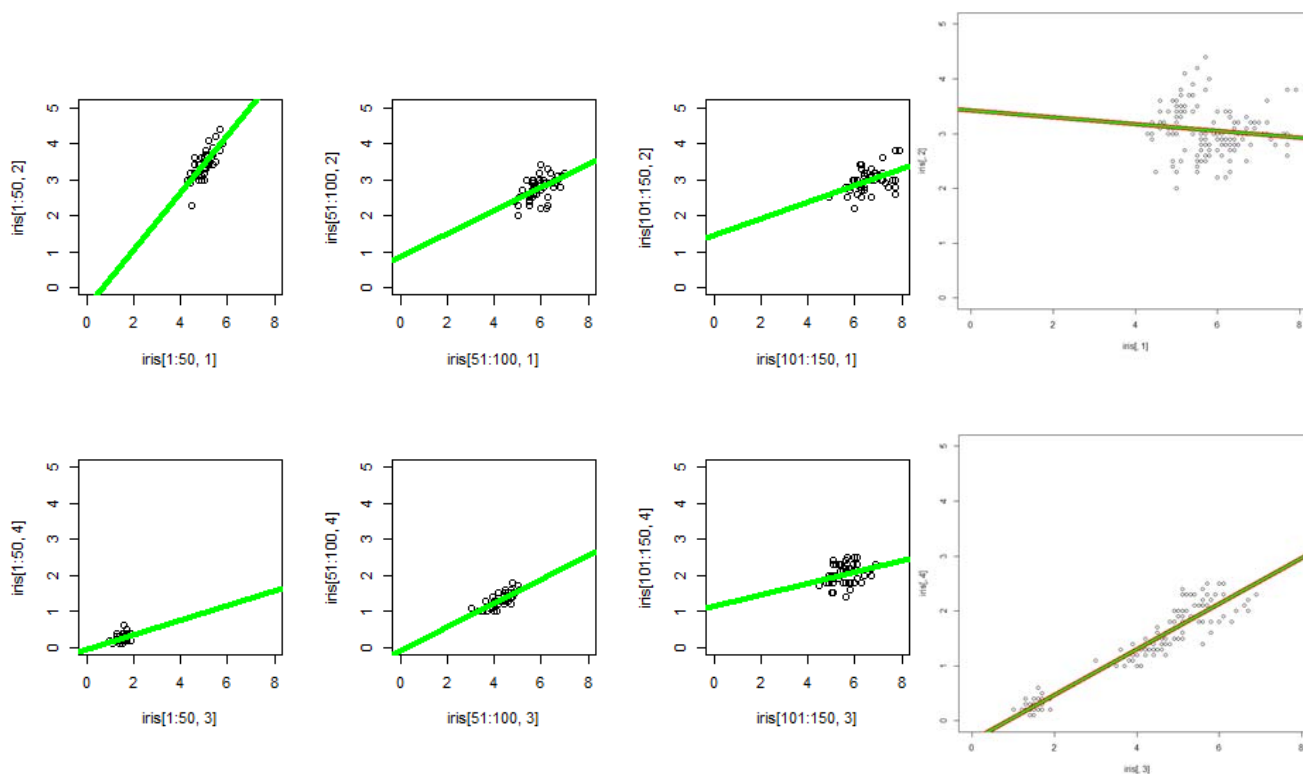
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- `layout(matrix(1:6, nrow = 2, byrow = T))`
- `plot(iris[1:50, 1], iris[1:50, 2], xlim = c(0, 8), ylim = c(0, 5))`
- `abline(lm_iris_11, col = "green", lwd = 4)`
- `plot(iris[51:100, 1], iris[51:100, 2], xlim = c(0, 8), ylim = c(0, 5))`
- `abline(lm_iris_12, col = "green", lwd = 4)`
- `plot(iris[101:150, 1], iris[101:150, 2], xlim = c(0,8), ylim = c(0,5))`
- `abline(lm_iris_13, col = "green", lwd = 4)`
- `plot(iris[1:50, 3], iris[1:50, 4], xlim = c(0, 8), ylim = c(0, 5))`
- `abline(lm_iris_21, col = "green", lwd = 4)`
- `plot(iris[51:100, 3], iris[51:100, 4], xlim = c(0, 8), ylim = c(0, 5))`
- `abline(lm_iris_22, col = "green", lwd = 4)`
- `plot(iris[101:150, 3], iris[101:150, 4], xlim = c(0,8), ylim = c(0,5))`
- `abline(lm_iris_23, col = "green", lwd = 4)`

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另一個資料：iris, 依照種類

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資料間的相關性

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相關性

cor(), correlation 相關係數

cor(x, y)

cor_matrix <- cor(data_all, use = "pairwise")

cor_iris <- cor(iris[, 1:4], use = "pairwise")

cor_iris

```
> cor_iris
```

	Sepal.Length	Sepal.Width	Petal.Length	Petal.Width
Sepal.Length	1.0000000	-0.1175698	0.8717538	0.8179411
Sepal.Width	-0.1175698	1.0000000	-0.4284401	-0.3661259
Petal.Length	0.8717538	-0.4284401	1.0000000	0.9628654
Petal.Width	0.8179411	-0.3661259	0.9628654	1.0000000

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相關性

plotcorr(), 繪製相關圖

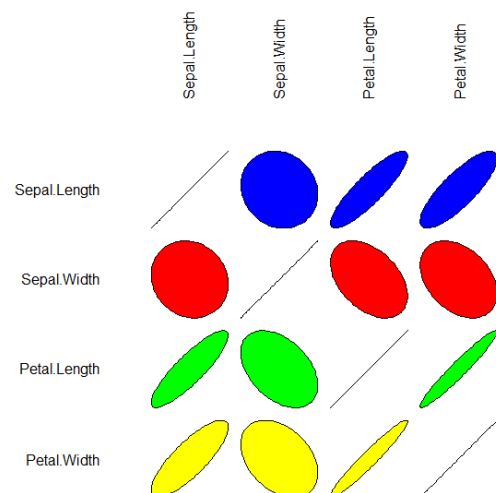
install.packages("ellipse")

library(ellipse)

plotcorr(cor_iris, col = c("blue", "red", "green", "yellow"))

```
> cor_iris
```

	Sepal.Length	Sepal.Width	Petal.Length	Petal.Width
Sepal.Length	1.0000000	-0.1175698	0.8717538	0.8179411
Sepal.Width	-0.1175698	1.0000000	-0.4284401	-0.3661259
Petal.Length	0.8717538	-0.4284401	1.0000000	0.9628654
Petal.Width	0.8179411	-0.3661259	0.9628654	1.0000000



相關性

```
# use weather dataset
```

```
install.packages( "rattle" )
```

```
library( rattle )
```

```
data( weather )
```

```
head( weather[ , 12:21] ) # 12 to 21 variable names, values
```

```
> head( weather[ , 12:21] )
```

	WindSpeed9am	WindSpeed3pm	Humi di ty9am	Humi di ty3pm	Pressure9am	Pressure3pm	Cl oud9am	Cl oud3pm	Temp9am	Temp3pm
1	6	20	68	29	1019.7	1015.0	7	7	14.4	23.6
2	4	17	80	36	1012.4	1008.4	5	3	17.5	25.7
3	6	6	82	69	1009.5	1007.2	8	7	15.4	20.2
4	30	24	62	56	1005.5	1007.0	2	7	13.5	14.1
5	20	28	68	49	1018.3	1018.5	7	7	11.1	15.4
6	20	24	70	57	1023.8	1021.7	7	5	10.9	14.8

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相關性

```
# correlation matrix 相關係數矩陣
```

```
var <- c( 12:21 )
```

```
cor_matrix <- cor( weather[ var ], use = "pairwise" )
```

```
> cor_matrix
```

	WindSpeed9am	WindSpeed3pm	Humi di ty9am	Humi di ty3pm	Pressure9am	Pressure3pm	Cl oud9am	Cl oud3pm	Temp9am	Temp3pm
WindSpeed9am	1.0000000	0.47296617	-0.2706229	0.14665712	-0.35633183	-0.24795238	0.10184246	-0.02247149	0.06407405	-0.2351864
WindSpeed3pm	0.47296617	1.0000000	-0.2660925	-0.02636775	-0.35980011	-0.33732535	-0.02642642	0.00720724	-0.01776636	-0.1875697
Humi di ty9am	-0.27062286	-0.26609247	1.0000000	0.54671844	0.13572697	0.13442050	0.39284158	0.27193809	-0.43655057	-0.3551186
Humi di ty3pm	0.14665712	-0.02636775	0.5467184	1.0000000	-0.08794614	-0.01005189	0.55163264	0.51010790	-0.25568147	-0.5816761
Pressure9am	-0.35633183	-0.35980011	0.1357270	-0.08794614	1.0000000	0.96789496	-0.15755279	-0.14100043	-0.46041819	-0.2536738
Pressure3pm	-0.24795238	-0.33732535	0.1344205	-0.01005189	0.96789496	1.0000000	-0.12894408	-0.14383718	-0.49263629	-0.3454853
Cl oud9am	0.10184246	-0.02642642	0.3928416	0.55163264	-0.15755279	-0.12894408	1.0000000	0.52521793	0.02104135	-0.2023440
Cl oud3pm	-0.02247149	0.00720724	0.2719381	0.51010790	-0.14100043	-0.14383718	0.52521793	1.0000000	0.04094519	-0.1728142
Temp9am	0.06407405	-0.01776636	-0.4365506	-0.25568147	-0.46041819	-0.49263629	0.02104135	0.04094519	1.0000000	0.8444058
Temp3pm	-0.23518635	-0.18756965	-0.3551186	-0.58167615	-0.25367375	-0.34548531	-0.20234405	-0.17281423	0.84440581	1.0000000

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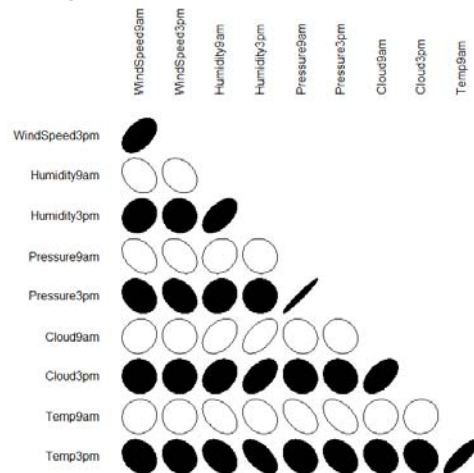
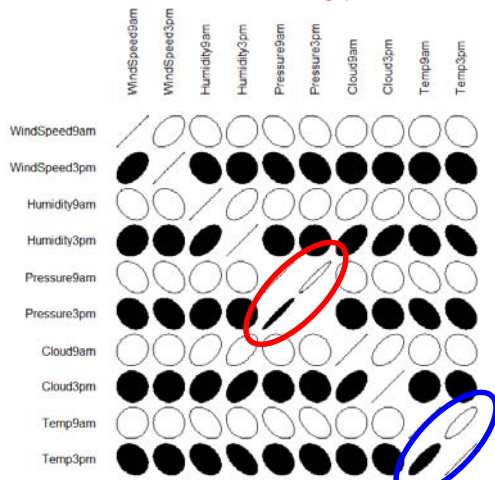
```
# plotcoor(), 繪製相關圖
```

```
install.packages("ellipse")
```

```
library(ellipse)
```

```
plotcorr(corr_matrix, col = rep(c("white", "black"))) )
```

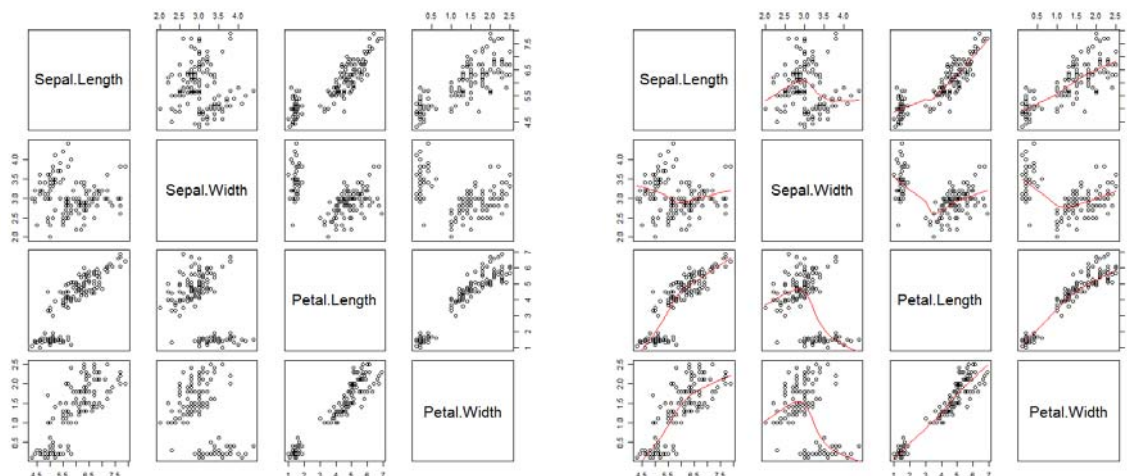
```
plotcorr(corr_matrix, type = "lower", col = rep(c("white", "black"))) )
```



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多維關係繪圖

- iris
- x <- iris[, 1:4]
- plot(x)
- pairs(x)
- pairs(x, panel = panel.smooth)



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多維繪圖 - 散點 直方 核密度

- iris
 - x <- iris[, 1:4]
- scatterplot
- ```

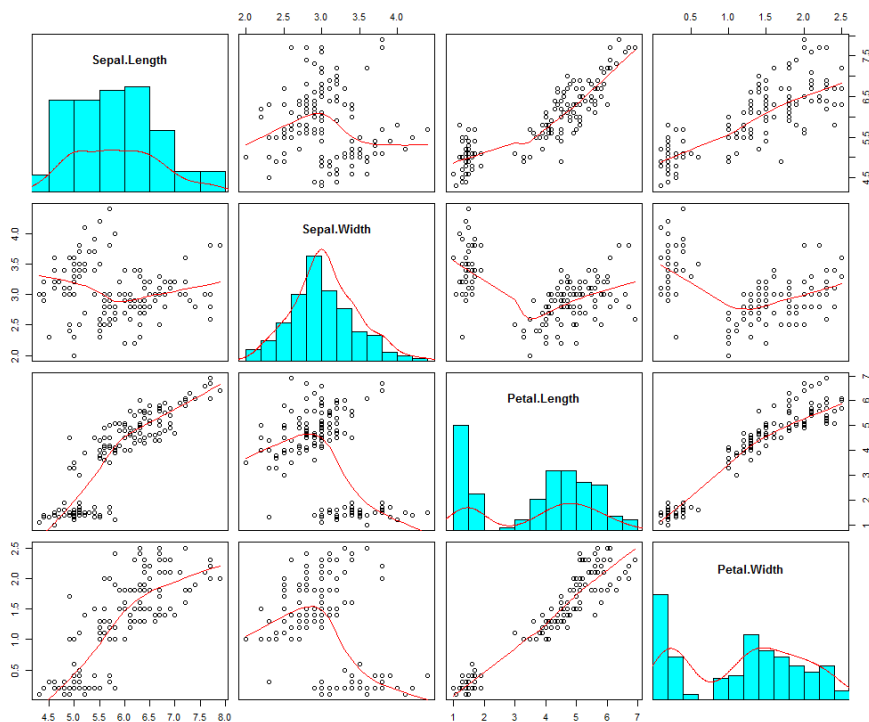
■ panel.hist <- function(x, ...) {
■ usr <- par("usr"); on.exit(par(usr))
■ par(usr = c(usr[1:2], 0, 1.5))
■ h <- hist(x, plot = FALSE)
■ breaks <- h$breaks; nB <- length(breaks)
■ y <- h$counts; y <- y / max(y)
■ rect(breaks[-nB], 0, breaks[-1], y, col = "cyan", ...)
■ lines(density(x, na.rm = TRUE), col = "red")
■ }

```
- pairs( x, panel = panel.smooth, pch = 1, bg = "lightcyan",
  - diag.panel = panel.hist, font.labels = 2, cex.labels = 1.2 )

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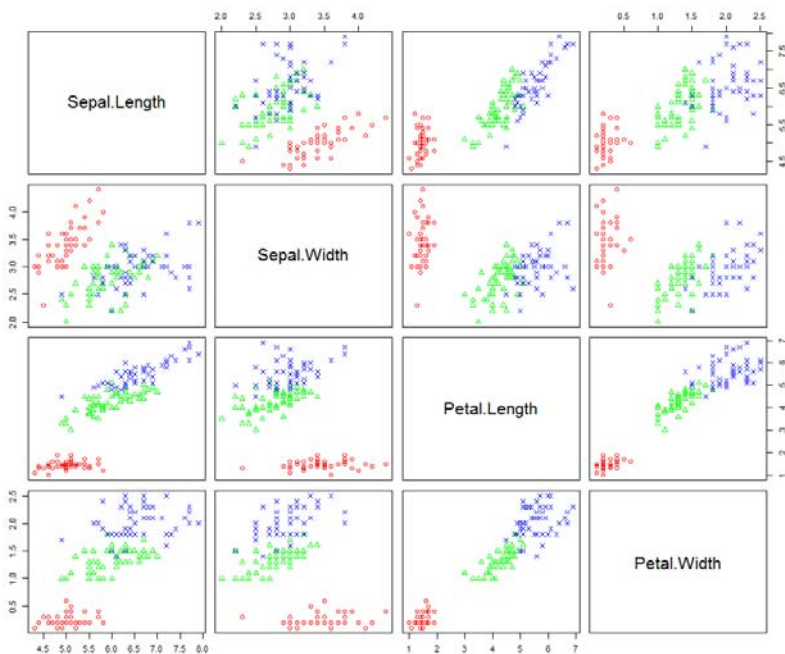


## scatterplot

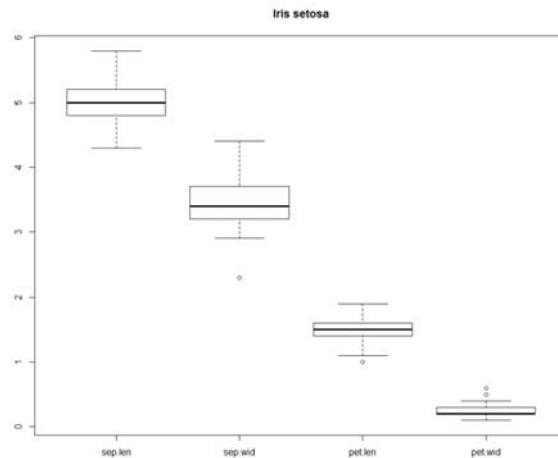


- iris
- `pairs(iris[, 1:4], pch = c(1, 2, 4)[iris$Species], col = c("red", "green", "blue")[iris$Species])`

## scatterplot 不同品種之 散點圖

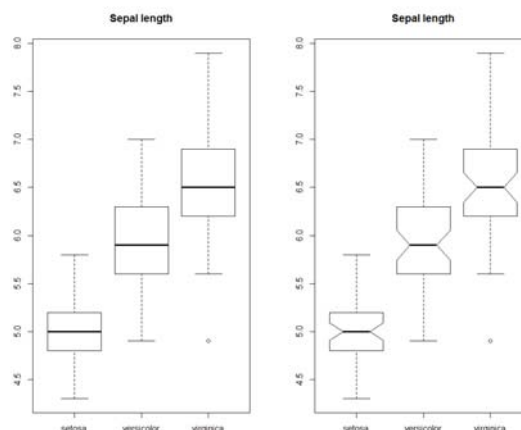


- 第一品種之中，  
花萼長度, 花萼寬度, 花瓣長度, 花瓣寬度，分布情形
- `setosa <- iris[ iris$Species == "setosa", 1:4 ]`
- `boxplot( setosa, names = c( "sep.len", "sep.wid", "pet.len", "pet.wid" ),  
main = "Iris setosa" )`



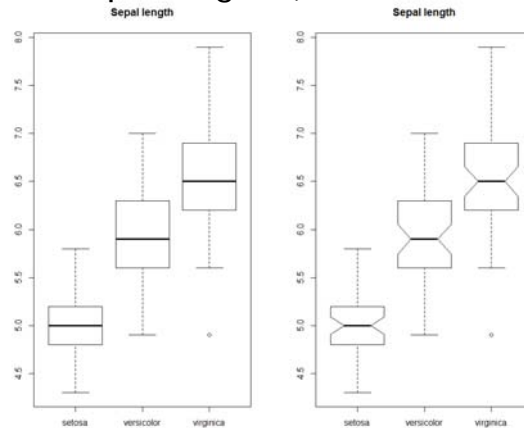
- 35

- 三個品種，  
花萼長度, 花萼寬度, 花瓣長度, 花瓣寬度，分布情形
- `par( mfrow = c(1, 2) )`
- `with( iris, boxplot( Sepal.Length ~ Species, main = "Sepal length" ) )`
- `with( iris, boxplot( Sepal.Length ~ Species, notch = TRUE, main =  
"Sepal length" ) )`



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- 三個品種，  
花萼長度, 花萼寬度, 花瓣長度, 花瓣寬度，分布情形
- 依照不同種類，先分成三群
- `par(mfrow = c(1, 2) )`
- `sx <- with( iris, split( Sepal.Length, Species ) )`
- `boxplot( sx, main = "Sepal length" )`
- `boxplot( sx, notch = TRUE, main = "Sepal length" )`



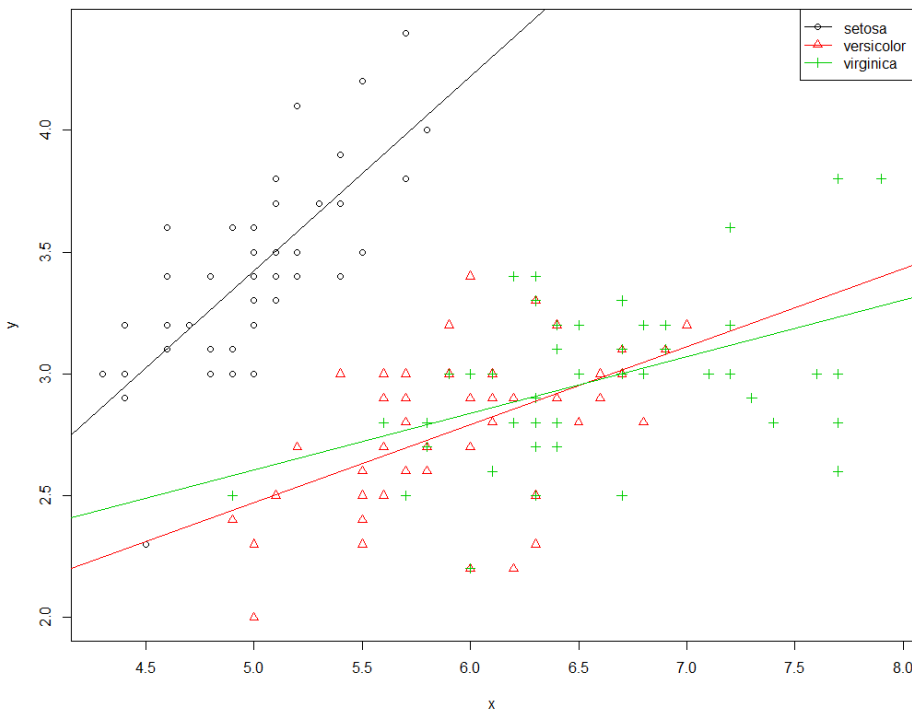
- 37

- 花萼長度與花萼寬度之間的關係
- 依照不同種類，先分成三群
- `sx <- with( iris, split( Sepal.Length, Species ) )`
- `sy <- with( iris, split( Sepal.Width, Species ) )`
- `par( mfrow = c(1, 1) )`
- `plot( 0, xlim = range(sx), ylim = range(sy), type = "n", xlab = "x", ylab = "y" )`
- `points( sx[[1]], sy[[1]], pch = 1, col = 1 )`
- `points( sx[[2]], sy[[2]], pch = 2, col = 2 )`
- `points( sx[[3]], sy[[3]], pch = 3, col = 3 )`
- `for (i in 1:3) abline( lm(sy[[i]] ~ sx[[i]]), col = i )`
- `legend( "topright", legend = c("setosa", "versicolor", "virginica"), lty = 1, pch = 1:3, col = 1:3 )`

不同品種之  
散點圖

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## 不同品種之散點圖

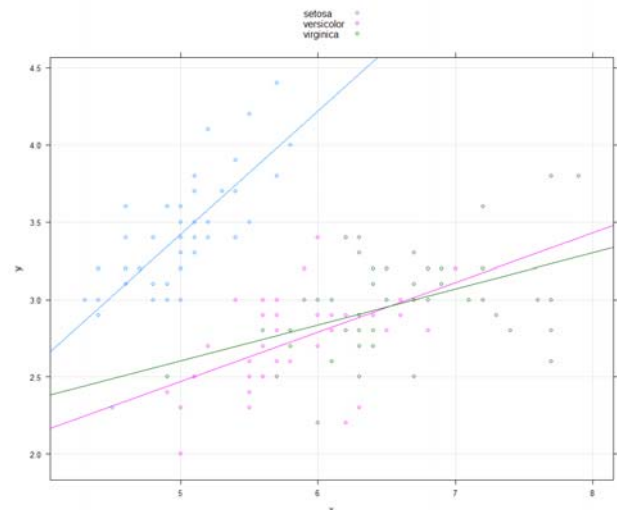


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## 不同品種之散點圖

- 花萼長度與花萼寬度之間的關係
- 依照不同種類，先分成三群

- `x <- iris[[1]]`
- `y <- iris[[2]]`
  
- `species <- iris[[5]]`
  
- `library(lattice)`



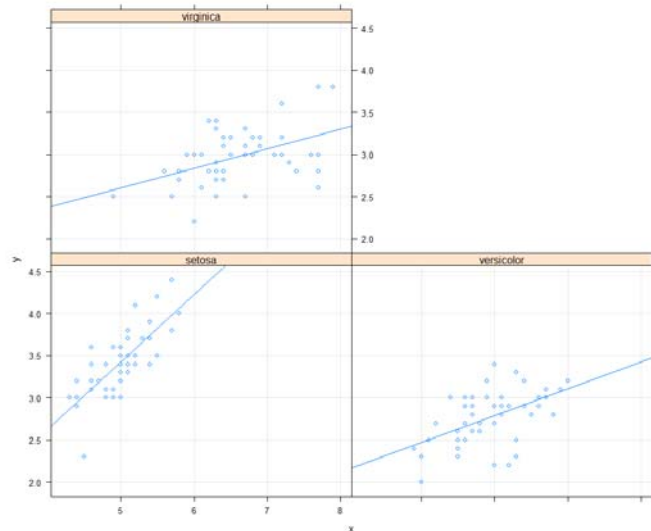
- `xyplot(y ~ x, groups = species, type = c("g", "p", "r"), auto.key = TRUE)`

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- 花萼長度與花萼寬度之間的關係
- 依照不同種類，先分成三群

## 不同品種分開 之散點圖

- `x <- iris[[1]]`
- `y <- iris[[2]]`
  
- `species <- iris[[5]]`
  
- `library(lattice)`



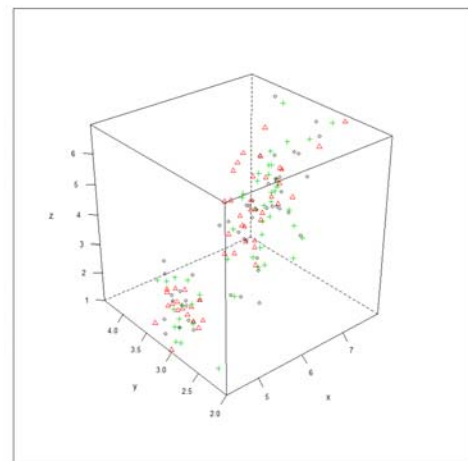
- `xyplot(y ~ x | species, type = c("g", "p", "r"), auto.key = TRUE)`

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# 多維繪圖 - 三維散點圖

- (花萼長度, 花萼寬度, 花瓣長度)

- `data(iris)`
- `x <- iris[, 1]`
- `y <- iris[, 2]`
- `z <- iris[, 3]`
  
- `library(lattice)`



- `cloud(z ~ x * y, groups = iris$Species, pch = 1:3, col = 1:3,`
- `scales = list(arrows = FALSE),`
- `light.source = c(10, 0, 10) )`

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