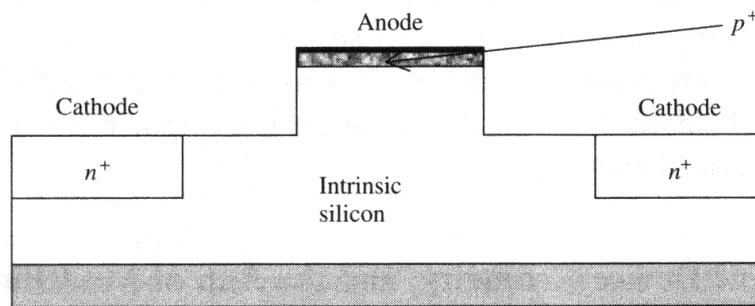


## Silicon Photonics Homework #6

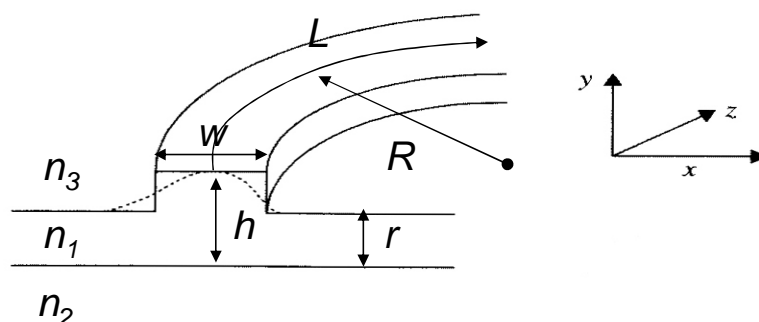
HW 6-1. Consider a silicon optical phase modulator/VOA shown in the following figure. Assume that when the current is injected through the anode and cathode, the carrier concentration  $\Delta N$  ( $=\Delta N_e = \Delta N_h$ ) is uniformly distributed in the intrinsic rib region. Assume the effective index of the waveguide mode is approximately the same as the refractive index in the rib region. Device length  $L = 2$  mm. Operating wavelength  $\lambda_0 = 1.55 \mu\text{m}$ . Please calculate

- (a) The required  $\Delta N$  for  $\pi$ -phase shift. (i.e.,  $|\Delta n L| = \lambda_0/2$ )
- (b) The required  $\Delta N$  for 30 dB attenuation. (i.e.,  $e^{-\Delta \alpha L} = 0.001$ )



HW 6-2. Consider a rib waveguide shown in the following figure with  $n_1 = 3.5$ ,  $n_2 = 1.5$ ,  $n_3 = 1.0$ ,  $w = 2.5 \mu\text{m}$ ,  $h = 3 \mu\text{m}$ ,  $r = 1.7 \mu\text{m}$ ,  $R = 1\text{mm}$  and  $\lambda_0 = 1.55 \mu\text{m}$ . Please calculate (by using the effective index method where  $\beta = 2\pi N_{\text{wg}}/\lambda_0$ ,  $k_{\text{yg}} = (n_{\text{effg}}^2 - N_{\text{wg}}^2)^{0.5} \cdot 2\pi / \lambda_0$ , and  $k_{\text{xs}} = (N_{\text{wg}}^2 - n_{\text{effp}}^2)^{0.5} \cdot 2\pi / \lambda_0$ ),

- (a) the bending loss coefficient  $\alpha_{\text{bend}}$
- (b) the total bending loss for a  $90^\circ$  bend (i.e., the total bending loss  $= e^{-\alpha L}$  when the length of the arc  $L = \pi R/2$ )



HW 6-3. If two identical rib waveguides as described in HW-6.2 are placed closely parallel to each other with a separation  $s = 1 \mu\text{m}$ , please calculate (by using the effective index method as in HW 6-2, where  $k_{xc} = k_{xg}$ )

(a) the coupling coefficient  $\kappa$

(b) the coupling length  $L_{\pi}$

