## Silicon Photonics Homework #3

HW 3-1.

For the Corning SMF-28<sup>TM</sup> step-index single-mode optical fiber with a relative refractive index difference  $\Delta = 0.0036$ , a core diameter  $2a = 8.2 \ \mu$  m, and a core index  $n_1 = 1.468$ , please find

(a) the normalized frequency V at  $\lambda_0 = 1.55 \ \mu \text{ m}$ 

- (b) the normalized propagation constant *b* (using the fitting curve in *b*-*V* diagram) at  $\lambda_0$ = 1.55  $\mu$  m
- (c) the effective index  $N (= \beta / k_0)$  at  $\lambda_0 = 1.55 \ \mu \text{ m}$
- (d) the mode field diameter  $2w_0$  at  $\lambda_0 = 1.55 \ \mu \,\mathrm{m}$
- (e) if the group velocity dispersion (GVD)  $D = 17 \text{ ps/nm} \cdot \text{km}$  at  $\lambda_0 = 1.55$
- $\mu$  m and a laser with a spectral width  $\Delta \lambda = 0.1$  nm is used as the signal source, what is the maximum bit rate  $B_T$  due to chromatic dispersion?
- (f) what is the numerical aperture NA of the optical fiber?
- (g) for single mode operation, what is the cut-off wavelength  $\lambda_{c}$ ?

## HW 3-2.

For the Corning SMF-28<sup>TM</sup> step-index single-mode optical fiber with a relative refractive index difference  $\Delta = 0.0036$ , a core diameter  $2a = 8.2 \ \mu$  m, and a core index  $n_1 = 1.458$ , please find

(a) the normalized frequency V at  $\lambda_0 = 1.31 \ \mu \text{ m}$ 

- (b) the normalized propagation constant b (using the fitting curve in b-V diagram) at  $~\lambda_{~0}\text{=}~1.31~~\mu$  m
- (c) the effective index  $N (= \beta / k_0)$  at  $\lambda_0 = 1.31 \ \mu \text{ m}$
- (d) the mode field diameter  $2w_0$  at  $\lambda_0 = 1.31 \ \mu \text{ m}$
- (e) if the group velocity dispersion (GVD) D = 0.01 ps/nm·km at  $\lambda_0 = 1.31 \ \mu$  m and a laser with a spectral width  $\Delta \lambda = 0.1$  nm is used as the signal source, what is the maximum bit rate  $B_T$  due to chromatic dispersion?

## HW 3-3.

For a step-index multimode fiber with a core diameter  $2a = 100 \ \mu$  m, a core index  $n_1 = 1.48$  and a cladding index  $n_2 = 1.46$ , please find (a) the normalized frequency *V* at  $\lambda_0 = 0.85 \ \mu$  m (b) the number of modes  $M (\approx V^2/2)$ 

(c) the maximum bit rate  $B_T$  due to intermodal (multimode) dispersion.