



#### **Definition of Algorithm**

An algorithm is an **ordered** set of **unambiguous**, **executable** steps that defines a **terminating** process.





#### Chapter 5: Algorithms

- 5.1 The Concept of an Algorithm
- 5.2 Algorithm Representation
- 5.3 Algorithm Discovery
- 5.4 Iterative Structures
- 5.5 Recursive Structures
- 5.6 Efficiency and Correctness



#### Algorithm Representation

- Requires well-defined primitives
- A collection of primitives constitutes a programming language.





# **Figure 5.2** Folding a bird from a square piece of paper

]-J-A-D-20 , N° A-Q-Q-5



#### **Pseudocode Primitives**

• Assignment

 $name \leftarrow expression$ 

Conditional selection

if condition then action



#### Figure 5.3 Origami primitives

Syntax	Semantics	
-0-	Turn paper over as in	
Shade one side of paper	Distinguishes between different sides of paper as in	
$\backslash$	Represents a valley fold so that T represents	
$\backslash$	Represents a mountain fold so that represents	
	Fold over so that D produces	
•	Push in so that produces	6



#### Pseudocode Primitives (continued)

• Repeated execution

while condition do activity

• Procedure

procedure name (generic names)





# **Figure 5.4** The procedure Greetings in pseudocode

### procedure Greetings

Count  $\leftarrow$  3; while (Count > 0) do (print the message "Hello" and Count  $\leftarrow$  Count -1)





#### Polya's Problem Solving Steps

- 1. Understand the problem.
- 2. Devise a plan for solving the problem.
- 3. Carry out the plan.
- 4. Evaluate the solution for accuracy and its potential as a tool for solving other problems.



#### Getting a Foot in the Door

- Try working the problem backwards
- Solve an easier related problem
  - Relax some of the problem constraints
  - Solve pieces of the problem first (bottom up methodology)
- Stepwise refinement: Divide the problem into smaller problems (top-down methodology)





#### Ages of Children Problem

- Person A is charged with the task of determining the ages of B's three children.
  - B tells A that the product of the children's ages is 36.
  - A replies that another clue is required.
  - B tells A the sum of the children's ages.
  - A replies that another clue is needed.
  - $-\,$  B tells A that the oldest child plays the piano.
  - $-\,$  A tells B the ages of the three children.
- How old are the three children?





<b>a</b> . Triples	whose product is 36	<b>b.</b> Sums of triples f	rom part
(1,1,36)	(1,6,6)	1 + 1 + 36 = 38	1+6
(1,2,18)	(2,2,9)	1 + 2 + 18 = 21	2 + 2
(1,3,12)	(2,3,6)	1 + 3 + 12 = 16	2 + 3
(1,4,9)	(3,3,4)	1 + 4 + 9 = 14	3 + 3





#### **Iterative Structures**

• Pretest loop:

```
while (condition) do
  (loop body)
```

#### • Posttest loop:

```
repeat (loop body)
until(condition)
```



# **Figure 5.6** The sequential search algorithm in pseudocode



# Figure 5.7 Components of repetitive control

Initialize:	Establish an initial state that will be modified toward the termination condition
Test:	Compare the current state to the termination condition and terminate the repetition if equal
Modify:	Change the state in such a way that it moves toward the termination condition





# Figure 5.8 The while loop structure





### **Figure 5.10** Sorting the list Fred, Alex, Diana, Byron, and Carol alphabetically





# Figure 5.9 The repeat loop structure





# Figure 5.11 The insertion sort algorithm expressed in pseudocode

# $\begin{array}{l} \textbf{procedure Sort (List)} \\ \textbf{N} \leftarrow 2; \\ \textbf{while (the value of N does not exceed the length of List) do \\ (Select the Nth entry in List as the pivot entry; \\ Move the pivot entry to a temporary location leaving a hole in List; \\ \textbf{while (there is a name above the hole and that name is greater than the pivot) do \\ (move the name above the hole down into the hole leaving a hole above the name) \\ Move the pivot entry into the hole in List; \\ \textbf{N} \leftarrow \textbf{N} + 1 \end{array}$



#### Recursion

- The execution of a procedure leads to another execution of the procedure.
- Multiple activations of the procedure are formed, all but one of which are waiting for other activations to complete.



# **Figure 5.13** A first draft of the binary search technique

#### if (List empty)





## Figure 5.12 Applying our strategy to search a list for the entry John

Alice Bob Carol David Elaine Fred George Harry Irene John Kelly Larry Mary Nancy	Original list	First sublist	Second sublist
Oliver _ Oliver	Alice Bob Carol David Elaine Fred George Harry Irene John Kelly Larry Mary Nancy Oliver	Irene John Kelly Larry Mary Nancy Oliver	Irene John Kelly



# Figure 5.14 The binary search algorithm in pseudocode







### Figure 5.16





Search (List Tannethlahue)

that the search failed.) iddle" entry in List to be the TestEnt

> Evelyn Fred

George

(TestEntry)

#### **Algorithm Efficiency**

Figure 5.17

Caurch II ist. Tarr

entry in List to be the TestEn

List

Carol

(TestEntry)

We are here.

dure Search (List TargetUs

entry in List to be the TestE

List

6.38

6.39

- Measured as number of instructions executed
- Big theta notation: Used to represent efficiency classes
  - Example: Insertion sort is in  $\Theta(n^2)$
- Best, worst, and average case analysis



# **Figure 5.18** Applying the insertion sort in a worst-case situation

In tel state	companionio made for caon pivot				Control
list	1st pivot	2nd pivot	3rd pivot	4th pivot	list
Elaine David Carol Barbara Alfred	1 CElaine David Carol Barbara Alfred	3 David 2 Elaine Carol Barbara Alfred	6 Carol David 5 Elaine 4 Barbara Alfred	10 Barbara 9 Carol 9 David 8 Elaine 7 Alfred	Alfred Barbara Carol David Elaine



# Figure 5.20 Graph of the worst-case analysis of the binary search algorithm





# **Figure 5.19** Graph of the worst-case analysis of the insertion sort algorithm





6.3:

#### Software Verification

- Proof of correctness
  - Assertions
    - Preconditions
    - Loop invariants
- Testing



### Chain Separating Problem

- A traveler has a gold chain of seven links.
- He must stay at an isolated hotel for seven nights.
- The rent each night consists of one link from the chain.
- What is the fewest number of links that must be cut so that the traveler can pay the hotel one link of the chain each morning without paying for lodging in advance?



# Figure 5.22 Solving the problem with only one cut





**Figure 5.21** Separating the chain using only three cuts





**Figure 5.23** The assertions associated with a typical while structure

