# Financial Intermediaries, Asset Transformation, and Liquidity 

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September 2012

## Road map of the talk

- Motivations:
- assets' liquidity and their characteristics
- the role for financial intermediaries
- The environment:
- markets; assets; banks
- private information
- Types of equilibria
- banks' portfolios
- asset liquidity and prices
- welfare implications for banks


## Motivations

Imperfect recognizability of an asset's authenticity or true value weakens its usefulness as a payment instrument or collateral.

- During 2007-2008, asset-backed securities became hard to serve as collateral, due to the complexity in these assets that hinders investors to verify their true value.
- Some banknotes ceased to circulate since they were threatened by counterfeits by the 1850s in the U.S.


## Motivations

- Akerlof (1970): goods with lemons problem $\rightarrow$ market failure
- there is a role for middlemen to facilitate trades
- This paper: assets with imperfect recognizability $\rightarrow$ market failure $\rightarrow$ liquidity $\rightarrow$ output

Can financial intermediaries improve aggregate liquidity and welfare in an economy with private information?

## Objectives

- frictions: the quality of real assets is private information.
- liquidity: the role of assets in payments.
(Lagos (2010), Rocheteau (2011), Li and Rocheteau (2010))

To provide a theory of asset liquidity and explore implications for

1. the relationship between assets' characteristics, liquidity, and asset prices;
2. the effects of banks on liquidity and welfare.

## Features of banks

- Asset transformation

- banks' portfolios are public information;
- deposits and bank equity: recognizable means of payment.
- Banks have no informational advantages over individuals - price-quantity schedules in the asset market: screening assets' quality.


## Main insights

Can banks' screening eliminate the private information problem?

$\searrow$
no
to signal, good assets may
be held but not spent
$\downarrow$
good assets are subject to an endogenous liquidity constraint
$\downarrow$
lower aggregate liquidity

## Related literature

- Liquidity constraints:

Kiyotaki and Moore (2005, 2008), Lester et al. (2008), Li and Rocheteau (2010), Tomura (2010).

- The recognizability of assets:

Lester et al. (2008), Green and Weber (1996), Nosal and Wallace (2007), Rocheteau (2011).

- Bank liabilities serve as payments:

Gorton and Pennacchi (1990), Williamson (1999).

## The environment

- Each period contains a DM and a CM
- DM: decentralized market
- CM: competitive market
- Two types of agents: Buyers and Sellers



## Trades

DM: buyers and sellers meet bilaterally and randomly

- the buyer makes a take-it-or-leave-it offer
- output: $x_{1}$
- assets transferred from buyer: $\left(y_{a}, y_{d}, y_{e}\right)$
- buyers: utility $u_{1}\left(x_{1}\right)$; sellers: disutility $c_{1}\left(x_{1}\right)$


## Trades

CM: all agents consume and produce

- each buyer is endowed with $A^{E}$ units of real assets
- one-period-lived assets
- the private signal about the quality of $A^{E}$
- production technology: $x_{2}=h$
- banks open
- portfolio choices: deposits and bank equity
- an asset market opens in late CM

In DM, buyers use assets to make payments
$\triangleright$ deposits and bank equity
$\triangleright$ real assets may be subject to private information problem
$\Rightarrow$ private information regarding means of payment

## Time sequence



## Private information

The quality of real assets:


- The expected value of bad assets is lower than that of good assets.


## Agents' problem in the CM

The value function of a buyer is

$$
W^{b}\left(a, d, e ; k_{j}\right)=\max _{x_{2}, h a^{\prime}, d^{\prime}, e^{\prime}}\left\{x_{2}-h+\beta V_{j,+1}^{b}\left(a^{\prime}, d^{\prime}, e^{\prime}\right)\right\}
$$

s.t. $x_{2}+d^{\prime}+q_{e} e^{\prime}=h+k_{j} a+(1+i) d+k_{e} e+q_{a}^{j,+1}\left(A^{E}-a^{\prime}\right)$

- $k_{j}$ : dividends of asset $j, j \in\{h, \ell\}$; $k_{e}$ : dividends of bank equity; $q_{e}$ : the price of bank equity;
- $i$ : deposit interest rate; $q_{a}^{j,+1}$ : price of asset $j,+1$.
- $V_{j,+1}^{b}\left(a^{\prime}, d^{\prime}, e^{\prime}\right)$ : buyer's value function in the DM of period $t+1$.


## Value function in the DM

$\left(x_{1}, y_{a}, y_{d}, y_{e}\right)$ : the quantity of outputs and transfers of assets.

- The buyer's value function is,

$$
V_{j}^{b}\left(a^{\prime}, d^{\prime}, e^{\prime}\right)=S_{j}\left(a^{\prime}, d^{\prime}, e^{\prime}\right)+k_{j} a+(1+i) d+k_{e} e+W^{b}(0,0,0)
$$

- $S_{j}\left(a^{\prime}, d^{\prime}, e^{\prime}\right)$ : buyer's surplus from trade in the DM
- $S_{j}\left(a^{\prime}, d^{\prime}, e^{\prime}\right) \equiv u_{1}\left[x_{1}\left(y_{a}, y_{d}, y_{e}\right)\right]-k_{j} y_{a}\left(a^{\prime}, d^{\prime}, e^{\prime}\right)$

$$
-(1+i) y_{d}\left(a^{\prime}, d^{\prime}, e^{\prime}\right)-k_{e} y_{e}\left(a^{\prime}, d^{\prime}, e^{\prime}\right)
$$

## Portfolio choices

- All buyers choose the same $d$ and $e$;

$$
\begin{array}{r}
\frac{1-(1+i) \beta}{\beta} \geq \xi S_{h, 2}(a, d, e)+(1-\xi)\left\{\eta\left[S_{h, 2}(a, d, e)+(1-\eta) S_{\ell, 2}(a, d, e)\right]\right\} \\
" \quad "=" \text { if } d>0 \\
\frac{q_{e}-k_{e} \beta}{\beta} \geq \xi S_{h, 3}(a, d, e)+(1-\xi)\left\{\eta\left[S_{h, 3}(a, d, e)+(1-\eta) S_{\ell, 3}(a, d, e)\right]\right\} \\
"=" \text { if } e>0
\end{array}
$$

- $q_{a}^{j}$ : determined by banks' problem in the asset trade.

$$
\begin{aligned}
& \frac{q_{a}^{h}-k_{h} \beta}{\beta} \geq S_{h, 1}(a, d, e) \quad "=" \text { if } a_{h}>0 . \\
& \frac{q_{a}^{\ell}-k_{\ell} \beta}{\beta} \geq S_{\ell, 1}(a, d, e) \quad "=" \text { if } a_{\ell}>0 .
\end{aligned}
$$

## Banks' flow of funds

- Source of funds: deposits, equity, and dividends from bank assets
- Use of funds: investments, dividend and interest payments
- Flow of funds in period $t$ is

$$
k_{e} E+(1+i) D+q_{a}^{h} \Omega_{h}^{\prime}+q_{a}^{\ell} \Omega_{\ell}^{\prime}=D^{\prime}+q_{e} E^{\prime}+\left(k_{h} \Omega_{h}+k_{\ell} \Omega_{\ell}\right) .
$$

- $\Omega_{j}$ : the quantity of asset $j$ banks hold in period $t$.


## Banks' problem in the asset market

Banks want to buy $\omega_{j}$ units of asset $j$, at the price $q_{a}^{j}, j=h, \ell$

$$
\begin{array}{r}
\max _{q_{a}^{h}, q_{a}^{\ell}, \omega_{h}, \omega_{\ell}} \xi\left[-q_{a}^{h} \omega_{h}+\beta k_{h} \omega_{h}\right]+(1-\xi)\left[-q_{a}^{\ell} \omega_{\ell}+\beta k_{\ell} \omega_{\ell}\right] \\
\text { s.t. } \quad q_{a}^{h} \omega_{h}+\beta V_{h}^{b}\left(a_{h}, d, e ; k_{h}\right) \geq \beta V_{h}^{b}\left(A^{E}, d, e ; k_{h}\right), \\
\\
q_{a}^{\ell} \omega_{\ell}+\beta V_{\ell}^{b}\left(a_{\ell}, d, e ; k_{\ell}\right) \geq \beta V_{\ell}^{b}\left(A^{E}, d, e ; k_{\ell}\right) \\
q_{a}^{h} \omega_{h}+\beta V_{h}^{b}\left(a_{h}, d, e ; k_{h}\right) \geq q_{a}^{\ell} \omega_{\ell}+\beta V_{h}^{b}\left(a_{\ell}, d, e ; k_{h}\right) \\
q_{a}^{\ell} \omega_{\ell}+\beta V_{\ell}^{b}\left(a_{\ell}, d, e ; k_{\ell}\right) \geq q_{a}^{h} \omega_{h}+\beta V_{\ell}^{b}\left(a_{h}, d, e ; k_{\ell}\right)  \tag{5}\\
q_{a}^{h}, q_{a}^{\ell} \geq 0, \omega_{h} \leq A^{E}, \omega_{\ell} \leq A^{E} .
\end{array}
$$

- Condition (1)-(2): participation constraints.
- Condition (3)-(4): incentive compatibility constraints.


## Algorithm to find an equilibrium

Strategy to pin down equilibrium:

1. conjecture a possible portfolio
2. check if the portfolio optimizes agents' and banks' problems in the CM
3. agents' and banks' portfolio choices; market clearing conditions $\rightarrow a_{h}, a_{\ell}, d, e, q_{a}^{h}, q_{a}^{\ell}, q_{e}, i, k_{e}$
4. bargaining in the DM $\rightarrow$ terms of trade: $\left(x_{1}, y_{a}, y_{d}, y_{e}\right)$

## Types of equilibria

- Banks solve the private information problem:

1. banks buy all of good assets and zero or some bad assets
2. banks buy all of bad assets and zero or some good assets

- Banks do not solve the private information problem:

3. banks buy more good assets than bad ones
4. banks buy more bad assets than good ones
5. banks buy the same quantity of good and bad assets $\Rightarrow$ real assets which serve as payments in the DM are threatened by private information problem

## Buyers' offer without private information

Any offer made by a buyer who does not sell all of real assets to banks is,

$$
\begin{array}{r}
\max _{x_{1}^{j}, y_{2}^{j}, y_{d}^{j}, y_{e}^{j}}\left[u_{1}\left(x_{1}\right)-k_{j} y_{a}-(1+i) y_{d}-k_{e} y_{e}\right] \\
\text { s.t. }-c_{1}\left(x_{1}\right)+k_{j} y_{a}+(1+i) y_{d}+k_{e} y_{e} \geq 0 \\
y_{a} \leq a_{j}, \quad y_{d} \leq d, \quad y_{e} \leq e
\end{array}
$$

Any offer made by a buyer who sells all of his real assets to banks is,

$$
\begin{array}{r}
\max _{x_{1}^{-j}, y_{d}^{-j}, y_{e}^{-j}}\left[u_{1}\left(x_{1}\right)-(1+i) y_{d}-k_{e} y_{e}\right] \\
\text { s.t. }-c_{1}\left(x_{1}\right)+(1+i) y_{d}+k_{e} y_{e} \geq 0 \\
y_{d} \leq d, \quad y_{e} \leq e
\end{array}
$$

## Proposition 1 (Asset prices)

When banks buy all one type of assets, deposits, bank equity and real assets have the same liquidity, and $\frac{k_{e}}{q_{e}}=1+i$.

1. If banks buy all good assets, then $q_{a}^{h}>q_{a}^{\ell}$.
2. If banks buy all bad assets and $\frac{\sigma_{\ell} k_{\ell}}{\sigma_{h} k_{h}}>1$, then

$$
q_{a}^{\ell}>q_{a}^{h}-\beta\left(k_{h}-k_{\ell}\right)
$$

where $\sigma_{j} \equiv \frac{u_{1}^{\prime}\left(x_{1}^{j}\right)}{c_{1}^{\prime}\left(x_{1}^{\prime}\right)}-1$. Moreover, when $k_{h}$ is large enough such that $\frac{\sigma_{\ell} k_{\ell}}{\sigma_{h} k_{h}}<1$, then banks buy good assets at a higher price, i.e., $q_{a}^{h}>q_{a}^{\ell}$.

## Buyers' offer under private information

Any offer made by a buyer with good assets is such that

$$
\begin{array}{r}
\max _{x_{1}^{h}, y_{a}^{h}, y_{d}^{h}, y_{e}^{h}}\left[u_{1}\left(x_{1}\right)-k_{h} y_{a}-(1+i) y_{d}-k_{e} y_{e}\right] \\
\text { s.t. }-c_{1}\left(x_{1}\right)+k_{h} y_{a}+(1+i) y_{d}+k_{e} y_{e} \geq 0, \\
u_{1}\left(x_{1}\right)-k_{\ell} y_{a}-(1+i) y_{d}-k_{e} y_{e} \leq u_{1}\left(x_{1}^{\ell}\right)-c_{1}\left(x_{1}^{\ell}\right), \\
y_{a} \leq a_{h}, y_{d} \leq d, y_{e} \leq e . \tag{9}
\end{array}
$$

- In eqm, condition (7) holds with equality because buyers make take-it-or-leave-it offers;
- condition (8) holds with equality to prevent imitating.


## Proposition 2 (The pecking-order payment arrangement)

The buyer $h$ 's offer, $\left(x_{1}^{h}, y_{a}^{h}, y_{d}^{h}, y_{e}^{h}\right)$, has the following properties:

- If $(1+i) d+k_{e} e<c_{1}\left(x_{1}^{*}\right)$, then

$$
\begin{gathered}
y_{d}^{h}=d \\
y_{e}^{h}=e
\end{gathered}
$$

And $\left(x_{1}^{h}, y_{a}^{h}\right)$ satisfies

$$
\begin{aligned}
k_{h} y_{a}^{h}= & c_{1}\left(x_{1}^{h}\right)-(1+i) d-k_{e} e \\
u_{1}\left(x_{1}^{\ell}\right)-c_{1}\left(x_{1}^{\ell}\right)= & u_{1}\left(x_{1}^{h}\right)-c_{1}\left(x_{1}^{h}\right) \\
& +\left(1-\frac{k_{\ell}}{k_{h}}\right)\left[c_{1}\left(x_{1}^{h}\right)-(1+i) d-k_{e} e\right]
\end{aligned}
$$

where $x_{1}^{\ell}=\min \left\{x_{1}^{*}, c_{1}^{-1}\left[k_{\ell} a_{\ell}+(1+i) d_{\ell}+k_{e} e_{\ell}\right]\right\}$.
Moreover, if $a_{h}>0$, then $x_{1}^{h}<x_{1}^{\ell}$ and $y_{a}^{h}<a_{h}$.

Proposition 2 (con't)

- If $(1+i) d+k_{e} e>c_{1}\left(x_{1}^{*}\right)$, then

$$
\begin{aligned}
x_{1}^{h} & =x_{1}^{*} \\
k_{h} y_{a}^{h}+(1+i) y_{d}^{h}+k_{e} y_{e}^{h} & =c_{1}\left(x_{1}^{*}\right) \\
y_{a}^{h} & =0 .
\end{aligned}
$$

Proposition 3 (The liquidity-price relationship)
When banks do not remove private information problems, good assets are subject to liquidity constraints, and the asset prices are such that $q_{a}^{h}<q_{a}^{\ell}+\beta\left(k_{h}-k_{\ell}\right)$.

## Welfare


eqli.1: banks buy all of good assets, and no bad ones;
eqli.2: banks buy all of bad assets, and no good ones;
eqli.3: banks buy some of good and bad assets.

## Conclusion

- Prices of risky real assets are affected by assets' contributions to trades.
- Good assets face an endogenous liquidity constraint under private information.
$\triangleright$ bank liabilities are preferred means of payment
$\triangleright$ to signal, good real assets may be held but not spent.
- Banks can improve aggregate liquidity and welfare by providing recognizable assets, even if they are not able to verify assets' quality.
- When bank liabilities are backed with high quality real assets, the economy achieves the highest welfare.

