Financial Intermediaries, Asset Transformation, and Liquidity

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# Road map of the talk

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- Motivations:
  - assets' liquidity and their characteristics
  - the role for financial intermediaries
- The environment:
  - markets; assets; banks
  - private information
- Types of equilibria
  - banks' portfolios
  - asset liquidity and prices
  - welfare implications for banks

### **Motivations**

Imperfect recognizability of an asset's authenticity or true value weakens its usefulness as a payment instrument or collateral.

- During 2007-2008, asset-backed securities became hard to serve as collateral, due to the complexity in these assets that hinders investors to verify their true value.
- Some banknotes ceased to circulate since they were threatened by counterfeits by the 1850s in the U.S.

#### **Motivations**

• Akerlof (1970):

goods with lemons problem  $\rightarrow$  market failure

- there is a role for middlemen to facilitate trades
- This paper:

assets with imperfect recognizability  $\rightarrow$  market failure  $\rightarrow$  liquidity  $\rightarrow$  output

Can financial intermediaries improve aggregate liquidity and welfare in an economy with private information?

## Objectives

- frictions: the quality of real assets is private information.
- liquidity: the role of assets in payments.
- (Lagos (2010), Rocheteau (2011), Li and Rocheteau (2010))

To provide a theory of asset liquidity and explore implications for

- 1. the relationship between assets' characteristics, liquidity, and asset prices;
- 2. the effects of banks on liquidity and welfare.

## Features of banks

• Asset transformation



- banks' portfolios are public information;
- deposits and bank equity: recognizable means of payment.
- Banks have no informational advantages over individuals
  price-quantity schedules in the asset market: screening assets' quality.

# Main insights

*Can banks' screening eliminate the private information problem?* 



### Related literature

• Liquidity constraints:

Kiyotaki and Moore (2005, 2008), Lester et al. (2008), Li and Rocheteau (2010), Tomura (2010).

- The recognizability of assets: Lester et al. (2008), Green and Weber (1996), Nosal and Wallace (2007), Rocheteau (2011).
- Bank liabilities serve as payments: Gorton and Pennacchi (1990), Williamson (1999).

## The environment

- Each period contains a DM and a CM
  - DM: decentralized market
  - CM: competitive market
- Two types of agents: Buyers and Sellers



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## Trades

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DM: buyers and sellers meet bilaterally and randomly • the buyer makes a take-it-or-leave-it offer

• output: *x*<sub>1</sub>

- assets transferred from buyer:  $(y_a, y_d, y_e)$
- buyers: utility  $u_1(x_1)$ ; sellers: disutility  $c_1(x_1)$

# Trades

- CM: all agents consume and produce
- each buyer is endowed with  $A^E$  units of real assets
  - one-period-lived assets
  - the private signal about the quality of  $A^E$
- production technology:  $x_2 = h$
- banks open
  - portfolio choices: deposits and bank equity
- an asset market opens in late CM
- In DM, buyers use assets to make payments
  - $\triangleright$  deposits and bank equity
  - real assets may be subject to private information problem
- $\Rightarrow$  private information regarding means of payment

#### Time sequence



## Private information

#### The quality of real assets:



The expected value of bad assets is lower than that of good assets.

#### Agents' problem in the CM

The value function of a buyer is

$$W^{b}(a, d, e; k_{j}) = \max_{x_{2}, h, a', d', e'} \{x_{2} - h + \beta V^{b}_{j, +1}(a', d', e')\}$$

s.t. 
$$x_2 + d' + q_e e' = h + k_j a + (1+i)d + k_e e + q_a^{j,+1}(A^E - a')$$

- *k<sub>j</sub>*: dividends of asset *j*, *j* ∈ {*h*, *ℓ*};
   *k<sub>e</sub>*: dividends of bank equity; *q<sub>e</sub>*: the price of bank equity;
- *i*: deposit interest rate;  $q_a^{j,+1}$ : price of asset j, +1.
- V<sup>b</sup><sub>j,+1</sub>(a', d', e'): buyer's value function in the DM of period t + 1.

### Value function in the DM

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 $(x_1, y_a, y_d, y_e)$ : the quantity of outputs and transfers of assets.

• The buyer's value function is,

$$V_{j}^{b}(a^{'},d^{'},e^{'}) = S_{j}(a^{'},d^{'},e^{'}) + k_{j}a + (1+i)d + k_{e}e + W^{b}(0,0,0)$$

#### Portfolio choices

• All buyers choose the same *d* and *e*;

$$\begin{aligned} \frac{1-(1+i)\beta}{\beta} &\geq \xi S_{h,2}(a,d,e) + (1-\xi) \{\eta [S_{h,2}(a,d,e) + (1-\eta) S_{\ell,2}(a,d,e)]\}, \\ &\quad \text{``=``` if } d > 0. \\ \\ \frac{q_e - k_e \beta}{\beta} &\geq \xi S_{h,3}(a,d,e) + (1-\xi) \{\eta [S_{h,3}(a,d,e) + (1-\eta) S_{\ell,3}(a,d,e)]\}, \\ &\quad \text{``=`` if } e > 0. \end{aligned}$$

•  $q_a^j$ : determined by banks' problem in the asset trade.

$$\begin{aligned} \frac{q_a^h-k_h\beta}{\beta} &\geq S_{h,1}(a,d,e) \quad ``=" \quad if \quad a_h > 0. \\ \frac{q_a^\ell-k_\ell\beta}{\beta} &\geq S_{\ell,1}(a,d,e) \quad ``=" \quad if \quad a_\ell > 0. \end{aligned}$$

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# Banks' flow of funds

- Source of funds: deposits, equity, and dividends from bank assets
- Use of funds: investments, dividend and interest payments
- Flow of funds in period *t* is

$$k_e E + (1+i)D + q_a^h \Omega_h' + q_a^\ell \Omega_\ell' = D' + q_e E' + (k_h \Omega_h + k_\ell \Omega_\ell).$$

•  $\Omega_j$ : the quantity of asset *j* banks hold in period *t*.

#### Banks' problem in the asset market

Banks want to buy  $\omega_j$  units of asset j, at the price  $q_a^j$ ,  $j = h, \ell$ 

$$\max_{\substack{q_a^h, q_a^\ell, \omega_h, \omega_\ell}} \xi[-q_a^h \omega_h + \beta k_h \omega_h] + (1 - \xi)[-q_a^\ell \omega_\ell + \beta k_\ell \omega_\ell]$$
s.t. 
$$q_a^h \omega_h + \beta V_h^b(a_h, d, e; k_h) \ge \beta V_h^b(A^E, d, e; k_h),$$
(1)
$$q_a^\ell \omega_\ell + \beta V_\ell^b(a_\ell, d, e; k_\ell) \ge \beta V_\ell^b(A^E, d, e; k_\ell);$$
(2)
$$q_a^h \omega_h + \beta V_h^b(a_h, d, e; k_h) \ge q_a^\ell \omega_\ell + \beta V_h^b(a_\ell, d, e; k_h),$$
(3)
$$q_a^\ell \omega_\ell + \beta V_\ell^b(a_\ell, d, e; k_\ell) \ge q_a^h \omega_h + \beta V_\ell^b(a_h, d, e; k_\ell);$$
(4)
$$q_a^h, q_a^\ell \ge 0, \omega_h \le A^E, \omega_\ell \le A^E.$$
(5)

- Condition (1)-(2): participation constraints.
- Condition (3)-(4): incentive compatibility constraints.

## Algorithm to find an equilibrium

Strategy to pin down equilibrium:

- 1. conjecture a possible portfolio
- 2. check if the portfolio optimizes agents' and banks' problems in the CM
- 3. agents' and banks' portfolio choices; market clearing conditions  $\rightarrow a_h, a_\ell, d, e, q_a^h, q_a^\ell, q_e, i, k_e$
- 4. bargaining in the DM  $\rightarrow$  terms of trade:  $(x_1, y_a, y_d, y_e)$

# Types of equilibria

- Banks solve the private information problem:
  - 1. banks buy all of good assets and zero or some bad assets
  - 2. banks buy all of bad assets and zero or some good assets
- Banks do not solve the private information problem:
  - 3. banks buy more good assets than bad ones
  - 4. banks buy more bad assets than good ones
  - 5. banks buy the same quantity of good and bad assets

 $\Rightarrow$  real assets which serve as payments in the DM are threatened by private information problem

## Buyers' offer without private information

Any offer made by a buyer who does not sell all of real assets to banks is,

$$\begin{split} \max_{x_1^j, y_a^j, y_d^j, y_e^j} & \left[ u_1(x_1) - k_j y_a - (1+i) y_d - k_e y_e \right] \\ s.t. - c_1(x_1) + k_j y_a + (1+i) y_d + k_e y_e \ge 0, \\ & y_a \le a_j, \ y_d \le d, \ y_e \le e, \end{split}$$

Any offer made by a buyer who sells all of his real assets to banks is,

$$egin{aligned} &\max_{x_1^{-j}, y_d^{-j}, y_e^{-j}} [u_1(x_1) - (1+i)y_d - k_e y_e] \ &s.t. - c_1(x_1) + (1+i)y_d + k_e y_e \geq 0, \ &y_d \leq d, \ y_e \leq e. \end{aligned}$$

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#### Proposition 1 (Asset prices)

When banks buy all one type of assets, deposits, bank equity and real assets have the same liquidity, and  $\frac{k_e}{a_e} = 1 + i$ .

- 1. If banks buy all good assets, then  $q_a^h > q_a^\ell$ .
- 2. If banks buy all bad assets and  $\frac{\sigma_\ell k_\ell}{\sigma_h k_h} > 1$ , then

$$q_a^\ell > q_a^h - eta(k_h - k_\ell),$$

where  $\sigma_j \equiv \frac{u'_1(x_1^j)}{c'_1(x_1^j)} - 1$ . Moreover, when  $k_h$  is large enough such that  $\frac{\sigma_\ell k_\ell}{\sigma_h k_h} < 1$ , then banks buy good assets at a higher price, i.e.,  $q_a^h > q_a^\ell$ .

#### Buyers' offer under private information

Any offer made by a buyer with good assets is such that

$$\max_{x_1^h, y_a^h, y_d^h, y_e^h} [u_1(x_1) - k_h y_a - (1+i)y_d - k_e y_e]$$
(6)

$$s.t. - c_1(x_1) + k_h y_a + (1+i)y_d + k_e y_e \ge 0,$$
 (7)

$$u_1(x_1) - k_\ell y_a - (1+i)y_d - k_e y_e \le u_1(x_1^\ell) - c_1(x_1^\ell), \qquad (8)$$

$$y_a \leq a_h, y_d \leq d, y_e \leq e.$$
 (9)

- In eqm, condition (7) holds with equality because buyers make take-it-or-leave-it offers;
- condition (8) holds with equality to prevent imitating.

Proposition 2 (The pecking-order payment arrangement)

The buyer *h*'s offer,  $(x_1^h, y_a^h, y_d^h, y_e^h)$ , has the following properties:

• If 
$$(1+i)d + k_e e < c_1(x_1^*)$$
, then

$$y_d^h = d,$$
  
 $y_e^h = e.$ 

And 
$$(x_1^h, y_a^h)$$
 satisfies  
 $k_h y_a^h = c_1(x_1^h) - (1+i)d - k_e e,$   
 $u_1(x_1^\ell) - c_1(x_1^\ell) = u_1(x_1^h) - c_1(x_1^h) + (1 - \frac{k_\ell}{k_h})[c_1(x_1^h) - (1+i)d - k_e e],$ 

where  $x_{1}^{\ell} = \min\{x_{1}^{*}, c_{1}^{-1}[k_{\ell}a_{\ell} + (1+i)d_{\ell} + k_{e}e_{\ell}]\}.$ Moreover, if  $a_{h} > 0$ , then  $x_{1}^{h} < x_{1}^{\ell}$  and  $y_{a}^{h} \leq a_{h}$ .

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#### Proposition 2 (con't)

• If  $(1+i)d + k_e e > c_1(x_1^*)$ , then

$$\begin{aligned} x_1^h &= x_1^* \\ k_h y_a^h + (1+i) y_d^h + k_e y_e^h &= c_1(x_1^*) \\ y_a^h &= 0. \end{aligned}$$

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#### Proposition 3 (The liquidity-price relationship)

When banks do not remove private information problems, good assets are subject to liquidity constraints, and the asset prices are such that  $q_a^h < q_a^\ell + \beta(k_h - k_\ell)$ .

#### Welfare



## Conclusion

- Prices of risky real assets are affected by assets' contributions to trades.
- Good assets face an endogenous liquidity constraint under private information.
  - bank liabilities are preferred means of payment
  - $\triangleright\,$  to signal, good real assets may be held but not spent.
- Banks can improve aggregate liquidity and welfare by providing recognizable assets, even if they are not able to verify assets' quality.
- When bank liabilities are backed with high quality real assets, the economy achieves the highest welfare.