

1. Consider altruistic preferences:  $U_i(X) = x_i + \alpha x_{-i}$ 
  - a. Can one use this to explain 50% contribution in the public goods game?
  - b. Can one use this to explain nearly full contribution in the public goods game with punishment?
  - c. Can one use this to explain rejections and fair offers in the ultimatum game?
2. Consider the inequality aversion model of Fehr and Schmidt (1999) having guilt-envy preferences:

$$U_i(X) = x_i - \frac{\alpha}{n-1} \sum_{k \neq i} \max(x_k - x_i, 0) - \frac{\beta}{n-1} \sum_{k \neq i} \max(x_i - x_k, 0).$$

- a. Attempt Question 4 of the 2008 Midterm Exam.
  - b. Demonstrate how such preference can explain rejections in the ultimatum game. (Hint: This is similar to costly punishment after a public goods game.) What about 50-50 offers?
  - c. Can one use this to explain 50-50 or zero offers in the dictator game? What about other offers that were in between?
  - d. Can one use this to explain ultimatum game results with competing proposers (all propose 1-99) or competing respondents (all accepting 99-1)?
3. Consider the fairness equilibrium proposed by Rabin (1993):

Two Players: 1 & 2; Strategy:  $a_i$ ;  $i$ 'th belief about other's strategy :  $b_j (= b_{3-j})$ ;  $i$ 'th belief about other's belief :  $c_i$ . For  $\pi_2(b_2)$  = possible payoffs of 2 given  $b_2$  (belief about 2's action)

equitable(ex:  $\frac{\pi^{\max} + \pi^{\min}}{2}$  excluding Pareto dominated), define **Kindness (of 1 toward 2)** :

$$f_1(a_1, b_2) = \frac{\pi_2(b_2, a_1) - \pi_2^{fair}(b_2)}{\pi_2^{\max}(b_2) - \pi_2^{\min}(b_2)}, f_1 > 0 : \text{kind}; f_1 < 0 : \text{mean}$$

**Perceived kindness (of what 1 think about 2's kindness to her):**

$$\tilde{f}_2(b_2, c_1) = \frac{\pi_1(c_1, b_2) - \pi_1^{fair}(c_1)}{\pi_1^{\max}(c_1) - \pi_1^{\min}(c_1)}$$

**Social Utility function(for 1)**

$$u_1(a_1, b_2, c_1) = \pi_1(a_1, b_2) + \alpha \cdot \tilde{f}_2(b_2, c_1) + \alpha \cdot \tilde{f}_2(b_2, c_1) \cdot f_1(a_1, b_2)$$

Eq. requires  $a_i = b_i = c_i (a_1 = b_1 = c_1, a_2 = b_2 = c_2)$

- a. Can one sustain (C, C) as a fairness equilibrium in the prisoner's dilemma?

|   |                |                |
|---|----------------|----------------|
|   | C              | D              |
| C | 4, 4           | $-\epsilon, 6$ |
| D | $6, -\epsilon$ | 0, 0           |

- b. Can one sustain both (C, C) and (D, D) as fairness equilibria in the chicken game?

|   |        |      |
|---|--------|------|
|   | C      | D    |
| C | -2, -2 | 2, 0 |
| D | 0, 2   | 1, 1 |

- c. Consider an ultimatum offer of (8, 2), and two possible rejection outcomes (0.8, 0.2) and (6,0). Empirical rejection rates are 38% and 19%, respectively. Can fairness equilibrium explain the empirical results? What about guilt-envy preferences?