

Population Uncertainty

- Game theory often assumes fixed-N players
- Not realistic in entry situations:
 - Voter turn-outs,
 - (Travel) congestion games,
 - Online auctions, etc.
- Games with population uncertainty (Myerson, IJGT 1998, GEB 2000, etc.)



- Poisson Games: Assume N ~ Poisson(n)
 - Environmental Equivalence (EE)
 - Independence of Actions (IA)
- Applied to voting games by Myerson (1998)
- Contests: Myerson and Warneryd (2006)
- Other applications?



Research Questions

- 1. Where is a Poisson game relevant?
- 2. How good does Poisson equilibrium fit the data (if there is such application)?
- 3. How did we get to equilibrium? Or, if it doesn't, why don't we get to equilibrium?

Join the Swedish LUPI Game 49 games played daily: Jan. 29 – Mar. 18, 07' Each choose an integer from 1 to K=99999 The person that chooses the <u>lowest unique</u> <u>number</u> wins LUPI: Lowest Unique Positive Integer Fixed Prize: Earn 10,000 Euros if win, 0 if not

Play against approximately 53,783 players
 Assume "approximately 54k" is Poisson(53783)

Why Care?

- LUPI is a part of the economy:
- The Swedish Limbo game
- Lowest unique bid auctions (ongoing research by Eichberger & Vinogradov, Raviv & Virag and Rapoport et al)
- Unique opportunity to test the theory
- Close field-laboratory parallel
- Full vs bounded rationality







Properties of the Unique Equilibrium

- Full support (Otherwise will jump in "gap")
- Decreasing probabilities
 - Lower numbers are preferred by the game
- Concave/convex
 - concave before 1/n; convex after 1/n
- Convergence to uniform with many players
 For any fixed K and n → ∞
- Probabilities \rightarrow 0 with many numbers





















Learning in the Field

- Winning numbers are the only feedback
- Nobody except the winner is reinforced
- Can update beliefs about other's strategy since they don't see the frequencies
- But, people do respond to winning numbers!























The type distribution is Poisson; players' beliefs are a truncated Poisson distribution













Conclusion

- Observe a well-defined game (LUPI) played in the field
- Poisson equilibrium explains the data surprisingly well
- Imitation learning explains convergence
- CH (τ = 2.98) accounts for initial overshooting of low numbers
- Shouldn't we apply population uncertainty to other games?
- LUBA (Least Unique Bid Auctions)