# Coordination協調賽局 

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## Why is Coordination Important?

- Which Equilibrium to Select Among Many?
- This requires Coordination!
- Examples of Coordination in Daily Life:
- Language
- Trading in Markets (Liquidity)
- Industry Concentration


## Why is Coordination Important?

- Equilibrium Selection in Game Theory
- Desirable Features: - Payoff-Dominance, Risk Dominance, etc.
- Convergence via Adaptation / Learning - Weibull (1995), Fudenberg and Levine (1998)
- Empirical: Infer "Selection Principles" by putting people in experiments and observe actual behavior/outcome


## Why is Coordination Important?

- Possible "Selection Principles" :
- Precedent, focal, culture understanding, etc.
- Why are observations useful?
- Schelling (1960, p.164):
- One cannot, without empirical evidence, deduce what understandings can be perceived in a nonzero-sum game of maneuver any more than one can prove, by purely formal deduction, that a particular joke is bound to be funny."


## Why is Coordination Important?

- Can' t Communication Solve This?
- Not always... (See Battle of Sexes below)
- Sometimes communication is not feasible:
- Avoiding Traffic Jams
- Speed Limits (useful because they reduce speed "variance", and hence, enhance coordination!)
- Miscommunication can have big inefficiency!


## Examples of Coordination Impact

- The standard width of US railroad tracks is 4 feet and 8.5 inch Because English wagons were about 5 feet (width of two horses)
- Space Shuttle rockets are smaller than ideal since they need to be shipped back by train...
- Industries are concentrated in small areas - Silicon Valley, Hollywood, Hsinchu Science Park
- Urban Gentrification - I want to live where others (like me) live


## Examples of Coordination Impact

- Drive on the Left (or Right) side of the road - Right: Asia, Europe (Same continent!)
- Left: Japan, UK, Hong Kong (all islands!)
- Sweden switched from left to right around 1900 (and at 12pm noon time!)
- What about America?
- Right: to avoid hitting someone with the whip on your right hand
- Bolivians switch to Left in mountainous area


## 3 Types of Coordination Games

- Matching Games
- Pure Coordination Game
- Games with Asymmetric Payoffs
- Battle of Sexes, Market Entry Game
- Games with Asymmetric Equilibria
- Stag Hunt, Weak-Link Game
- Applications: Market Adoption and Culture


## Examples of Coordination Impact

- Categorizing Products
- Where should you find Narnia? Family or Action?
- Can you find your favorite grocery at a new store?
- Common Language: Internet promotes English
- Some Koreans even get surgery to loosen their tongues, hoping to improve their pronunciation
- Key: Agreeing on something is better than not; but some coordinated choices are better.


## Matching Game

－GAMES magazine（1989）
－Pick one celebrity for President，one for Vice－President
－One person is randomly awarded prize among those who picked most popular one
－林書豪，陳偉殷，林飛帆，陳為廷，謝金燕，黃國昌，魏德聖，雞排妹，王炳忠，張安樂
－Prize？

## Matching Game

- US Results:
- Bill Cosby (1489): successful TV show
- Lee lacocca (1155): possible US candidate
- Pee-Wee Herman (656): successful TV show
- Oprah Winfrey (437): successful TV show
- Shirley MacLaine (196): self-proclaimed reincarnate


## Pure Coordination Game



- Both get 1 if pick the same; both get 0 if not
- Two pure NE, one mixed NE
- Which one will be played empirically?


## Matching Game

- Mehta, Starmer and Sugden (AER 1994)
- Picking Condition (P): Just pick a strategy
- Coordinating Condition (C): Win \$1 if your partner picks the same as you do
- Difference between $P$ and $C=$ How focal
- Choices: Years, Flowers, Dates, Numbers, Colors, Boy's name, Gender, etc.


## Matching Game

## Group P <br> Group C

Category

| Response | $\%$ | Response | $\%$ |
| :---: | :---: | :---: | :---: |
| 1971 | 8.0 | 1990 | 61.1 |
| Rose | 35.2 | Rose | 66.7 |
| Dec. 25 | 5.7 | Dec. 25 | 44.4 |
| 7 | 11.4 | 1 | 40.0 |
| Blue | 38.6 | Red | 58.9 |
| John | 9.1 | John | 50.0 |
| Him | 53.4 | Him | 84.4 |

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## Asymmetric Players: Battle of Sexes



- 100 lottery tickets $=$ $10 \%$ chance to win $\$ 1 / \$ 2$
- Pure NE: $(1,2)$ and $(2,1)$
- Players prefer equilibrium where they play strategy 2
- Mixed NE: $(1 / 4,3 / 4)$ each
- Which would you pick?


## Asymmetric Players: Battle of Sexes

- Cooper, DeJong, Forsythe \& Ross (AER 90')
- BOS: Baseline (MSE mismatch 62.5\%)
- BOS-300: Row player has outside option 300 - Forward induction predicts $(2,1)$
- BOS-100: Row player has outside option 100 - Forward induction doesn't apply
- Compare BOS-100 and BOS-300 shows if "any outside option" works...


## Battle of Sexes (Last 11 Periods)

## Game Outside (1,2) (2,1) Other Total Obs

BOS - $37(22 \%) \quad 31(19 \%) \quad 97(59 \%) \quad 165$
BOS-300 $33 \quad 0(0 \%) \quad 119(90 \%) \quad 13(10 \%) \quad 165$
BOS-100 $3 \quad 5(3 \%) \quad 102(63 \%) 55(34 \%) \quad 165$
BOS-1W
BOS-2W

| 33 | $0(0 \%)$ | $119(90 \%)$ | $13(10 \%)$ |
| :---: | :---: | :---: | :---: |
| 3 | $5(3 \%)$ | $102(63 \%)$ | $55(34 \%)$ |

165
165
BOS-SEQ
165

## Asymmetric Players: Battle of Sexes

- Cooper, DeJong, Forsythe \& Ross (AER 90')
- BOS-1W: 1 way communication by Row
- BOS-2W: 2 way communication by both
- BOS-SEQ: Both know that Row went first, but Column doesn't know what Row did - Information set same as simultaneous move - Would a sequential move act as an coordination device?


## Battle of Sexes (Last 11 Periods)

## Game Outside (1,2) (2,1) Other Total Obs

$$
\begin{array}{cccccc}
\text { BOS } & - & 37(22 \%) & 31(19 \%) & 97(59 \%) & 165 \\
\text { BOS-300 } & 33 & 0(0 \%) & 119(90 \%) & 13(10 \%) & 165 \\
\text { BOS-100 } & 3 & 5(3 \%) & 102(63 \%) & 55_{(34 \%)} & 165 \\
\text { BOS-1W } & - & 1_{(1 \%)} & 158(96 \%) & 6(4 \%) & 165 \\
\text { BOS-2W } & - & 49(30 \%) & 47(28 \%) & 69_{(42 \%)} & 165 \\
\text { BOS-SEQ } & - & 6(4 \%) & 103(62 \%) & 56_{(34 \%)} & 165
\end{array}
$$

## Where Does Meaning Come From?

- Communication can help us coordinate
- But how did the common language for communication emerge in the first place?
- Put people in a situation of no meaning and see how they create it!
- Blume, DeJong, Kim \& Sprinkle (AER 98') - See also BDKS (GEB 2001) which is better!


## Evolution of Meaning



## Evolution of Meaning

- Blume et al. (AER 1998)
- Game 1: Baseline as above
- Game 1NH: See only history of own match
- Game 2: Receiver can choose C (safe action) that gives $(4,4)$ regardless of T1/T2
- Theory: Pooling or Separating Equilibrium


## Percentage Consistent with Separating

## Game \Period <br> 1 <br> 5 <br> 10 <br> 15 <br> 20

1st Session
Game 1
48
65
74
89
95
2nd Session
Game 1
Game 1NH
Game 2
Separating
44
88
88
88
94
Pooling
39
05
00
05
05

## Evolution of Meaning

- Blume et al. (AER 1998)
- Game 2: Receiver can choose C (safe action) that gives $(4,4)$ regardless of $\mathrm{T} 1 / \mathrm{T} 2$
- Game 3: Coordinate payoffs become $(2,7)$ so sender wants to disguise types to force receiver to choose C (safe action)
- Allowed to send 2 or 3 messages...

Results of Game 3: 2 vs. 3 messages \# of Messages $11-10 \quad 11-20 \quad 21-30$ 31-40 $41-50$ 51-60 $\begin{array}{llllll}\text { 2-Separating } & 43 & 53 & 38 & 39\end{array}$ 2-Pooling $\begin{array}{llllll}33 & 34 & 41 & 43 & \text { 2nd Session }\end{array}$

| 3-Separating | 43 | 38 | 33 | 24 |
| :---: | :--- | :--- | :--- | :--- |
| 3-Pooling | 33 | 37 | 42 | 60 |

2-Separating | 39 | 27 | 23 | 24 | 24 | 23 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |

2-Pooling
3-Separating 3-Pooling

61

51
60
25
22
24
63
61 $23 \quad 22$ 55
55
56
57
61

1st Session

## Example of Asymmetric Payoffs

- Market Entry Game
- $n$ players decide to enter a market with capacity $c$
- Payoffs declines as number of entrants increase; $<0$ if number $>c$
- Kahneman (1988): Number close to equil.
- "To a psychologist, it looks like magic."
- See BI-SAW paper by Chen et al. (2012)...


## Market Entry Game Results (Sundali et al. 95'

Market capacity $\begin{array}{lllllllllll}\text { MSE } & 0 & 2.1 & 4.2 & 6.3 & 8.4 & 10.5 & 12.6 & 14.7 & 16.8 & 18.9\end{array}$
$1^{\text {st }}$ block
$\begin{array}{llllllllll}1.3 & 5.7 & 9.7 & 6.7 & 3.7 & 14.0 & 11.3 & 11.3 & 16.0 & 18.0\end{array}$ all data

## Games with Asymmetric Equilibria



## Games with Asymmetric Equilibria

- Cooper et al. (AER 1990)
- CG: Baseline Stag Hunt
- CG-900: Row has outside option 900 each - Forward induction predicts $(2,2)$
- CG-700: Row has outside option 700 each - Forward induction won't work
- CG-1W: 1 way communication by Row
- CG-2W: 2 way communication by both


## Stage Hunt (Last 11 Periods)

## Game Outside (1,1) (2,2) Other Total Obs

CG - $\quad 160(97 \%) \quad 0(0 \%) \quad 5(3 \%) \quad 165$

| CG-900 | 65 | $2(2 \%)$ | $77(77 \%)$ | $21(21 \%)$ | 165 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| CG-700 | 20 | $119(82 \%)$ | $0(0 \%)$ | $26(18 \%)$ | 165 |
| CG-1W | - | $26(16 \%)$ | $88(53 \%)$ | $51(31 \%)$ | 165 |
| CG-2W | - | $0(0 \%)$ | $150(91 \%)$ | $15(9 \%)$ | 165 |

## Weak-link Game: Team Production Example

- Van Huyck, Battalio and Beil (AER 1990)
- Each of you belong to a team
- Each of you can choose effort $X=1-4$ - Spade $=4$, Heart $=3$, Diamond $=2$, Club $=1$
- Earnings depend on your own effort and the smallest effort of your team
- Each person has to do his/her job for the whole team project to fly
- Have you every had such a project team?


## Weak-link Game: Team Production Example

- Payoff $=60+10 * \min \left\{\mathrm{X}_{\mathrm{j}}\right\}-10 *\left(\mathrm{X}_{\mathrm{i}}-\min \left\{\mathrm{X}_{\mathrm{i}}\right\}\right)$


## Team Project Payoff

Cost of Effort $X$

Your X
Smallest $X$ in the team

| 4 | 100 | 80 | 60 | 40 |
| :---: | :---: | :---: | :---: | :---: |
| 3 | - | 90 | 70 | 50 |
| 2 | - | - | 80 | 60 |
| 1 | - | - | - | 70 |

## Weak-link Game: Team Production Example

- What is your choice when...
- Group size $=2$ ?
- Group size $=3$ ?
- Group size $=20$ ?
- Can some kind of communication help coordinate everyone's effort?

